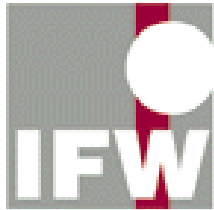


Introduction to Scanning Tunnelling Spectroscopy of correlated materials

Autumn School on Correlated Electrons, 12-16 Sept 2016

Christian Hess



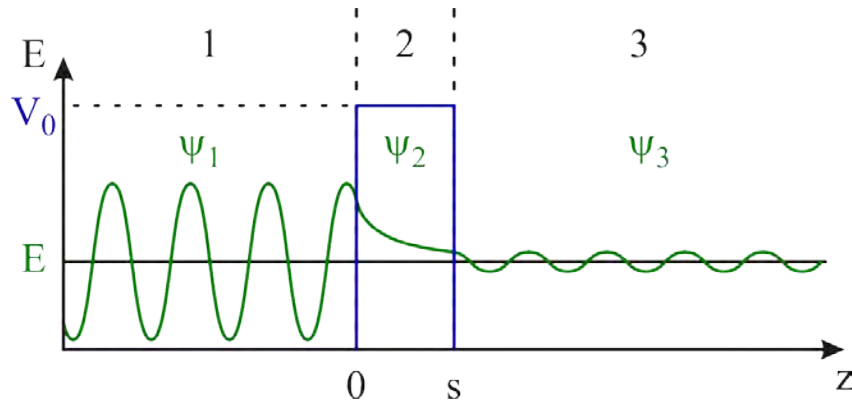
IFW Dresden
Institute for
Solid State Research

Outline

- Electron tunneling
- Iron pnictides
- Gap spectroscopy
- Vortex imaging
- Quasiparticle interference

Electron tunneling

Electron tunneling through a potential barrier



Consider single electron
and a potential barrier in 1D

Time-independent
Schrödinger equation

$$\left(-\frac{\hbar^2}{2m} \frac{d^2}{dz^2} + V(z) \right) \psi(z) = E \psi(z)$$

Free electron solutions in regions 1 and 3

Exponential decay in the barrier

$$\psi_1 = e^{ikz} + Ae^{-ikz}$$

$$\psi_2 = Be^{-\kappa z} + Ce^{\kappa z}$$

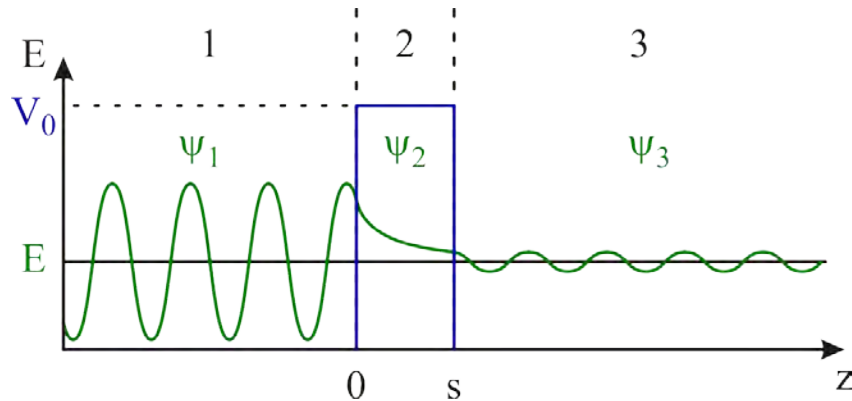
$$\psi_3 = De^{ikz}$$

The electron tunnels through the barrier!

$$k^2 = 2mE/\hbar^2$$

$$\kappa^2 = 2m(V_0 - E)/\hbar^2$$

Electron tunneling through a potential barrier



Consider single electron
and a potential barrier in 1D

Transmission coefficient:
transmitted/incoming amplitudes

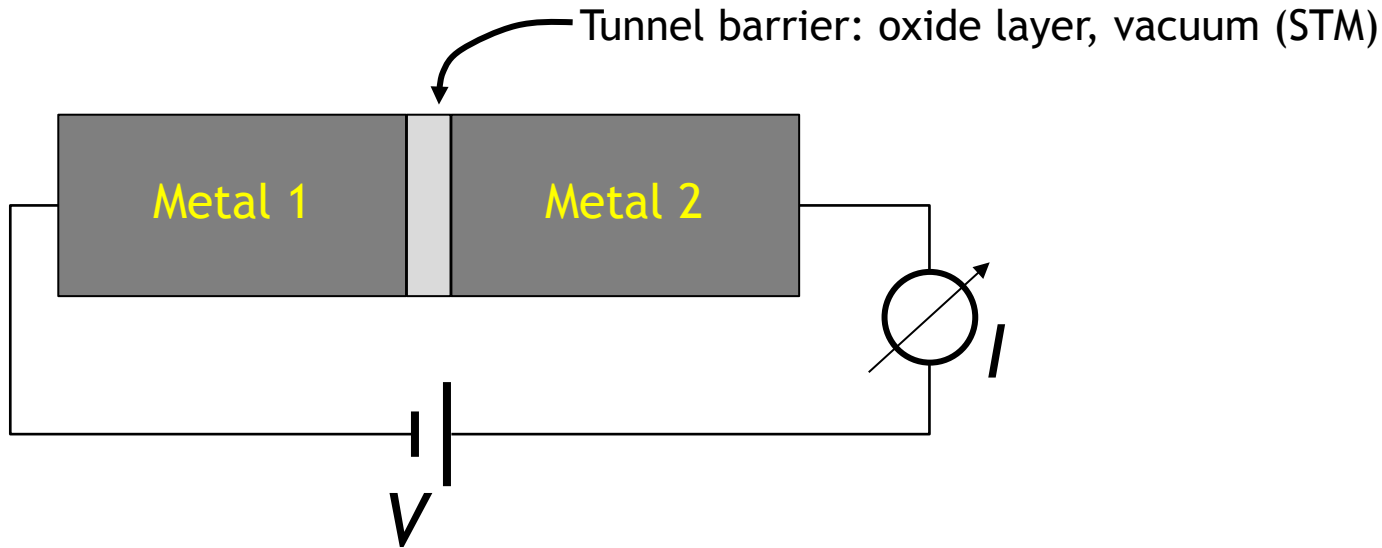
Simplified for wide and high barrier:

$$T \approx \frac{16k^2\kappa^2}{(k^2 + \kappa^2)^2} e^{-2\kappa s}$$

T decays exponentially with the barrier width

Electron tunneling through a potential barrier

Consider planar tunnel junction



General considerations:

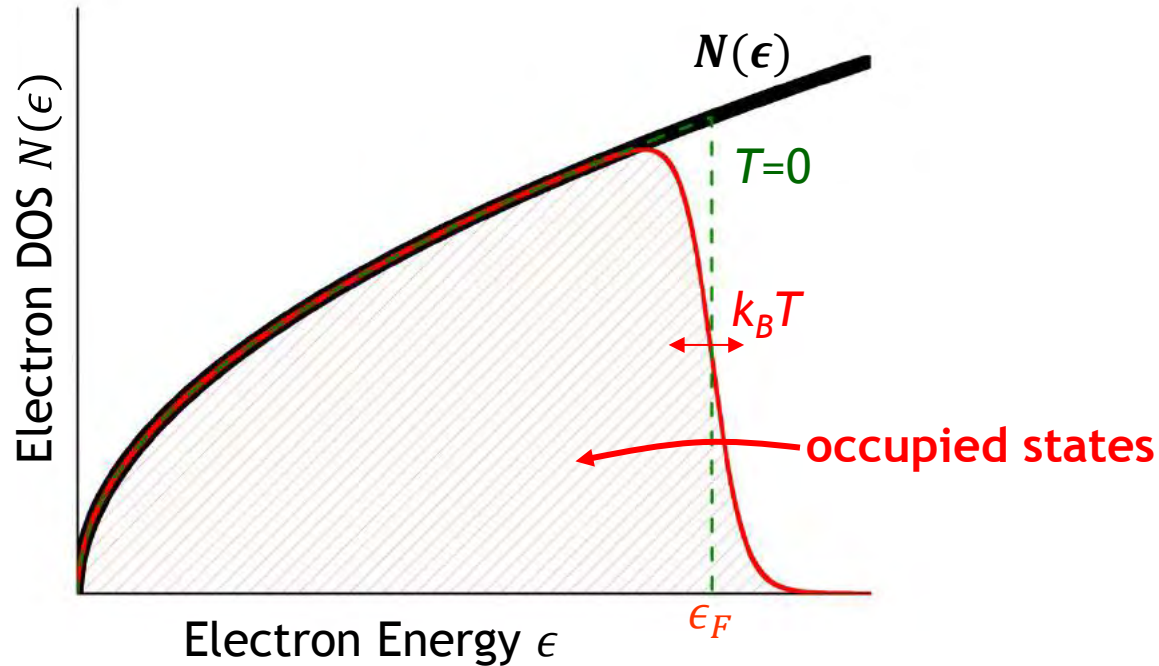
- Tunneling electrons obey Fermi statistics on both sides

$$f(E) = \frac{1}{e^{E/k_B T} + 1}; \quad E = \epsilon - \epsilon_F$$

- Tunneling depends on electronic density of states (DOS) of both electrodes

Electron tunneling through a potential barrier

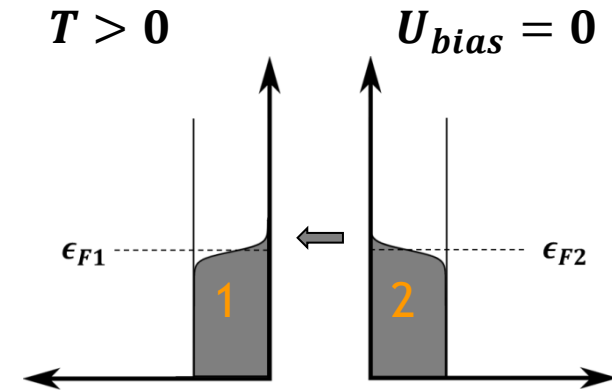
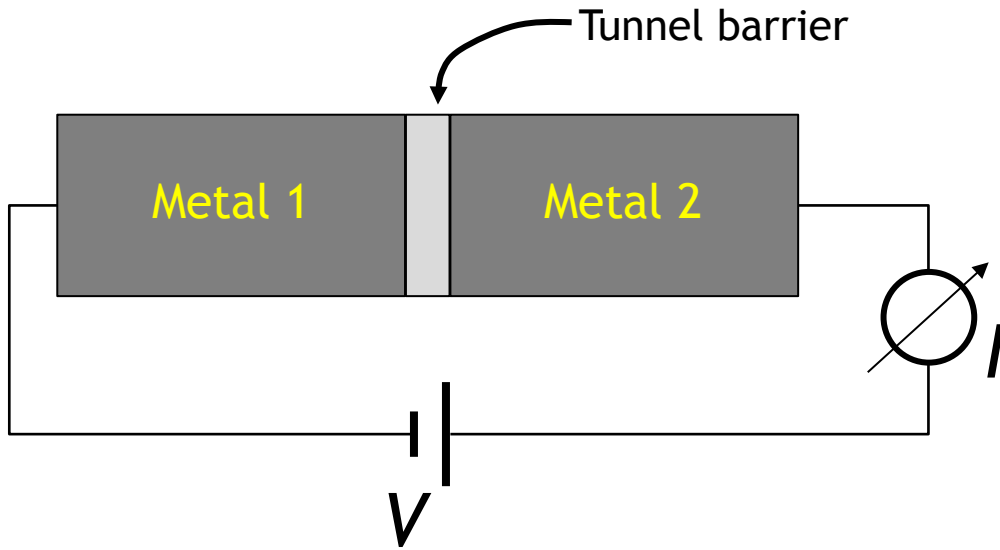
Free electron DOS: $N(\epsilon) \propto \sqrt{\epsilon}$



- Normally $k_B T \ll \epsilon_F$ even at room temperature, since $\epsilon_F/k_B \sim 10^4 \text{K}$
- For most simple metals: $N(\epsilon) \approx \text{const}$ for $\Delta E \sim k_B T$ near ϵ_F

Electron tunneling through a potential barrier

Consider planar tunnel junction¹



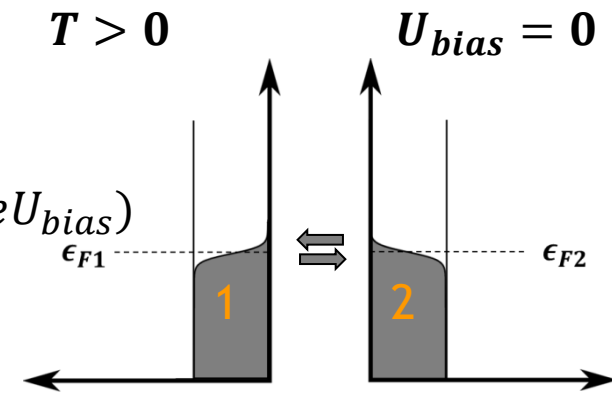
¹Bardeen, PRL 6, 57 (1961)

Electron tunneling through a potential barrier

Consider planar tunnel junction¹

Fermi's Golden Rule:

$$I_{2 \rightarrow 1} = \frac{2\pi e}{\hbar} \sum_{\mu, \nu} \underbrace{f(E_\mu)}_{\text{Occupied states metal 2}} \underbrace{[1 - f(E_\nu - eU_{bias})]}_{\text{Empty states metal 1}} |M_{\mu\nu}|^2 \delta(E_\mu - E_\nu + eU_{bias})$$



Use densities of states N_1 and N_2 :

$$I_{2 \rightarrow 1} = A \int_{-\infty}^{\infty} |M|^2 \underbrace{N_2(E) f(E)}_{\text{Occupied states metal 2}} \underbrace{N_1(E - eU_{bias}) [1 - f(E - eU_{bias})]}_{\text{Empty states metal 1}} dE$$

Opposite current:

$$I_{1 \rightarrow 2} = A \int_{-\infty}^{\infty} |M|^2 N_1(E - eU_{bias}) f(E - eU_{bias}) N_2(E) [1 - f(E)] dE$$

Total: $I = I_{2 \rightarrow 1} - I_{1 \rightarrow 2} = A |M|^2 N_1(0) \int_{-\infty}^{\infty} N_2(E) [f(E) - f(E - eU_{bias})] dE$

I is proportional to integral of N_2 in interval ϵ_F to $\epsilon_F + eU_{bias}$

¹Bardeen, PRL 6, 57 (1961)

Electron tunneling through a potential barrier

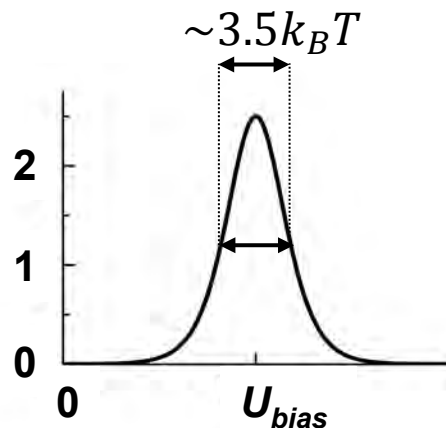
Principle of tunneling spectroscopy:

Measure $I(V)$ in order to obtain N_2 ...

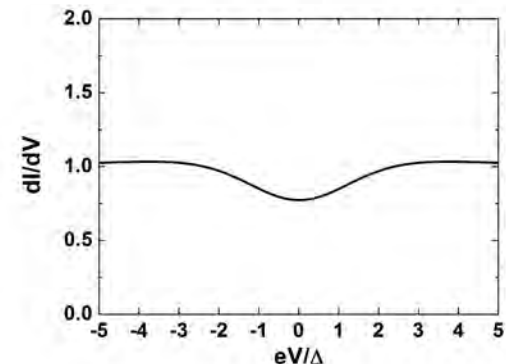
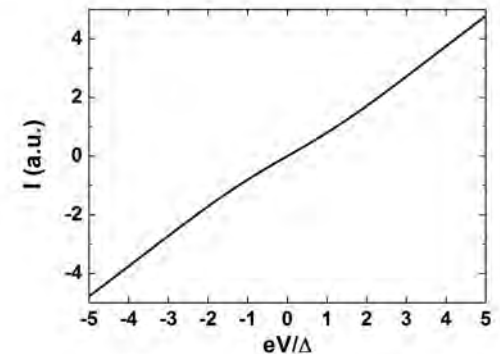
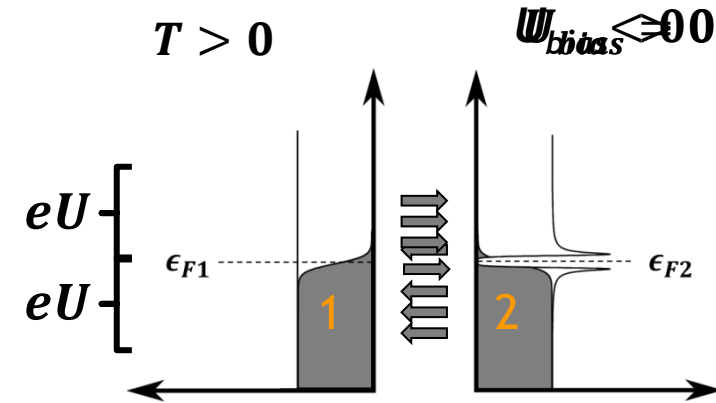
$$I \propto \int_{-\infty}^{\infty} N_2(E) [f(E) - f(E - eU_{bias})] dE$$

... and exploit the differential conductance:

$$\frac{dI}{dU} \propto \int_{-\infty}^{\infty} N_2(E) \left[\underbrace{-\frac{\partial f(E - eU_{bias})}{\partial (eU)}} \right] dE \approx N_2(eU_{bias})$$



Strongly temperature dependent energy resolution!



Electron tunneling through a potential barrier

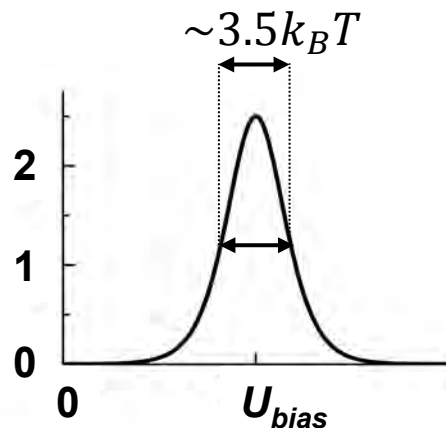
Principle of tunneling spectroscopy:

Measure $I(V)$ in order to obtain N_2 ...

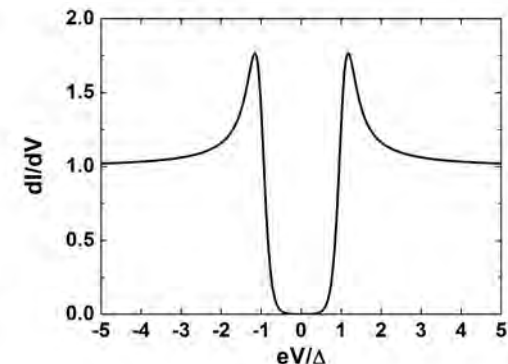
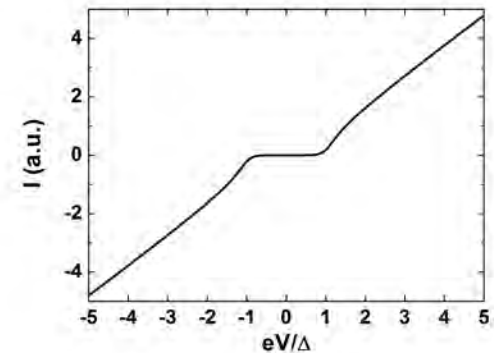
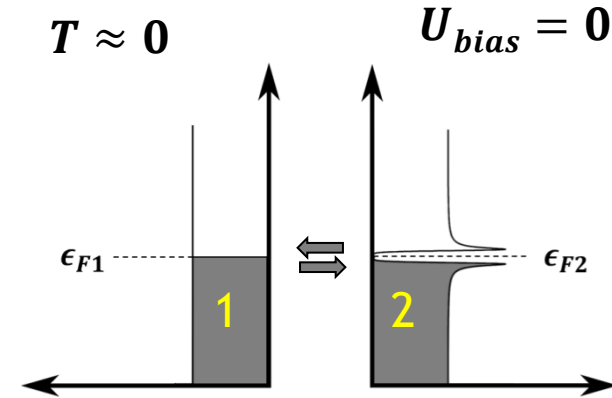
$$I \propto \int_{-\infty}^{\infty} N_2(E) [f(E) - f(E + eV)] dE$$

... and exploit the differential conductance:

$$\frac{dI}{dU} \propto \int_{-\infty}^{\infty} N_2(E) \left[\underbrace{-\frac{\partial f(E - eU_{bias})}{\partial (eU)}} \right] dE \approx N_2(eU_{bias})$$



Strongly temperature dependent energy resolution!



Electron tunneling through a potential barrier

Principle of tunneling spectroscopy:

Measure $I(V)$ in order to obtain N_2 ...

$$I \propto \int_{-\infty}^{\infty} N_2(E) [f(E) - f(E + eV)] dE$$

... and exploit the

$$\frac{dI}{dU} \propto \int_{-\infty}^{\infty} N_2(E)$$

Typical Values:

T = 300 K:

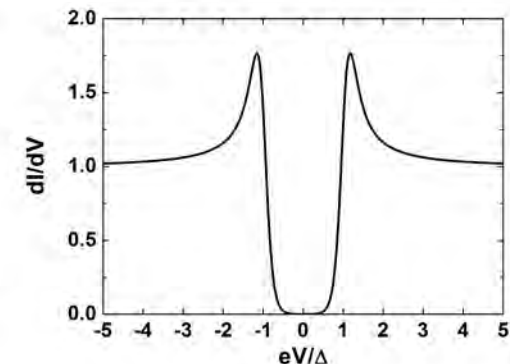
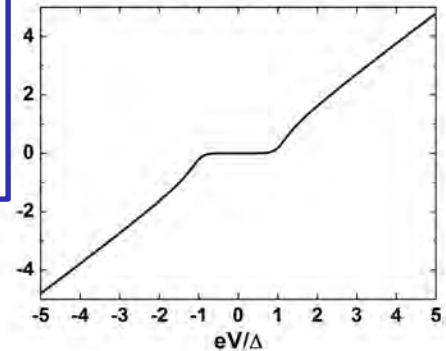
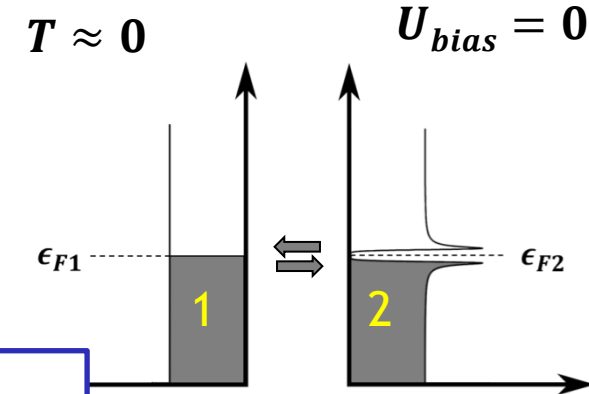
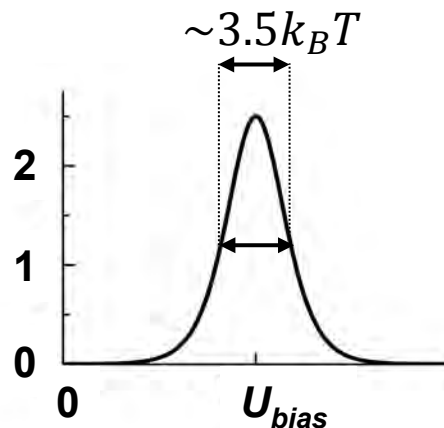
$\Delta E \sim 0.1$ eV

4.2 K:

~ 1.5 meV

300 mK:

~ 100 μ eV



Strongly temperature dependent energy resolution!

Working principle of STM/STS

Electron tunneling through a potential barrier

What is M ?

$$I = A|M|^2 N_1(\mathbf{0}) \int_{-\infty}^{\infty} N_2(E) [f(E) - f(E - eU_{bias})] dE$$

WKB-approximation¹:

$$|M|^2 \propto \exp(-2\gamma) \quad \text{with}$$

$$\gamma = \int_0^s \sqrt{2m\varphi/\hbar^2} dz = \frac{s}{\hbar} \sqrt{2m\varphi}$$

$$\varphi \approx (\Phi_1 + \Phi_2)/2$$

Barrier width

Barrier height

Work functions

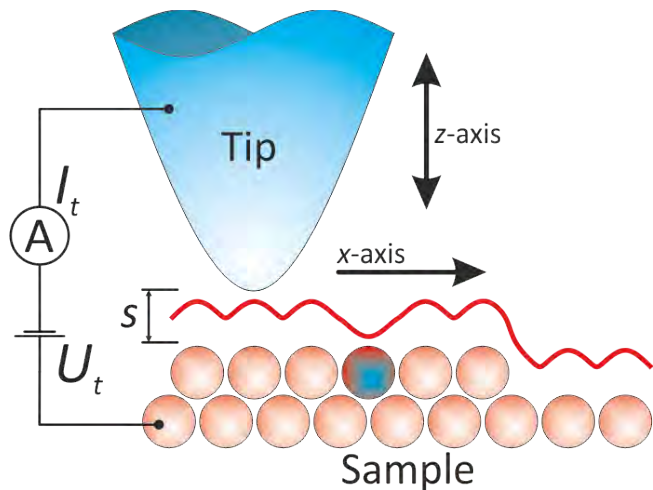


$T \approx 0$;
 $N_1 = \text{const}$

$$I \propto e^{-2\kappa s} \int_0^{eU_{bias}} N_2(E) dE$$

Idea of STM: exploit exponential width dependence...

Scanning Tunneling Microscopy (STM)



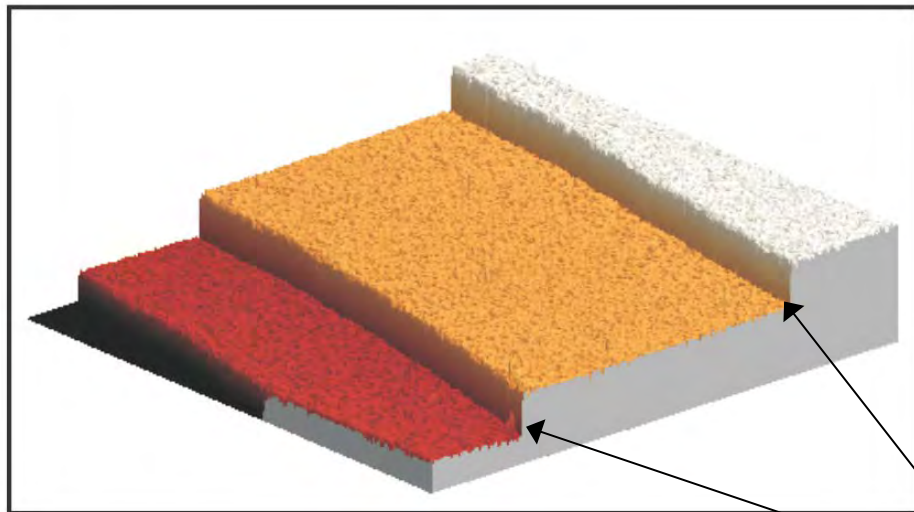
$$T \approx 0$$

$$I_t \propto e^{-2\kappa s} \int_0^{eU_{\text{bias}}} \text{LDOS}_{\text{sample}}(E) dE$$

distance

LDOS: Local Density of States

➔ Topographic surface data



W(110), 200 nm x 200 nm

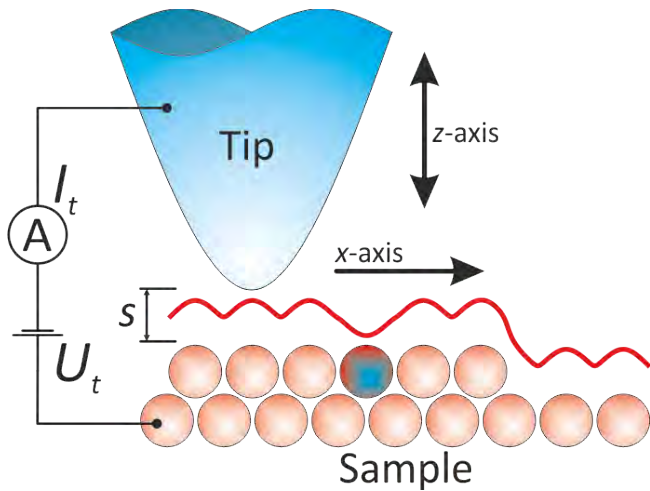
Recipe:

- Set U_{bias} constant
- Require $I_t(z)$ constant
- Measure $z(x, y)$

➔ Map of integrated LDOS

atomic steps

Scanning Tunneling Microscopy (STM)



$$T \approx 0$$

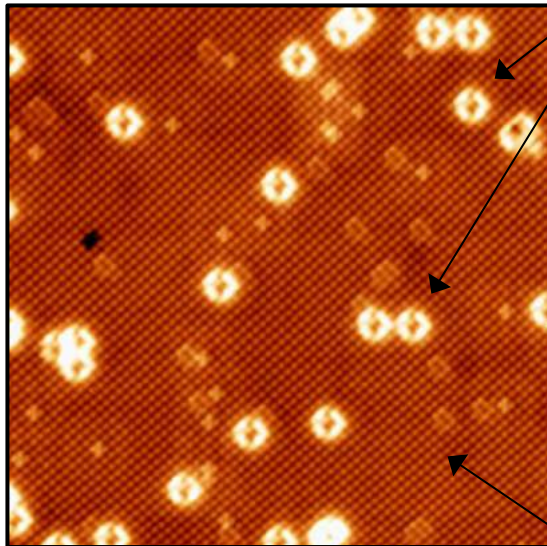
$$I_t \propto e^{-2\kappa s} \int_0^{eU_{\text{bias}}} N_s(E) dE$$

↖ ↖
distance LDOS_{sample}

LDOS: Local Density of States

➔ Topographic surface data

impurity sites



LiFeAs, 35 nm x 35 nm @ 5.5 K

$I_t = 2 \text{ nA}$, $U_{\text{bias}} = -50 \text{ mV}$

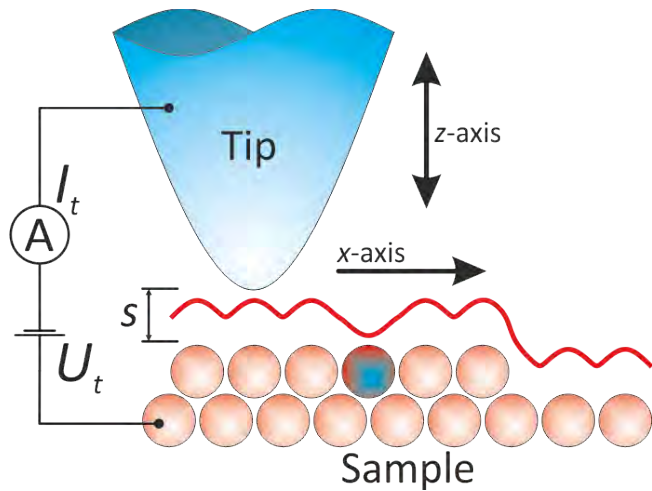
atomic corrugation

Recipe:

- Set U_{bias} constant
- Require $I_t(z)$ constant
- Measure $z(x, y)$

➔ Map of integrated LDOS

Scanning Tunneling Microscopy (STM)



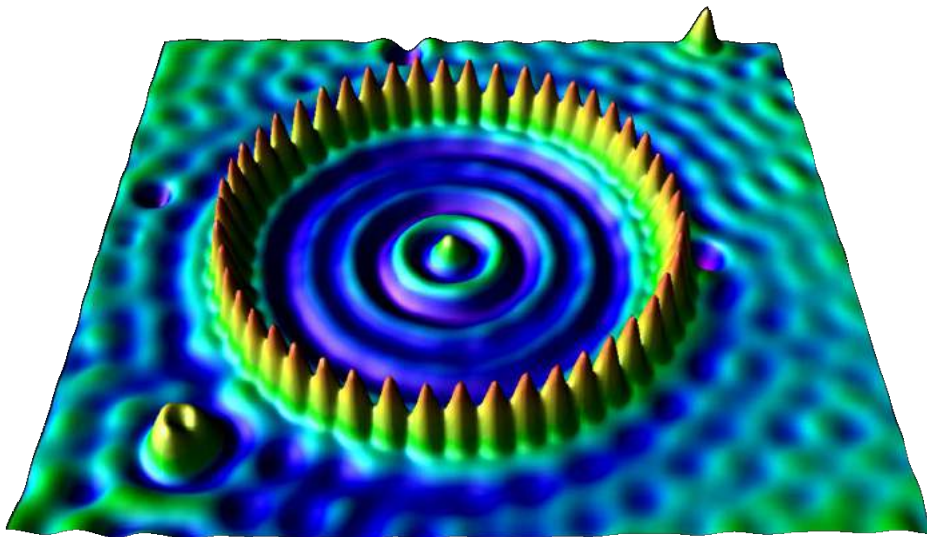
$$T \approx 0$$

$$I_t \propto e^{-2\kappa s} \int_0^{eU_{\text{bias}}} N_s(E) dE$$

↖ LDOS_{sample}
↖ distance

LDOS: Local Density of States

➔ Topographic surface data



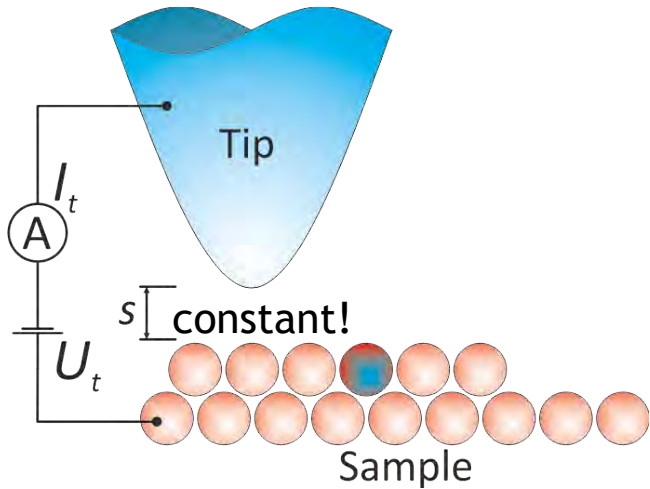
Cu (111) with Fe atom decoration (IBM Almaden Research Center)

Recipe:

- Set U_{bias} constant
- Require $I_t(z)$ constant
- Measure $z(x, y)$

➔ Map of integrated LDOS

Scanning Tunneling Spectroscopy (STS)

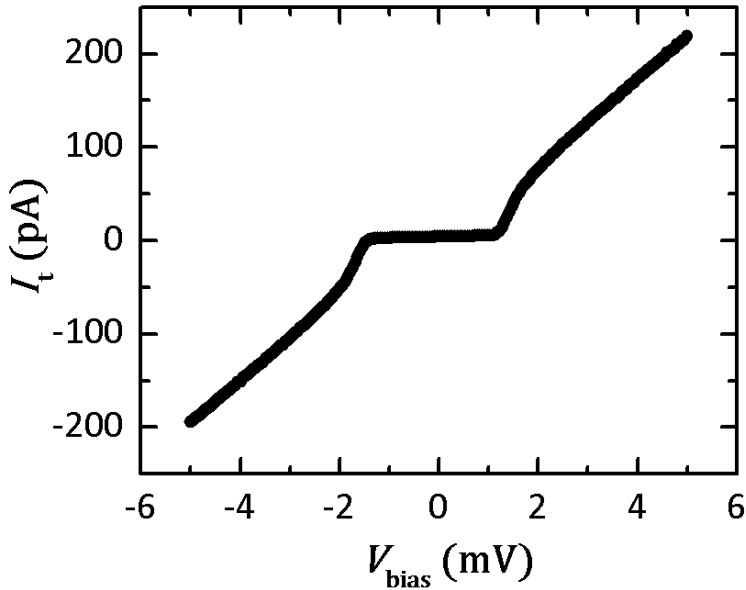


$$T \approx 0$$

$$\textcircled{1} \quad I_t \propto N_t \int_0^{eU_{\text{bias}}} \text{LDOS}_{\text{sample}} N_s(E) dE$$

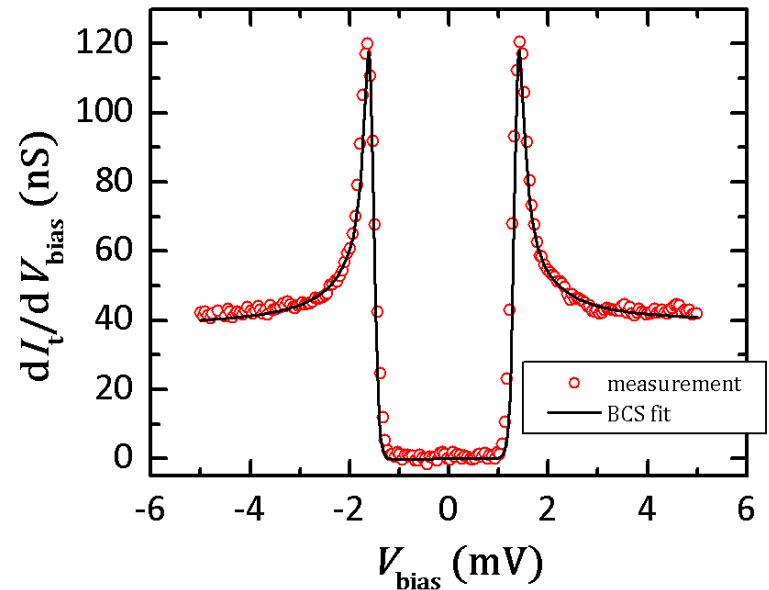
$$\textcircled{2} \quad \frac{dI_t}{dU}(U_{\text{bias}}) \propto N_s(eU_{\text{bias}})$$

$\textcircled{1}$ \rightarrow Local integrated DOS

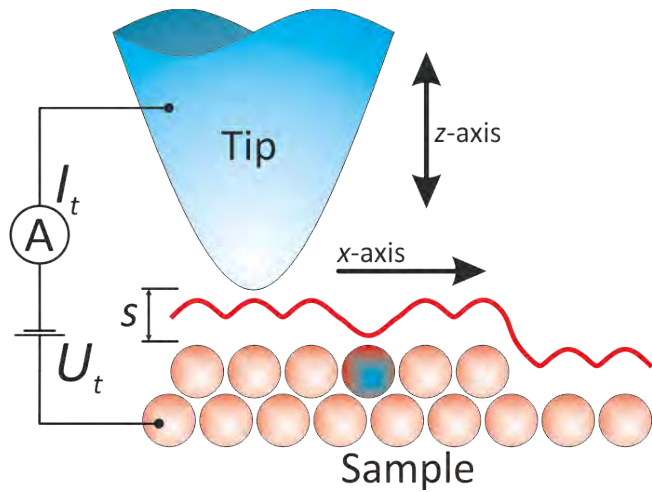


Superconducting Nb@W; T = 378 mK

$\textcircled{2}$ \rightarrow Local DOS $N_s(E)$



Scanning Tunneling Microscopy/Spectroscopy

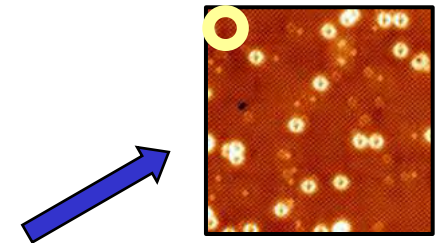


$$T \approx 0$$

$$I_t \propto e^{-2\kappa s} \int_0^{eU_{\text{bias}}} \text{LDOS}_{\text{sample}} N_s(E) dE$$

distance

LDOS: Local Density of States



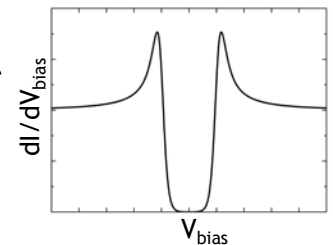
$$I_t = I_t(z) \quad \Rightarrow \quad \text{Topography maps (STM)}$$

$$dI_t/dU_{\text{bias}} \propto \text{LDOS}(E) \quad \Rightarrow \quad \text{LDOS maps (STS)}$$

STS energy resolution: $\sim 4k_B T$

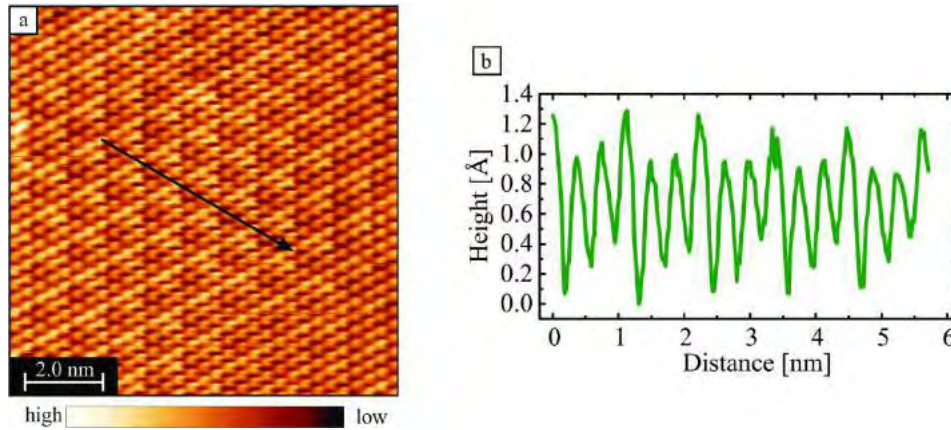
\Rightarrow use low-temperature!

300mK \sim 100 μ eV



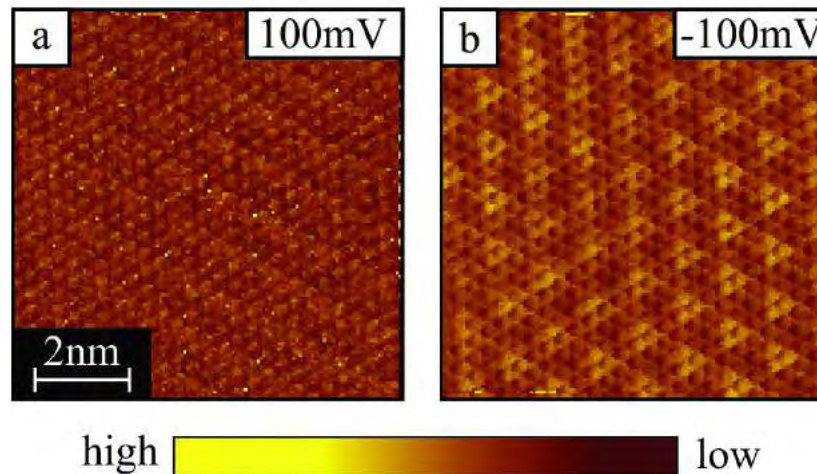
Example: NbSe₂ - Charge Density Wave

Topography

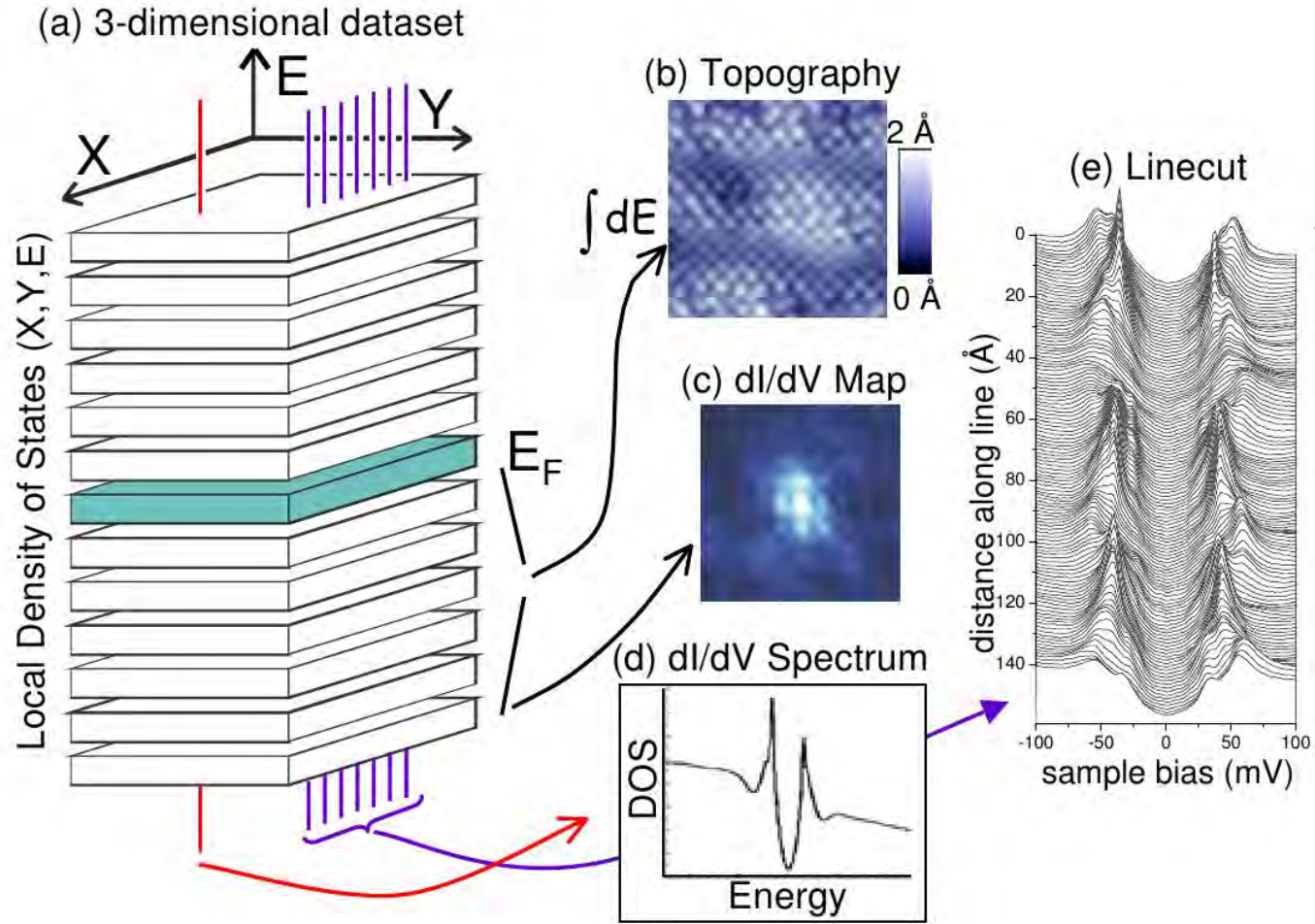


$U_{\text{bias}} = -200 \text{ mV}$, $I = 0.7 \text{ nA}$, $T = 10 \text{ K}$

Spectroscopic maps



Scanning Tunneling Microscopy/Spectroscopy



J. E. Hoffman, PhD thesis (2003)

Acquisition of full data set takes very long!
E.g.: $256 \times 256 \times 10 \text{ s} = 7.5 \text{ d}$

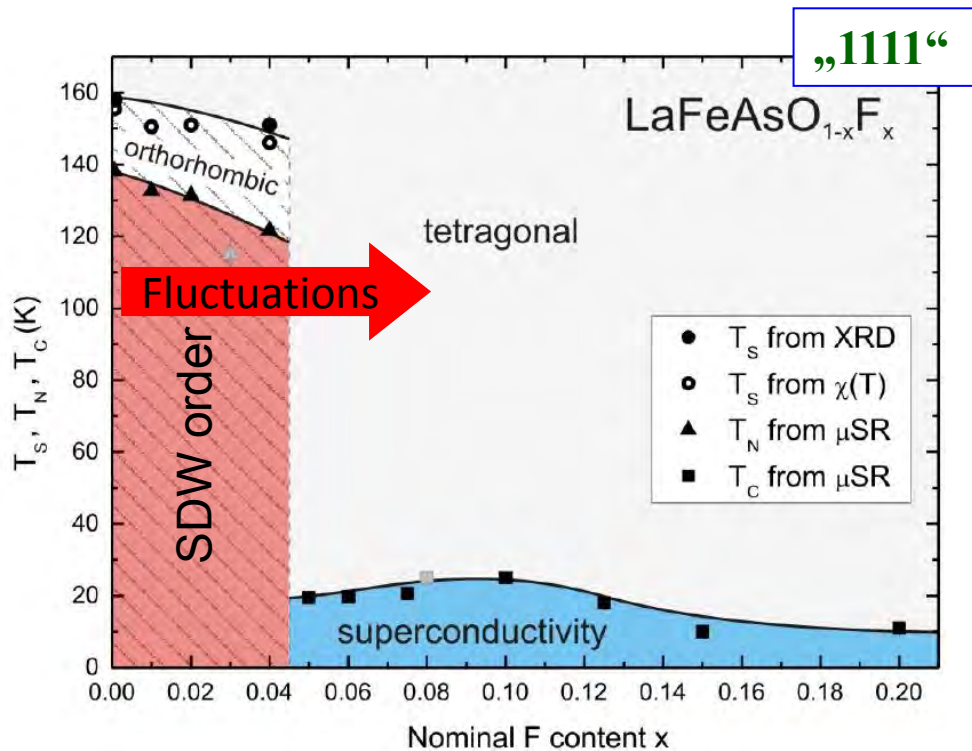


Long term stability required

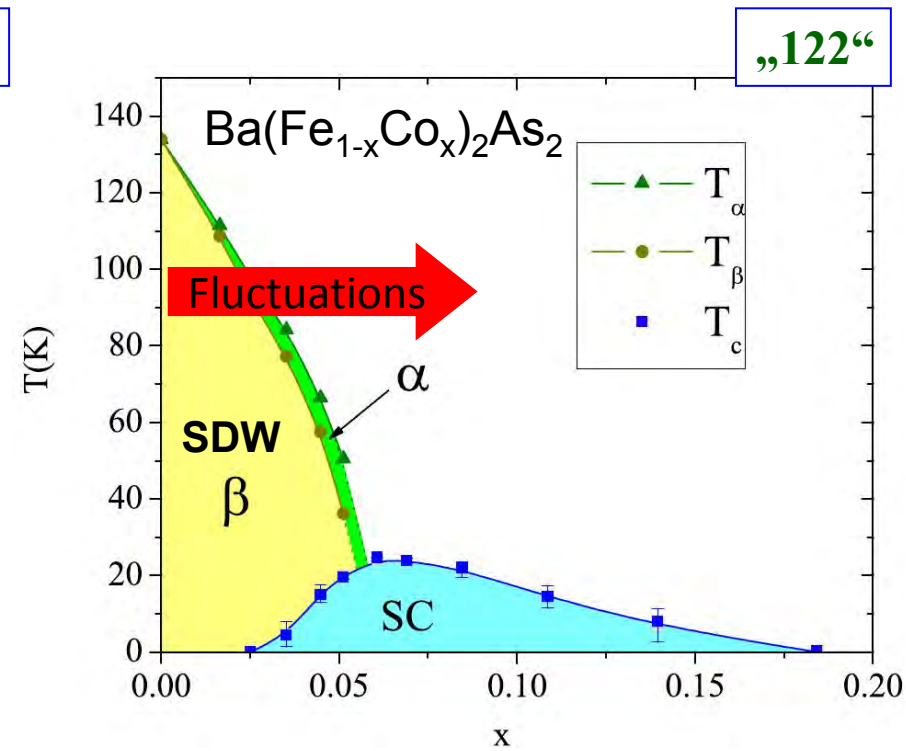
Number of pixels Acquisition time per spectrum

Magnetism vs Superconductivity

Fe pnictides – Magnetism vs Superconductivity



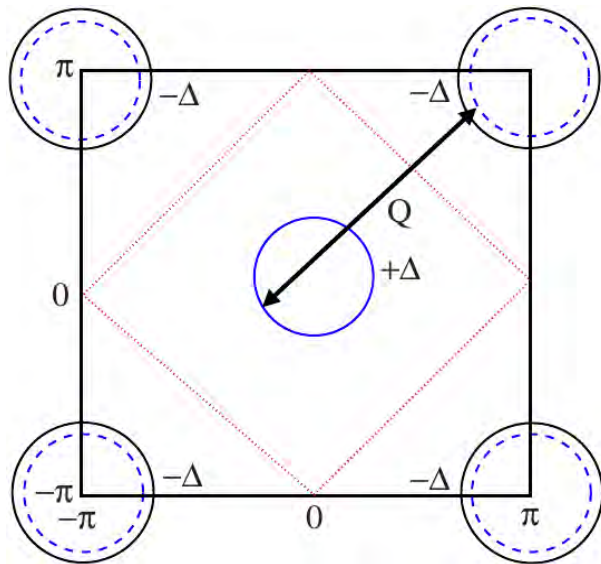
H. Luetkens, ..., CH et al., Nat Mater **8**, 305 (2009)



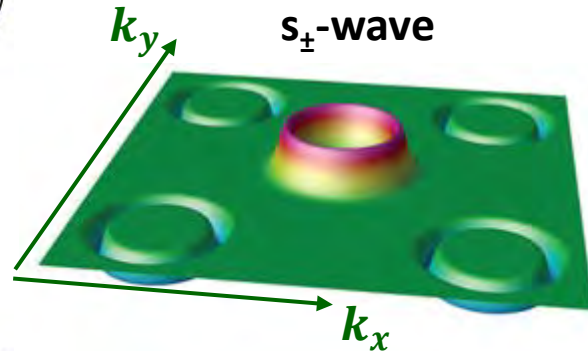
Chu et al., Phys. Rev. B **79**, 014506 (2009)

Unconventional superconductivity?

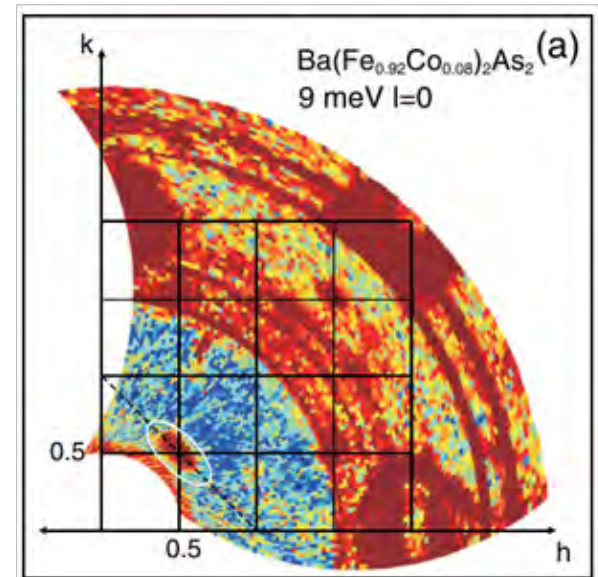
Fe pnictides – Magnetism vs Superconductivity



A. Chubukov et al.,
PRB **78**, 134512 (2008)



I. Mazin, Nature **464**, 183 (2010)



N. Qureshi et al., PRL **108**, 117001 (2012)

“Perfect” nesting of electron- and hole-like Fermi pockets

- ➔ Antiferromagnetic spin fluctuations (Q_{AFM})
- ➔ SDW order

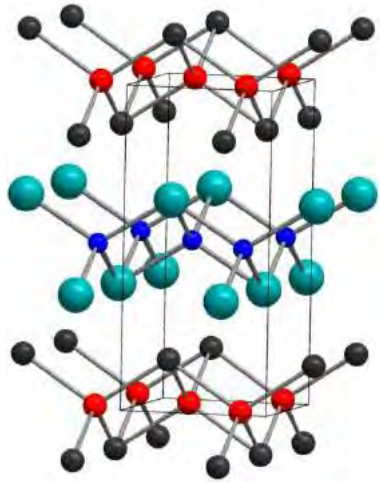
Doping: “Off-tuning” of nesting

➔ Suppression of SDW

Idea: Spin fluctuations drive s_{\pm} -wave superconductivity

I. Mazin, Phys. Rev. Lett. **101**, 057003 (2008)

Fe pnictides: A new class of high T_c superconductors



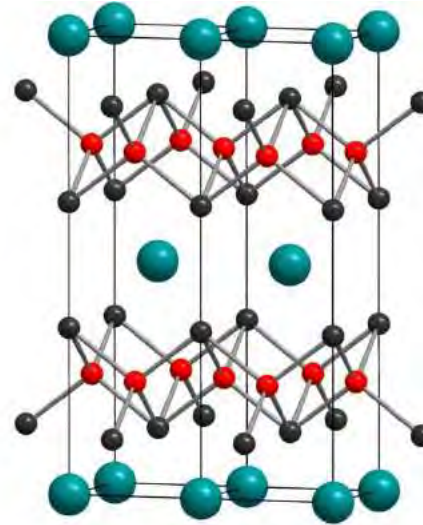
LaFeAsO

„1111“

La, Ce ... Gd-based
AFM parent state

F doped, O defici.

T_c up to 56 K



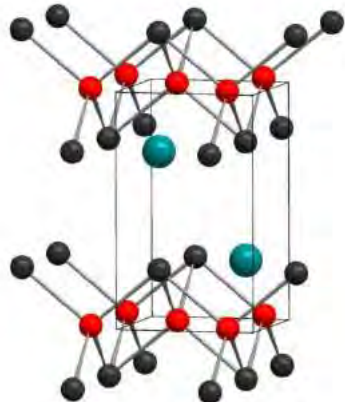
Ba(FeAs)₂

„122“

Ba, Sr, Eu, Ca- based
AFM parent state

K, Na, Co doped

T_c up to 39 K



LiFeAs

„111“

Stoichiometric
superconductor!

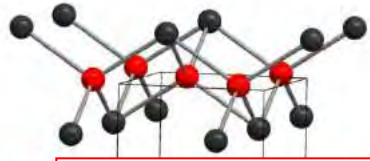


FeSe

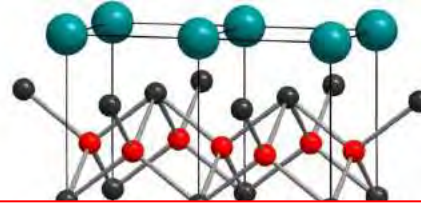
„11“

Stoichiometric
superconductor!

Fe pnictides: A new class of high T_c superconductors

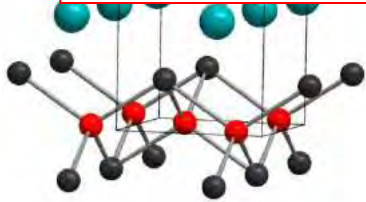


„1111“
La, Ce ... Gd-based
AFM parent state



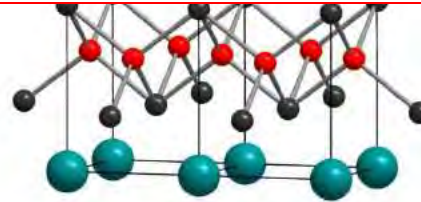
„122“
Ba, Sr, Eu, Ca- based
AFM parent state

Surface State and/or problematic surface



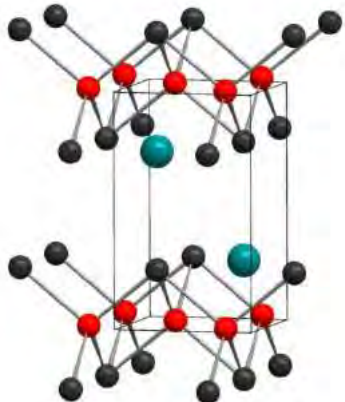
T_c up to 56 K

LaFeAsO



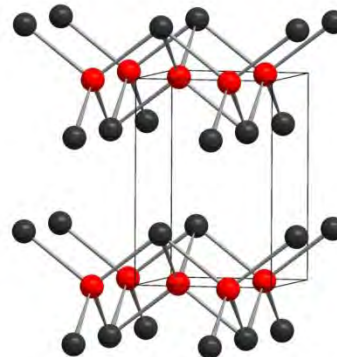
T_c up to 39 K

Ba(FeAs)₂



„111“
Stoichiometric
superconductor!

LiFeAs

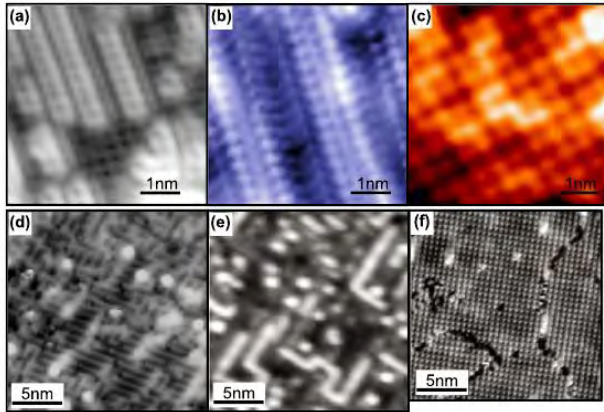


„11“
Stoichiometric
superconductor!

FeSe

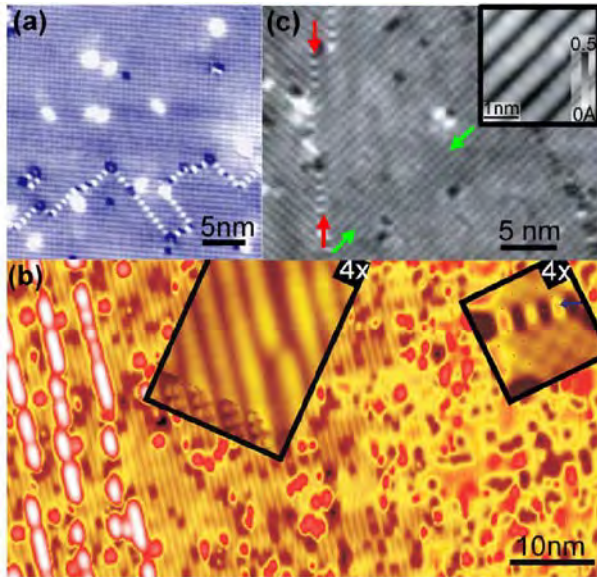
Problematic surfaces in 122 and 1111 systems

122...



BaFe_2As_2
 $\sqrt{2} \times \sqrt{2}$ reconstr.

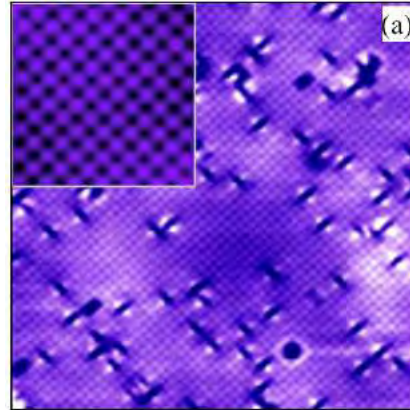
$\text{CaFe}_{1.94}\text{Co}_{0.06}\text{As}_2$
 2×1 reconstr.



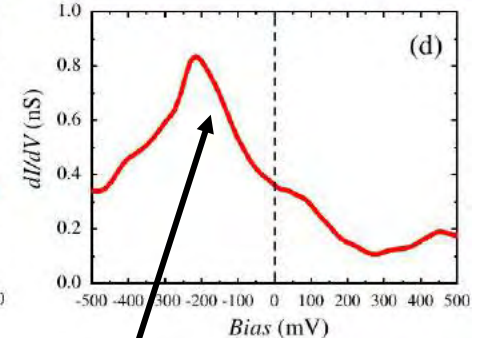
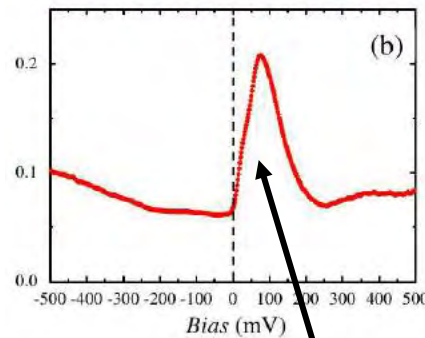
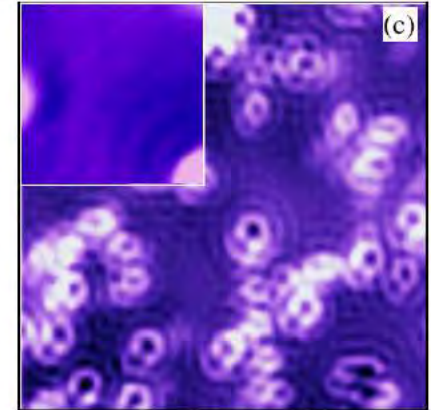
SrFe_2As_2 : $\sqrt{2} \times \sqrt{2} \rightarrow 2 \times 1$ crossover
J.E. Hoffman Rep. Prog. Phys. 74, 124513 (2011)

1111...

LaOFeAs
FeAs layer



LaO layer



X. Zhou et al., PRL 106 087001 (2011)

Surface states!

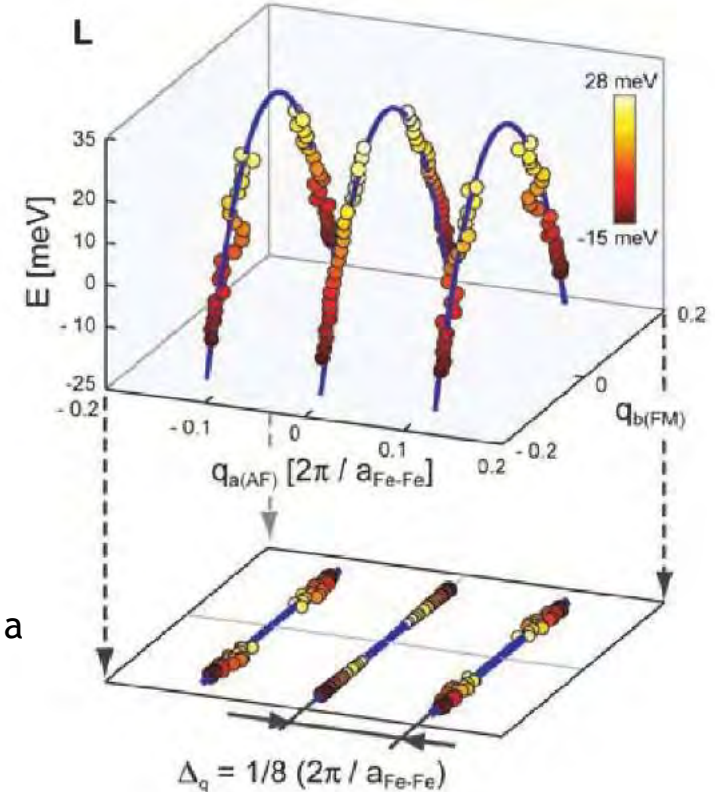
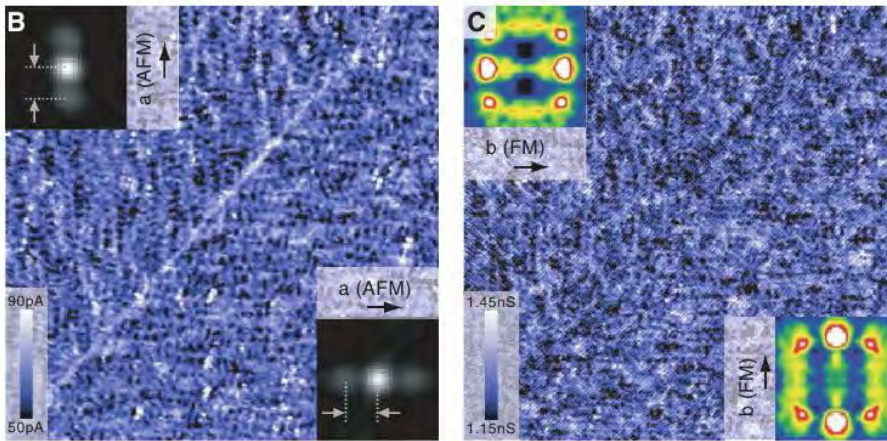
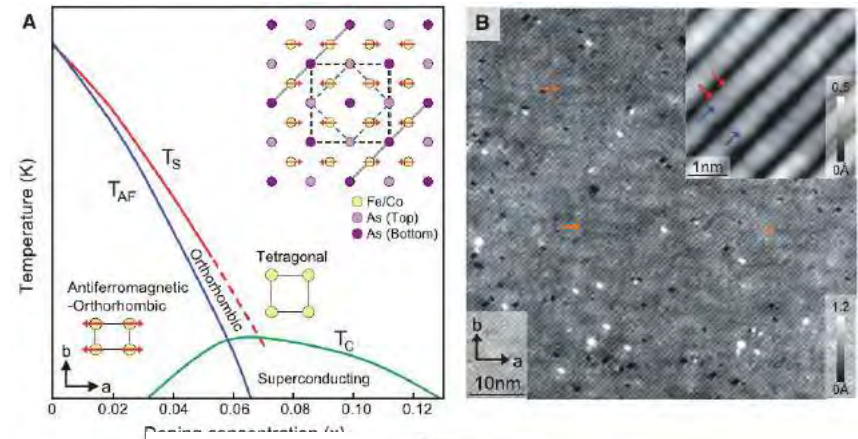
Agrees with DFT calculations:
H. Eschrig et al. PRB 81 155447 (2010)

Evidence for nematicity?

Nematic Electronic Structure in the “Parent” State of the Iron-Based Superconductor $\text{Ca}(\text{Fe}_{1-x}\text{Co}_x)_2\text{As}_2$

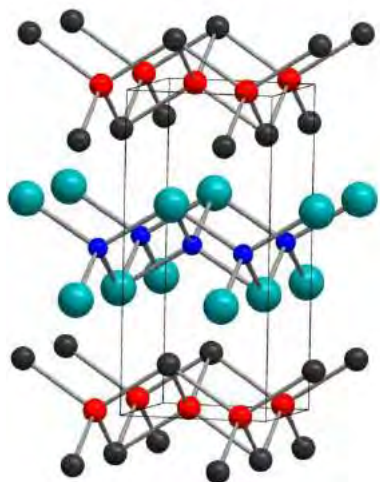
T.-M. Chuang,^{1,2*} M. P. Allan,^{1,3*} Jinho Lee,^{1,4} Yang Xie,¹ Ni Ni,^{5,6} S. L. Bud'ko,^{5,6}
G. S. Boebinger,² P. C. Canfield,^{5,6} J. C. Davis^{1,3,4,7†}

Science 327, 181 (2010)



- Static, unidirectional electronic nanostructures $d=8a_{\text{Fe-Fe}} \parallel a$
- QPI disperses $\parallel b$ axis

Fe pnictides: A new class of high T_c superconductors

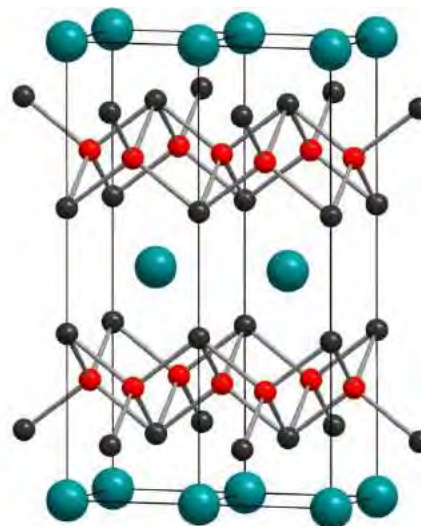


LaFeAsO

„1111“
La, Ce ... Gd-based
AFM parent state

F doped, O defici.

 T_c up to 56 K

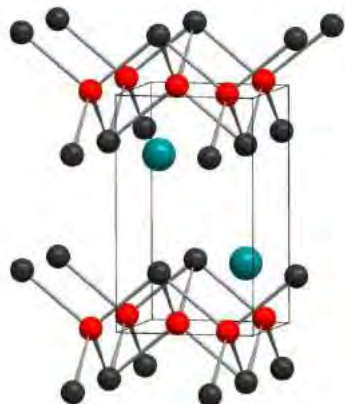


Ba(FeAs)₂

„122“
Ba, Sr, Eu, Ca- based
AFM parent state

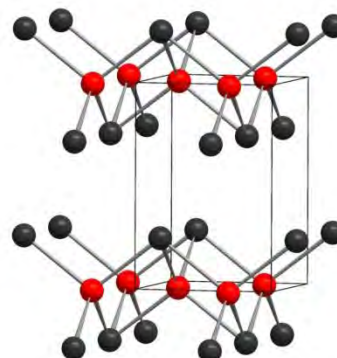
K, Na, Co doped

 T_c up to 39 K



LiFeAs

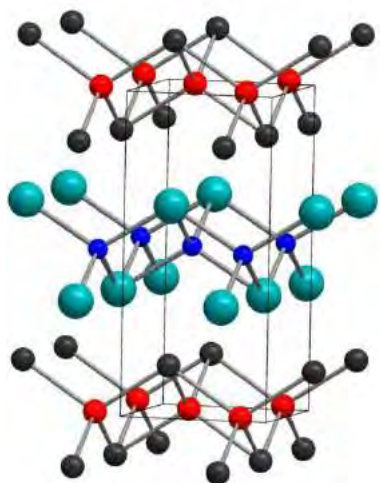
„111“
Stoichiometric
superconductor!



FeSe

„11“
Stoichiometric
superconductor!

Fe pnictides: A new class of high T_c superconductors



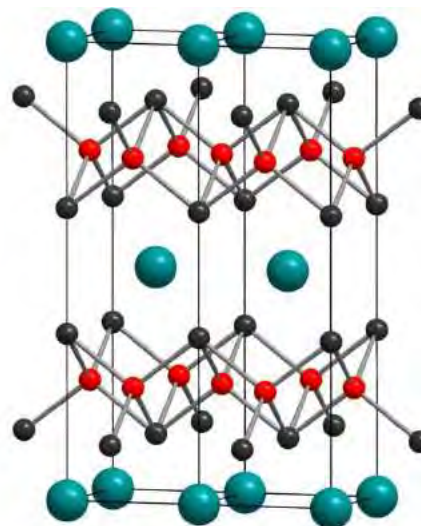
LaFeAsO

„1111“

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AFM parent state

F doped, O defici.

T_c up to 56 K



Ba(FeAs)₂

„122“

Ba, Sr, Eu, Ca- based
AFM parent state

K, Na, Co doped

T_c up to 39 K



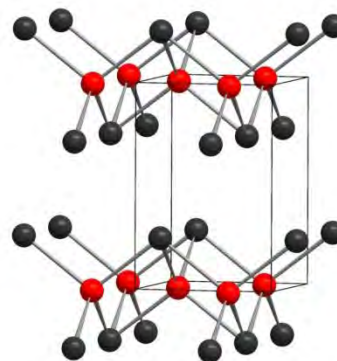
„111“

Stoichiometric
superconductor!

No surface states!

A. Lankau et al., PRB 82, 184518 (2010)

LiFeAs



„11“

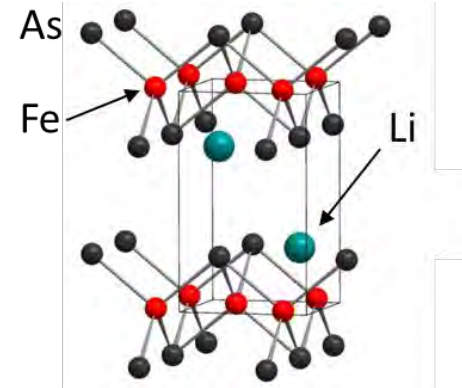
Stoichiometric
superconductor!

FeSe

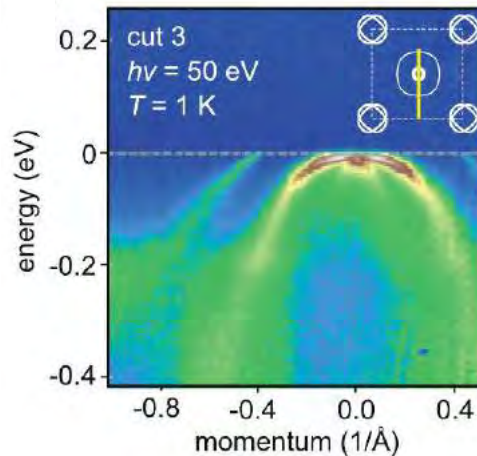
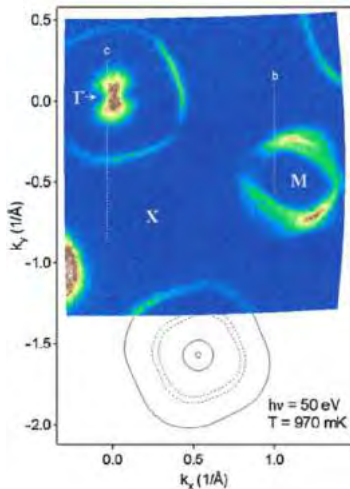
LiFeAs: is it different?

LiFeAs

- Stoichiometric superconductor
- $T_c \sim 18$ K
- No nesting
- High density of states near (0,0)
- Strong e-e-interaction
- No magnetism



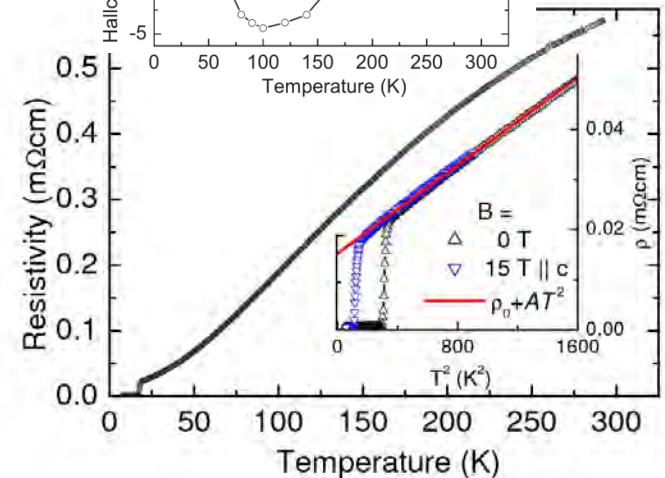
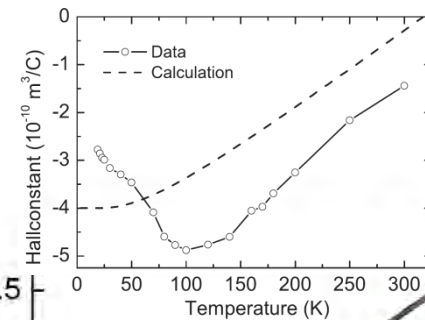
ARPES



S. Borisenko et al., PRL **105**, 067002 (2010)

A. Kordyuk et al. PRB **83**, 134513 (2011)

Transport



O. Heyer, CH, et al., PRB **84**, 064512 (2011)

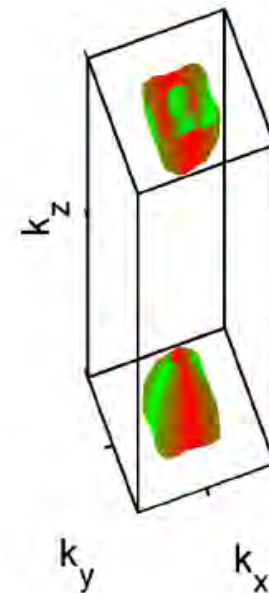
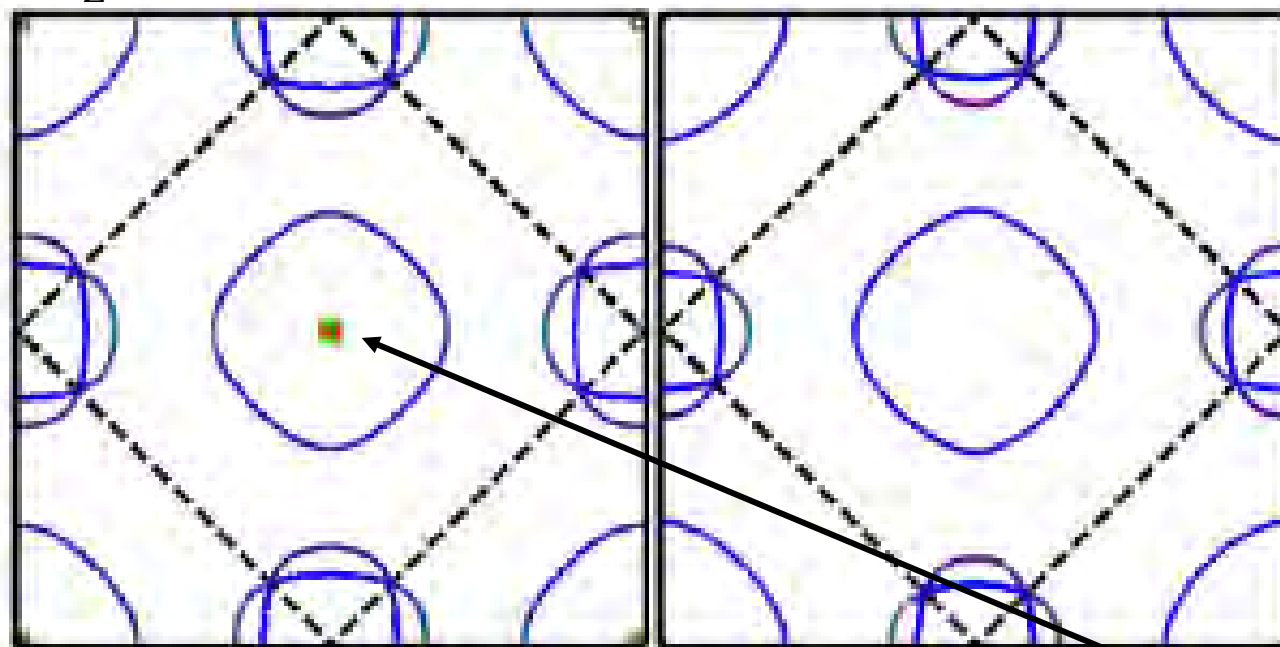
LiFeAs: Fermi Surface

10-orbital tight binding model:

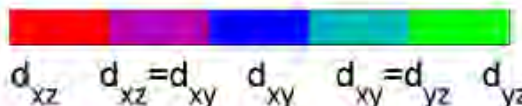
Y. Wang et al., PRB **88**, 174516 (2013)

$$k_z = \pi$$

$$k_z = 0$$



k_x

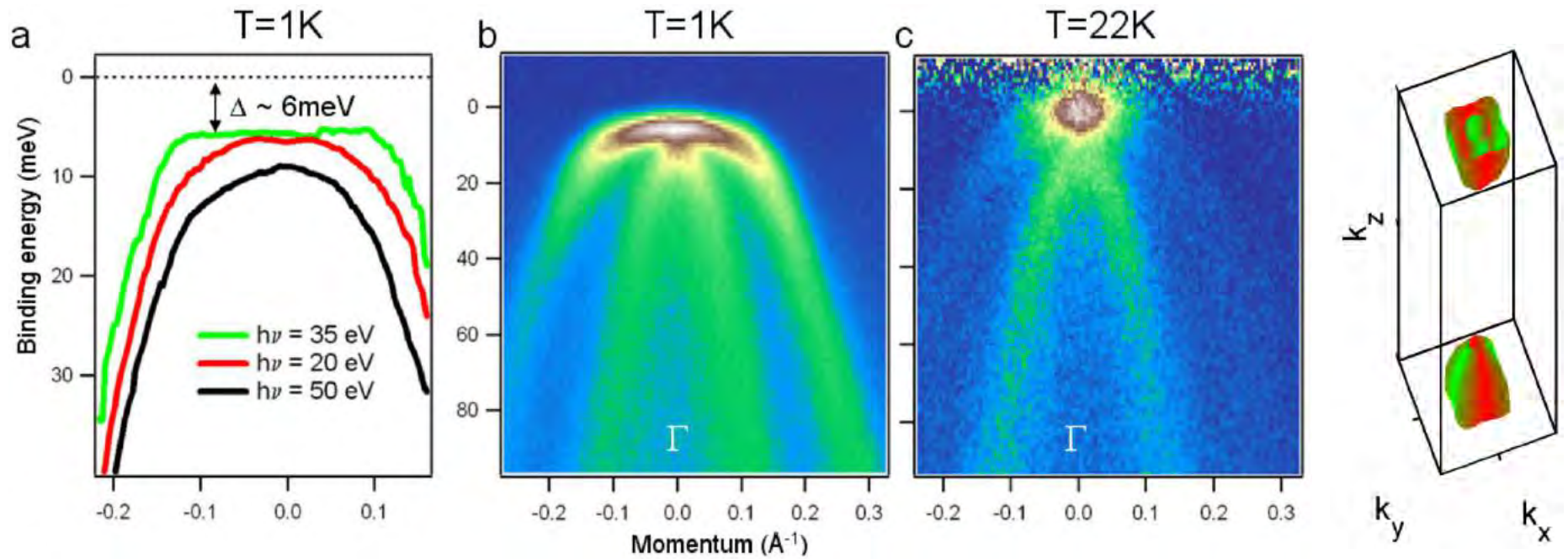


Largest gap ~ 6 meV

other FS: $\sim 3-4$ meV

S. Borisenko et al.,
Symmetry **4**, 251 (2012)

LiFeAs: Largest gap at Γ



Largest gap $\sim 6\text{ meV}$

other FS: $\sim 3\text{-}4\text{ meV}$

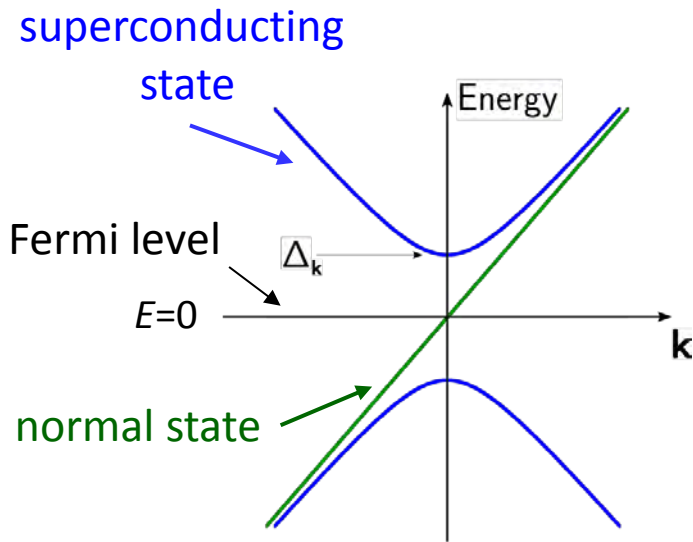
S. Borisenko et al.,
Symmetry **4**, 251 (2012)

Gap spectroscopy of LiFeAs

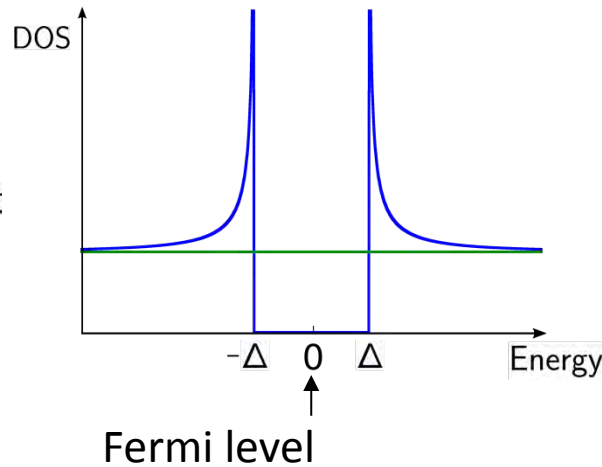
Superconducting State

Consequences of energy gap

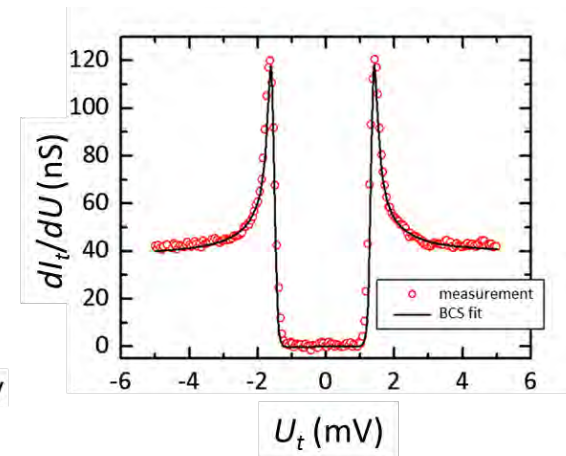
Band structure



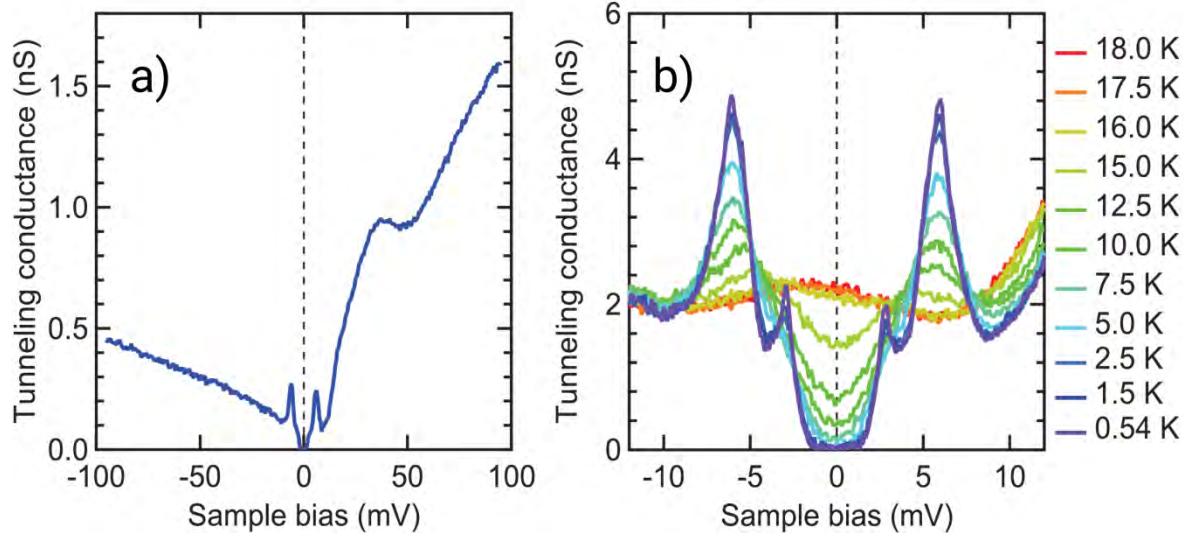
Density of states



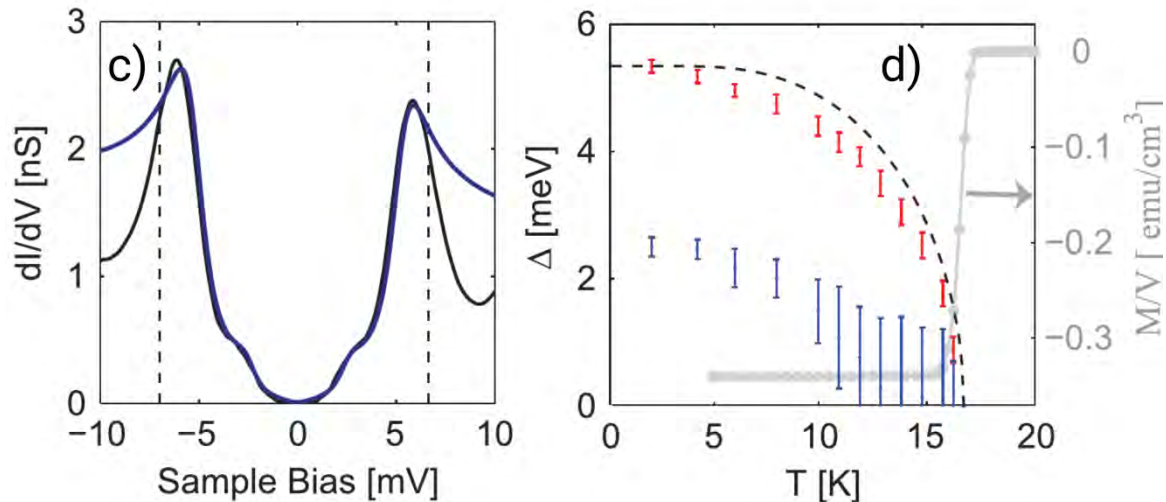
Tunneling!



Typical LiFeAs tunneling spectra



Hanaguri et al., PRB **85**, 214505 (2012)



Chi et al., PRL **109**, 087002 (2012)

Large gap ~ 6 meV

Small gap: $\sim 3-4$ meV

No nodes!

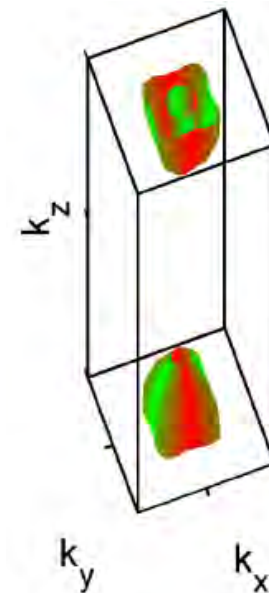
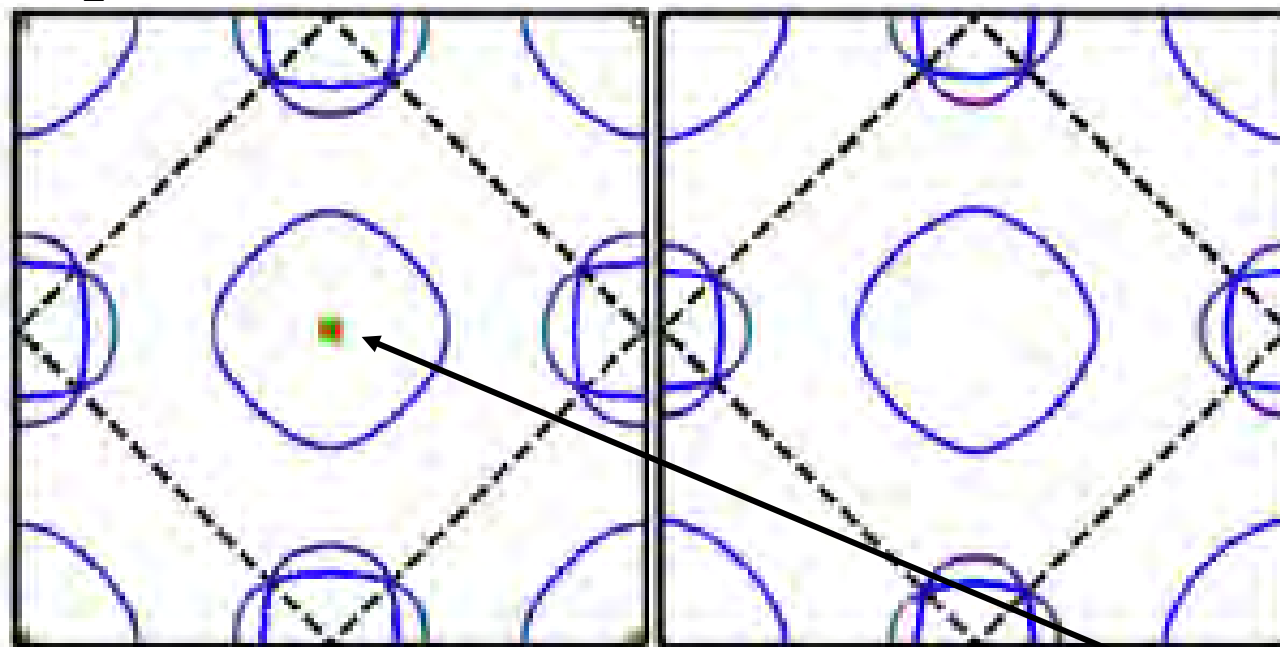
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10-orbital tight binding model:

Y. Wang et al., PRB **88**, 174516 (2013)

$$k_z = \pi$$

$$k_z = 0$$



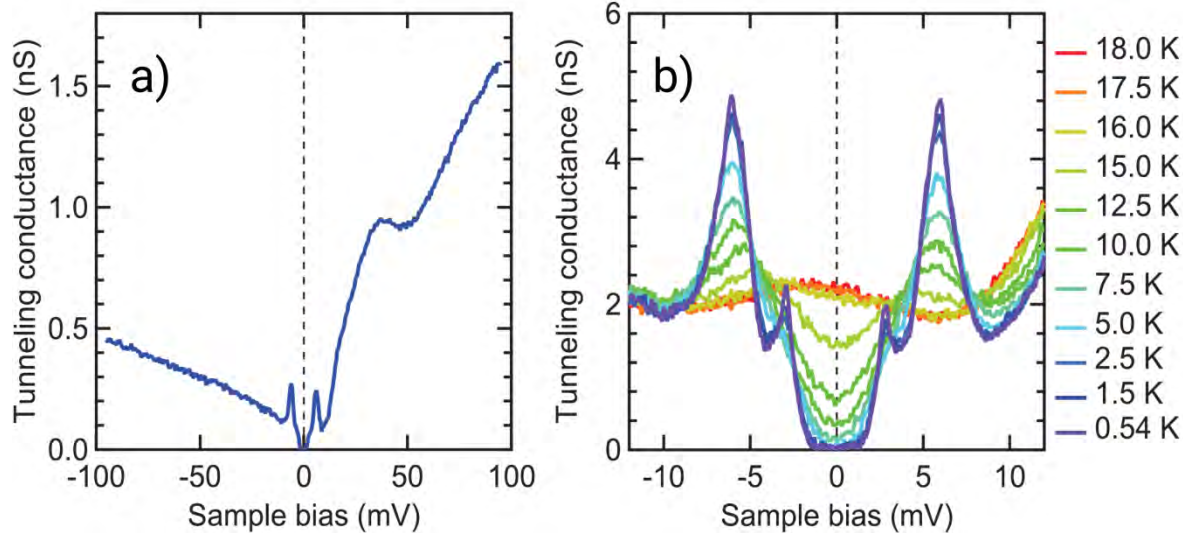
Largest gap ~ 6 meV

other FS: $\sim 3-4$ meV

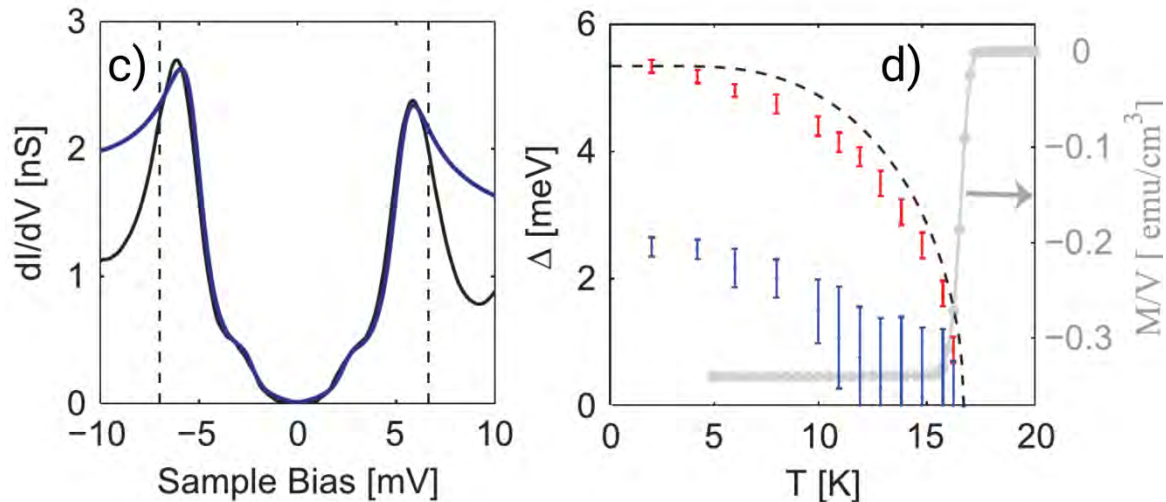
S. Borisenko et al.,
Symmetry **4**, 251 (2012)

F. Ahn et al., PRB **89**, 144513 (2014)

Typical LiFeAs tunneling spectra



Hanaguri et al., PRB **85**, 214505 (2012)



Chi et al., PRL **109**, 087002 (2012)

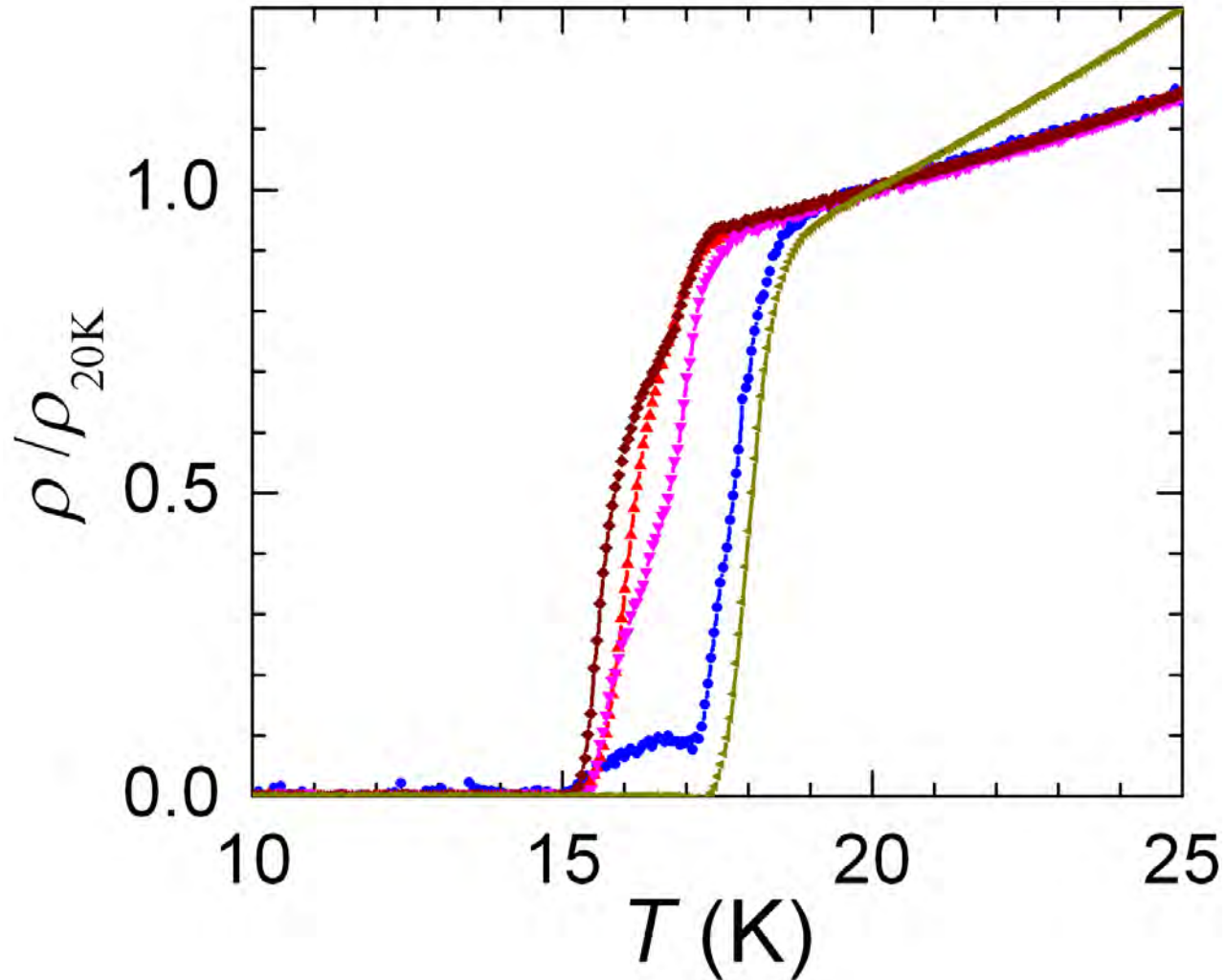
Large gap ~ 6 meV

Small gap: $\sim 3-4$ meV

No nodes!

Two T_c 's?

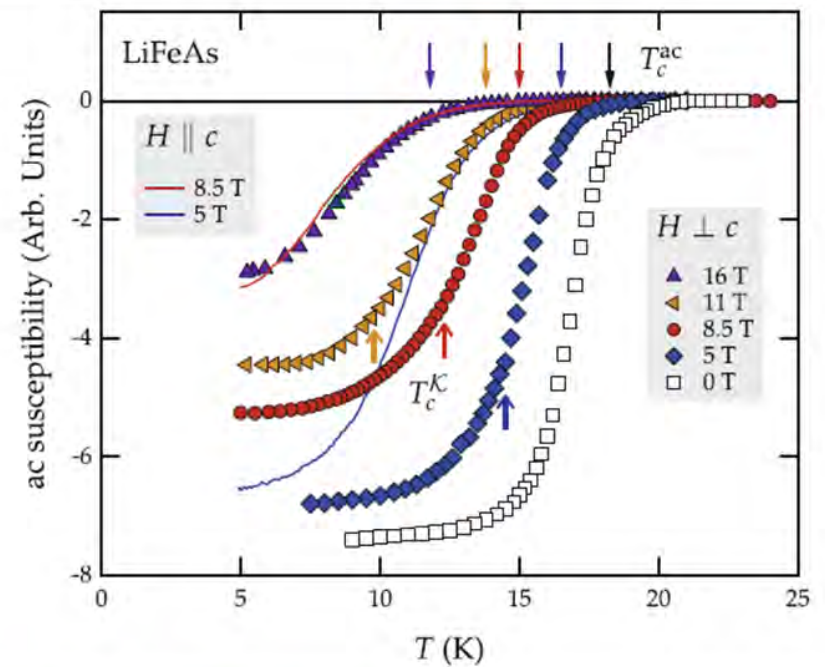
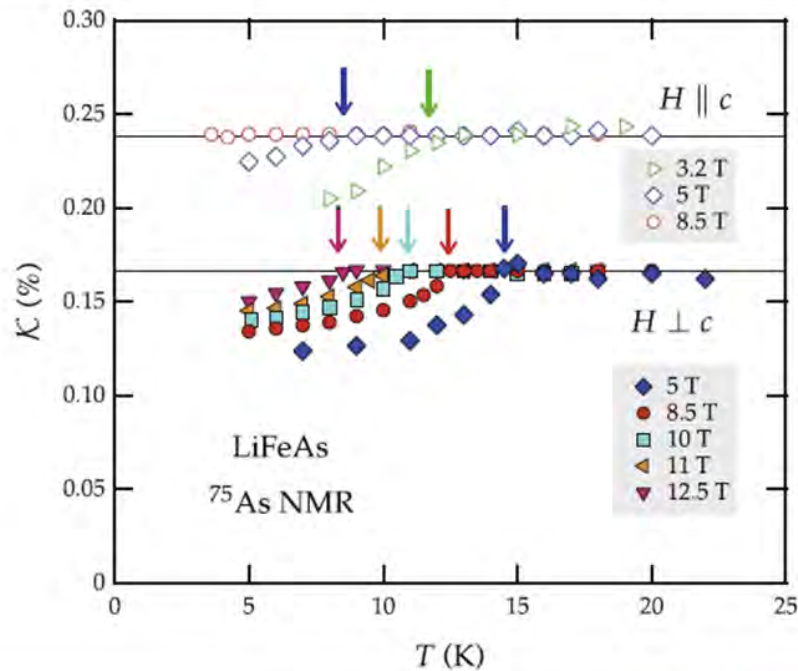
T_c of stoichiometric LiFeAs: either 16 K or 18 K



D. Bombor, CH et al. unpublished

Two T_c 's?

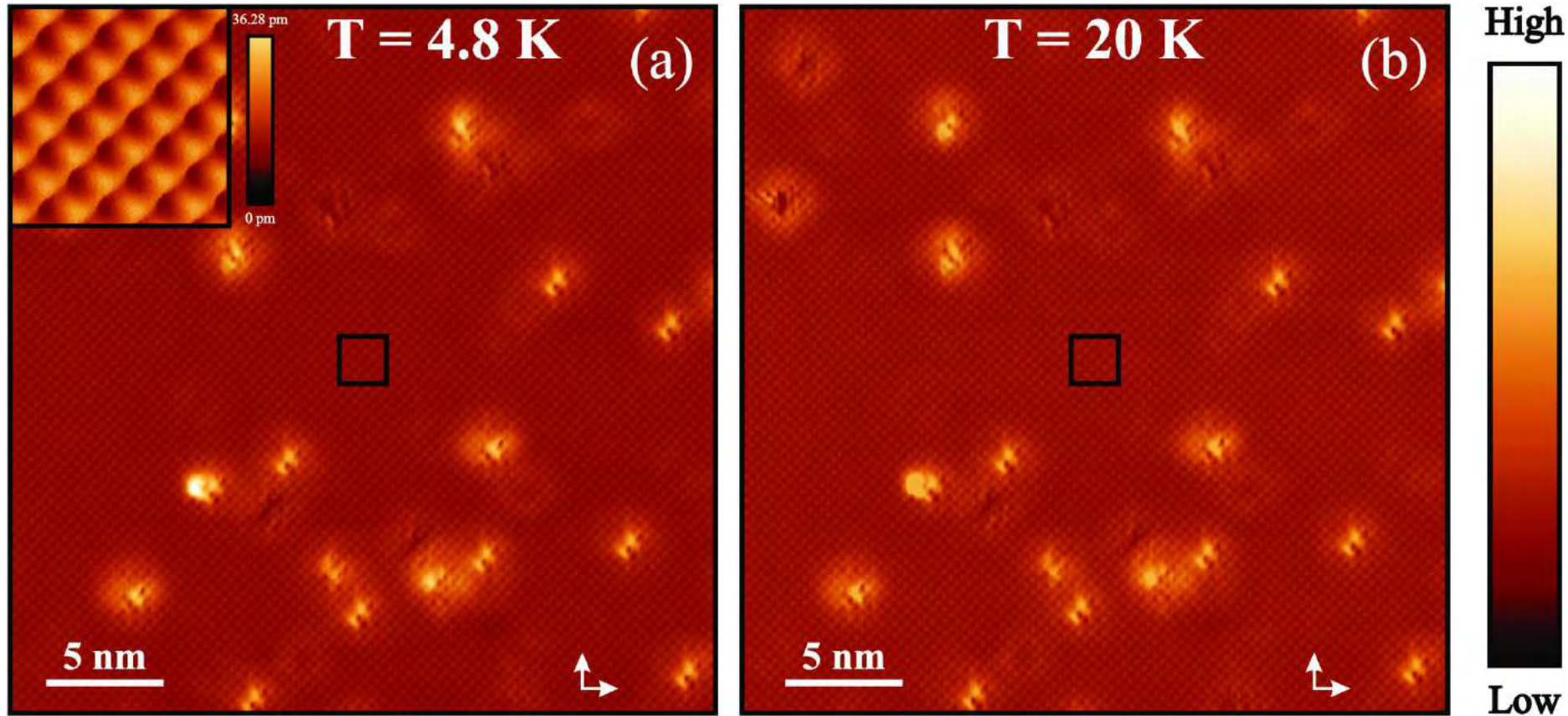
Knight shift and ac-susceptibility measurement



S.H. Baek et al., J.Phys. Condens. Matter 25, 162204 (2013)

Two separate transitions!

Temperature dependent STS on LiFeAs

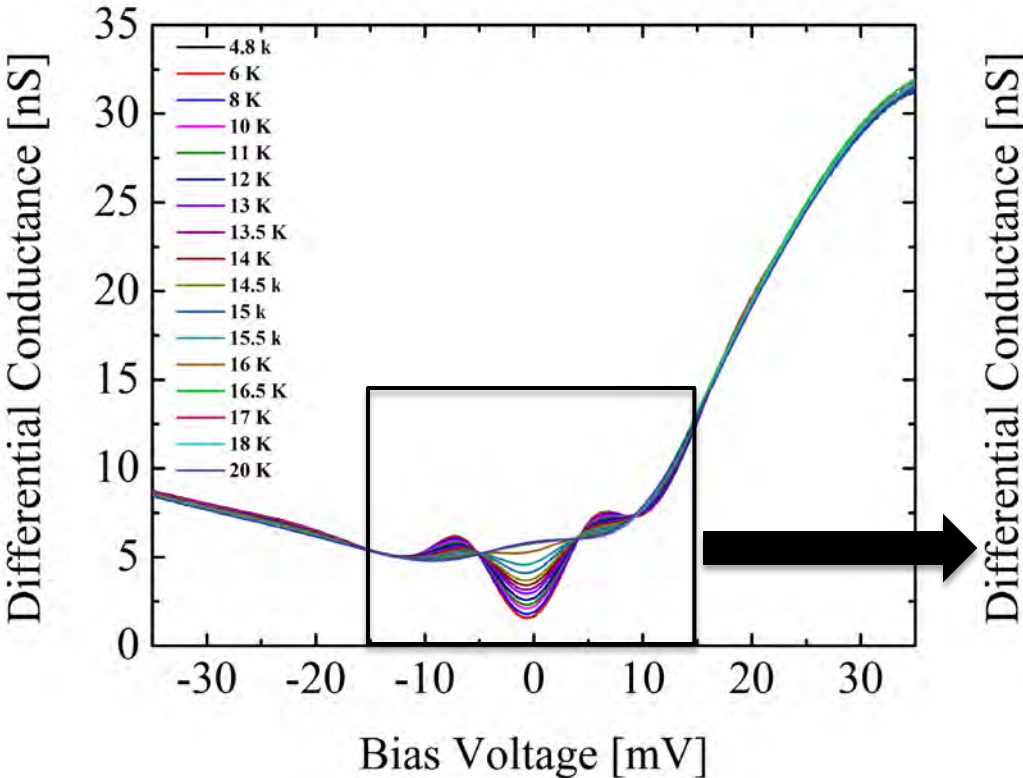


$$I_T = 300 \text{ pA}; U_{\text{bias}} = +35 \text{ mV}$$

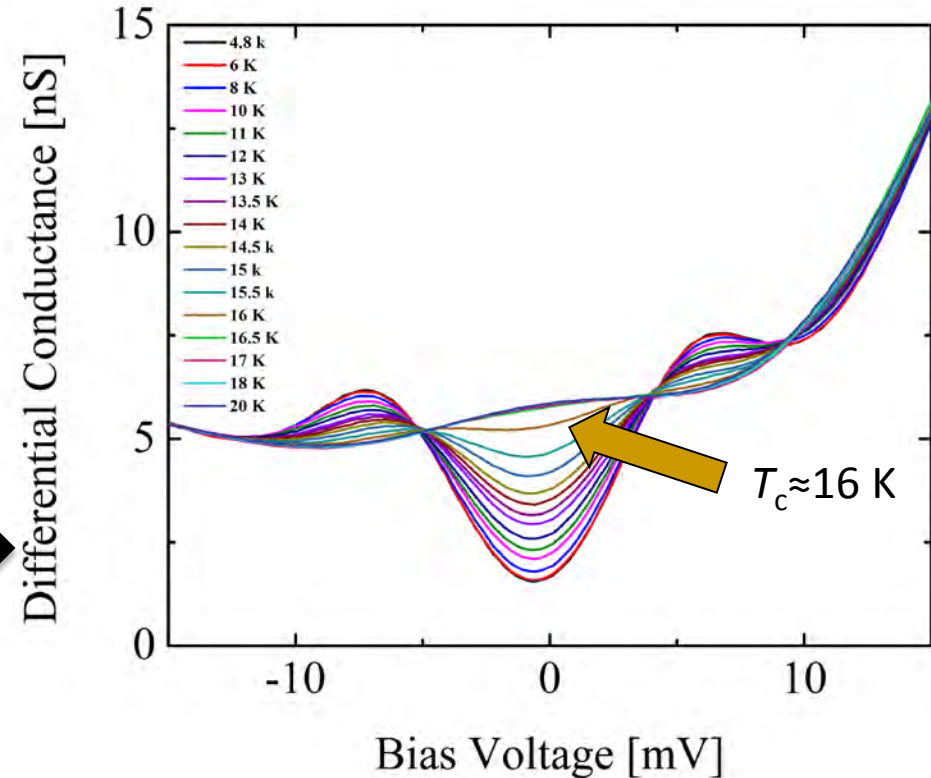
Clean area for temperature dependent spectra

Temperature dependent STS on LiFeAs

Raw Data



Raw Data



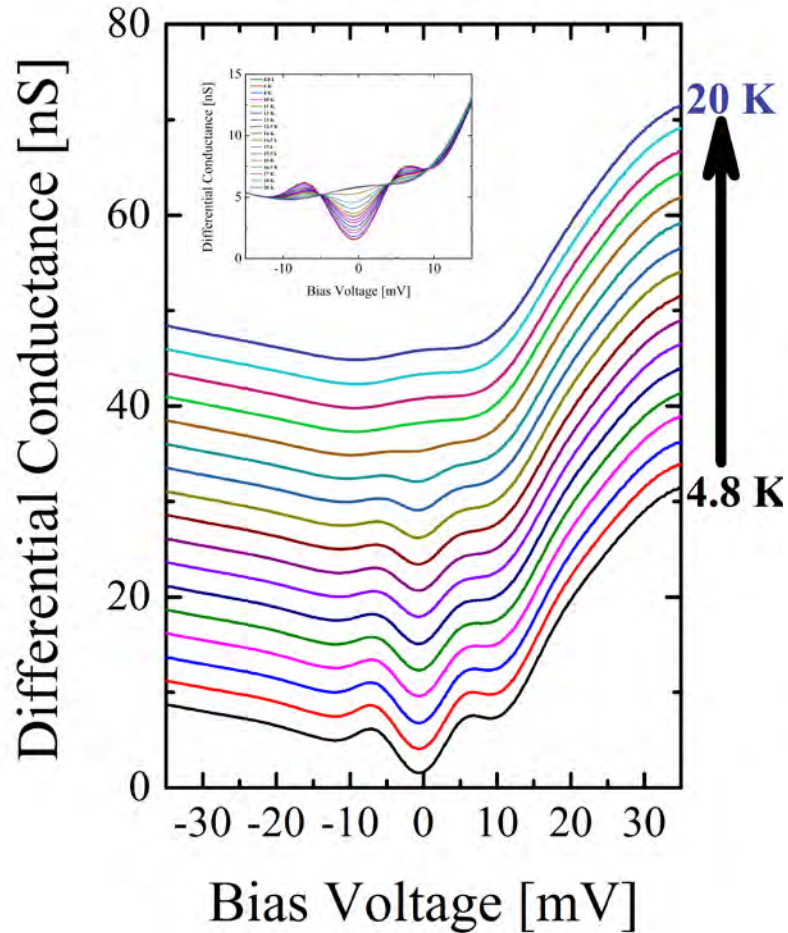
Superconducting gap seems to close at ~16K

See also: T. Hanaguri et al. PRB **85**, 214505 (2012)
S. Chi et al., PRL **109**, 087002

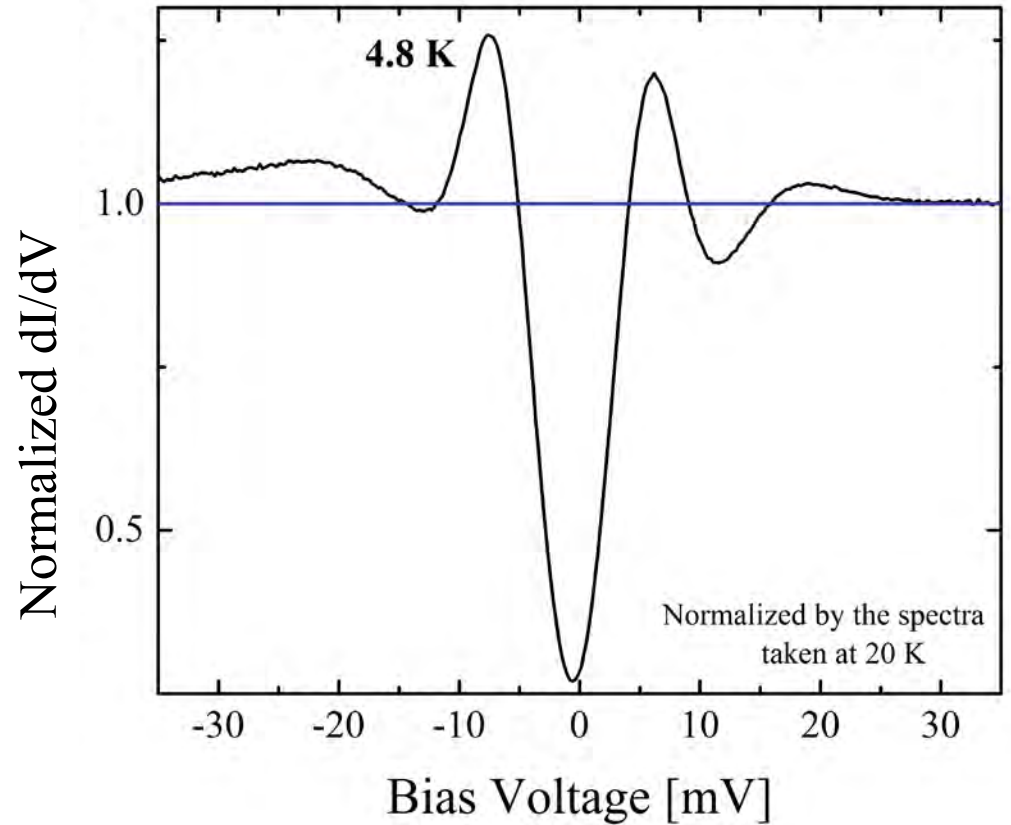
P.K. Nag et al., Scientific Reports **6**, 27926 (2016)

Temperature dependent STS on LiFeAs

Raw Data

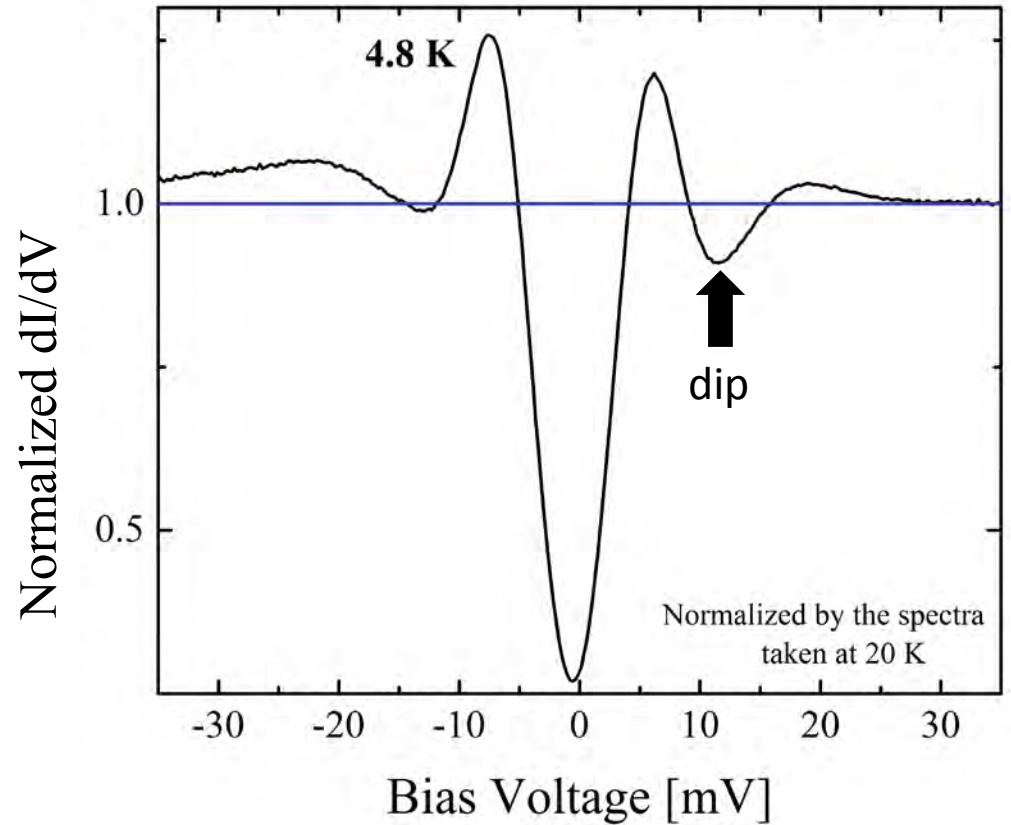
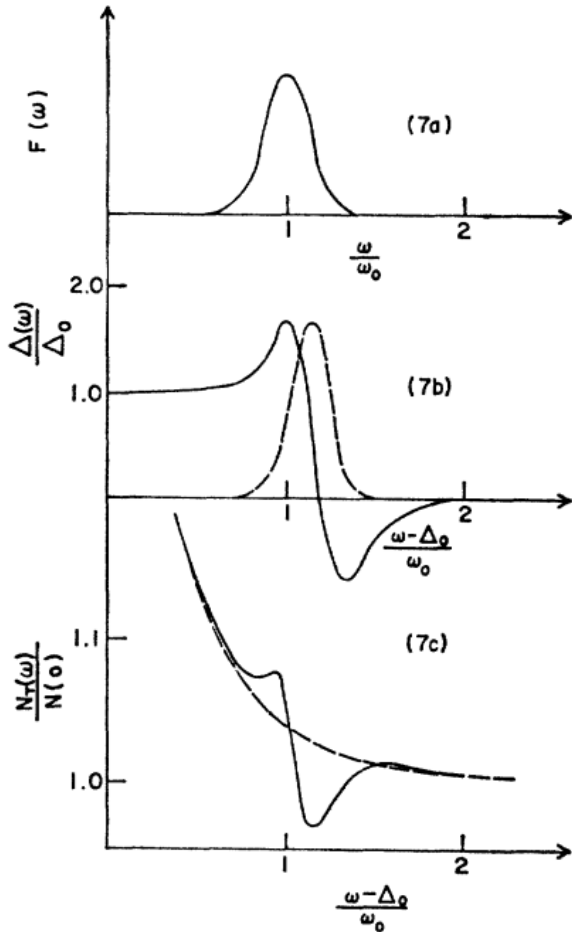


Normalized Data (20 K spectrum)



Temperature dependent STS on LiFeAs

Normalized Data (20 K spectrum)

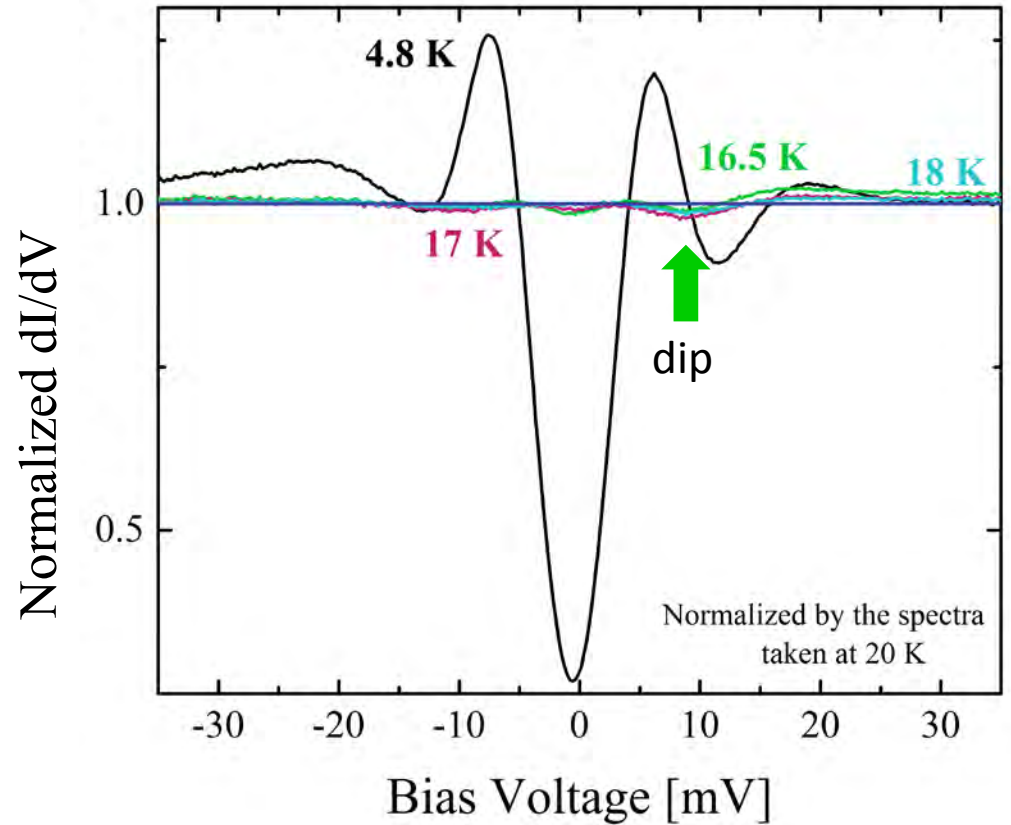
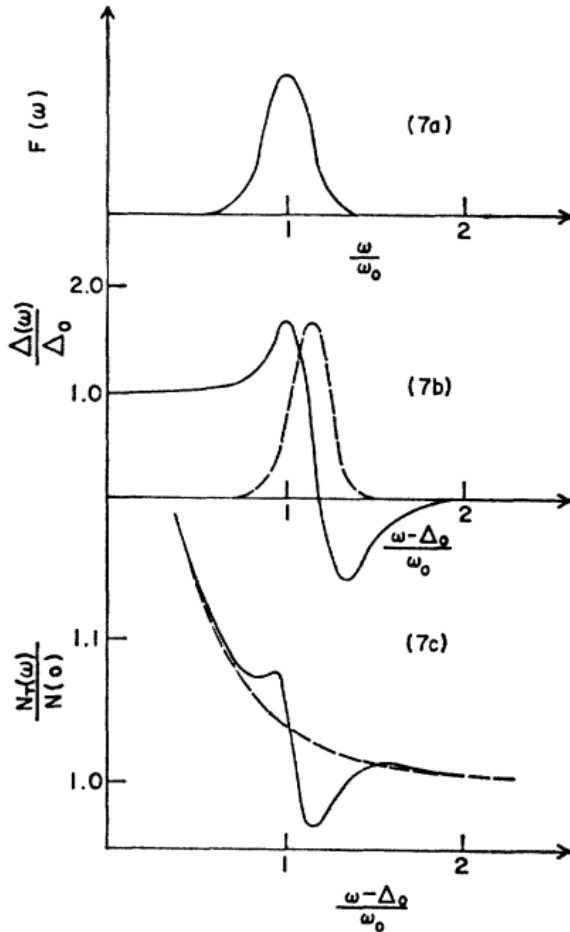


D.J. Scalapino et al. Phys. Rev. **148**, 263 (1966)

P.K. Nag et al., Scientific Reports **6**, 27926 (2016)

Temperature dependent STS on LiFeAs

Normalized Data (20 K spectrum)

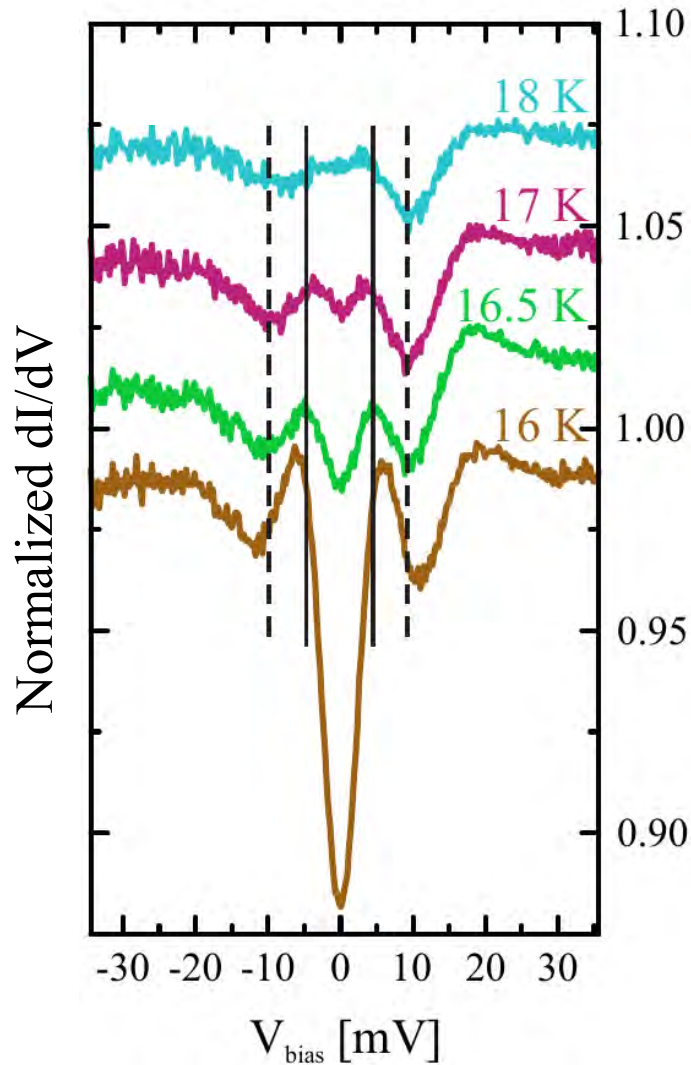


D.J. Scalapino et al. Phys. Rev. **148**, 263 (1966)

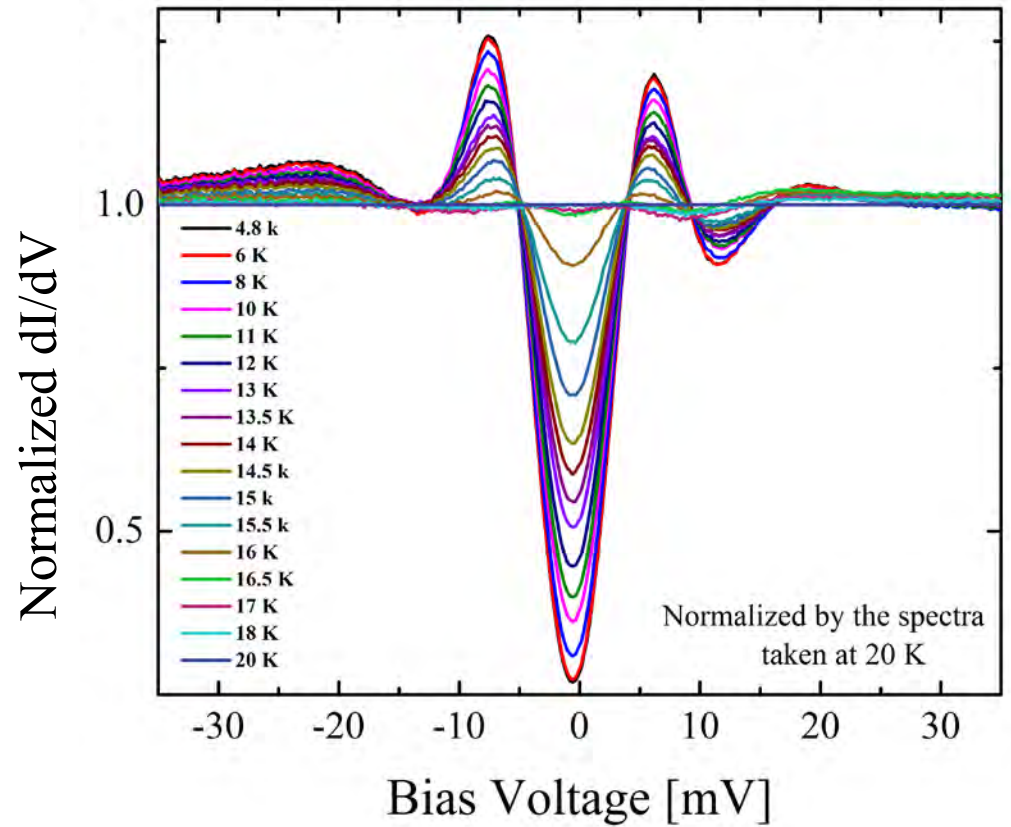
$$T_C^* \approx 18 \text{ K}$$

P.K. Nag et al., Scientific Reports **6**, 27926 (2016)

Temperature dependent STS on LiFeAs



Normalized Data (20 K spectrum)

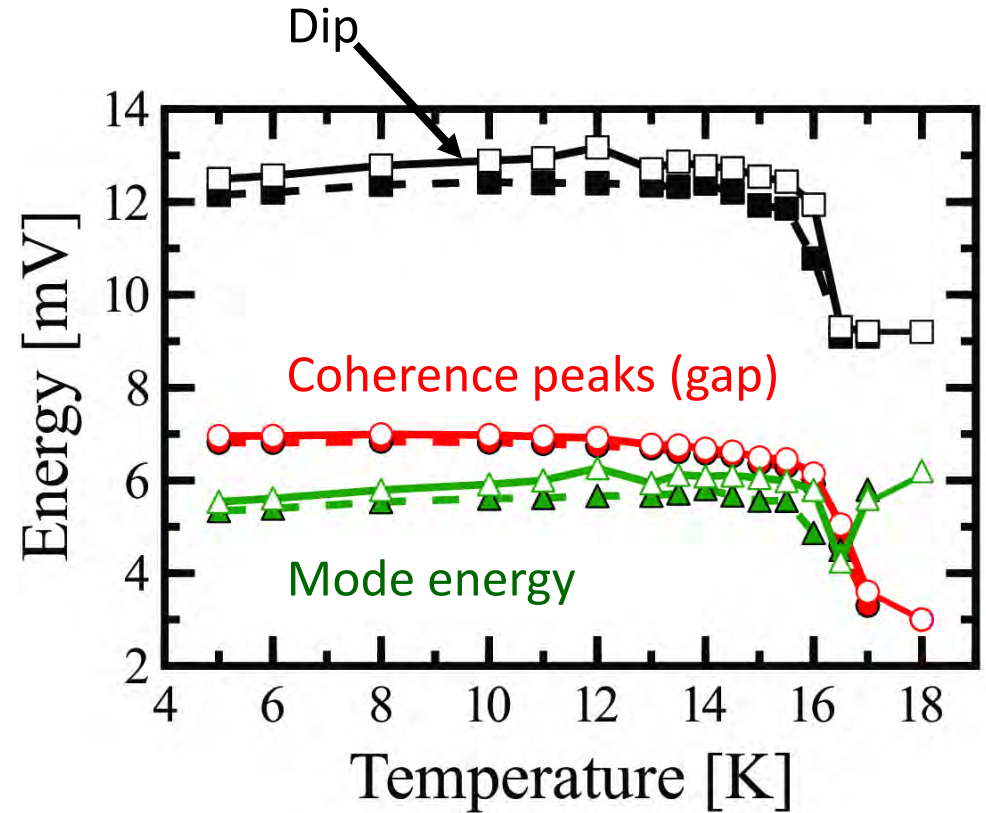
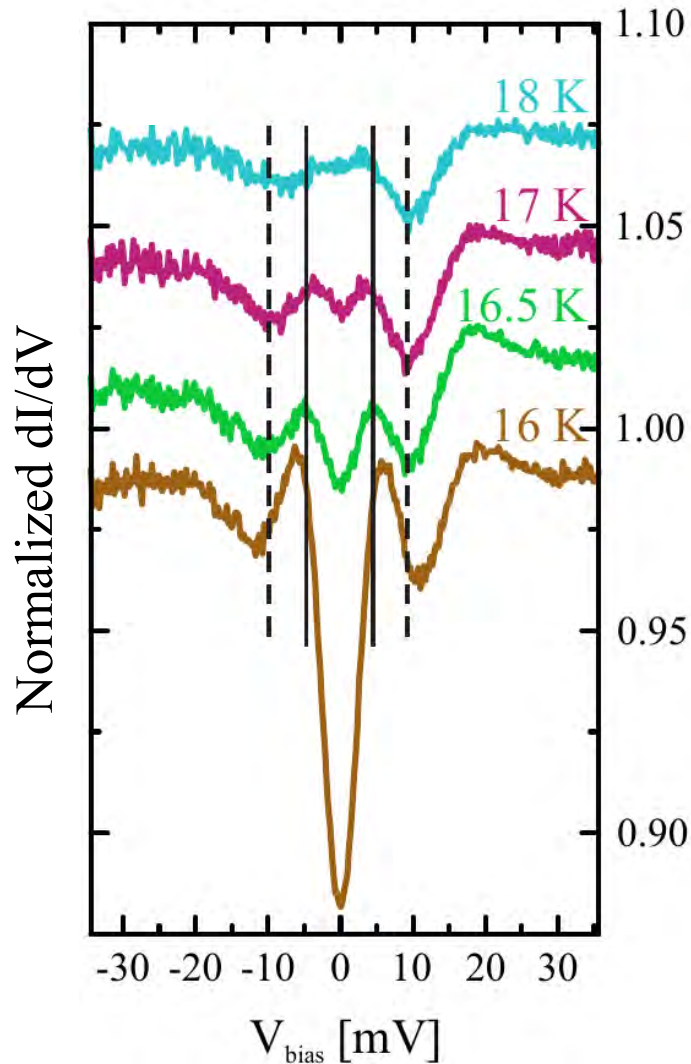


$$T_c^* \approx 18 \text{ K}$$

$$T_c \approx 16 \text{ K?}$$

P.K. Nag et al., Scientific Reports 6, 27926 (2016)

Temperature dependent STS on LiFeAs

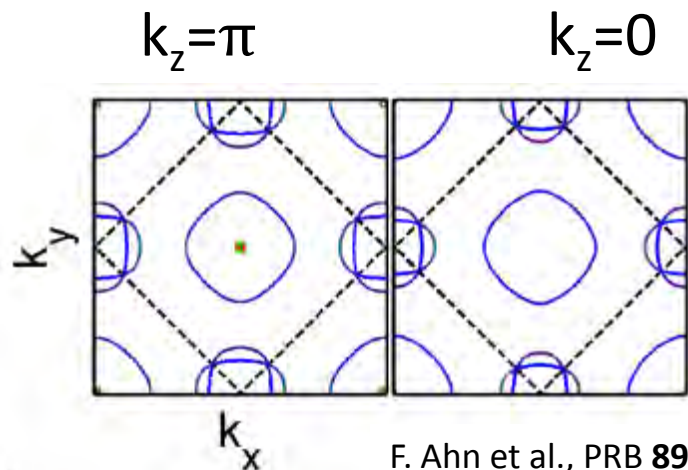


Evidence for unusual gap evolution

- Faint onset of superconductivity at 18 K
- Full superconductivity at 16 K
- Mode energy $\sim T$ -independent

P.K. Nag et al., Scientific Reports 6, 27926 (2016)

Proposed scenario and open issues



F. Ahn et al., PRB **89**, 144513 (2014)

- $T_c^* = 18$ K: Onset of superconductivity at $k_z = \pi$
- $T_c = 16$ K: Onset of superconductivity on full FS

Consistent with theoretical OP analysis

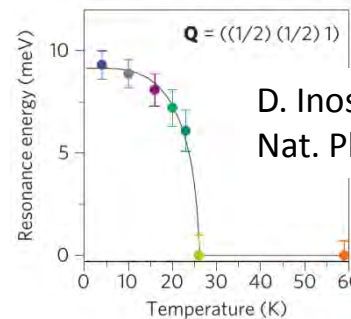
Bosonic mode energy: T-independent!

- Expectation for spin resonance:
scaling with sc order parameter
- No spin resonance in LiFeAs

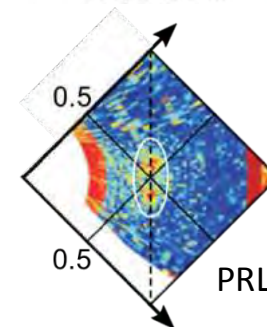
See also: S. Chi et al., PRL **109**, 087002



- Bosonic mode of different origin?
 - Large gap?
 - Inelastic scanning tunneling spectroscopy?
- P. Hlobil et al., arXiv:1603.05288



D. Inosov et al.,
Nat. Phys. **6**, 178 (2010)

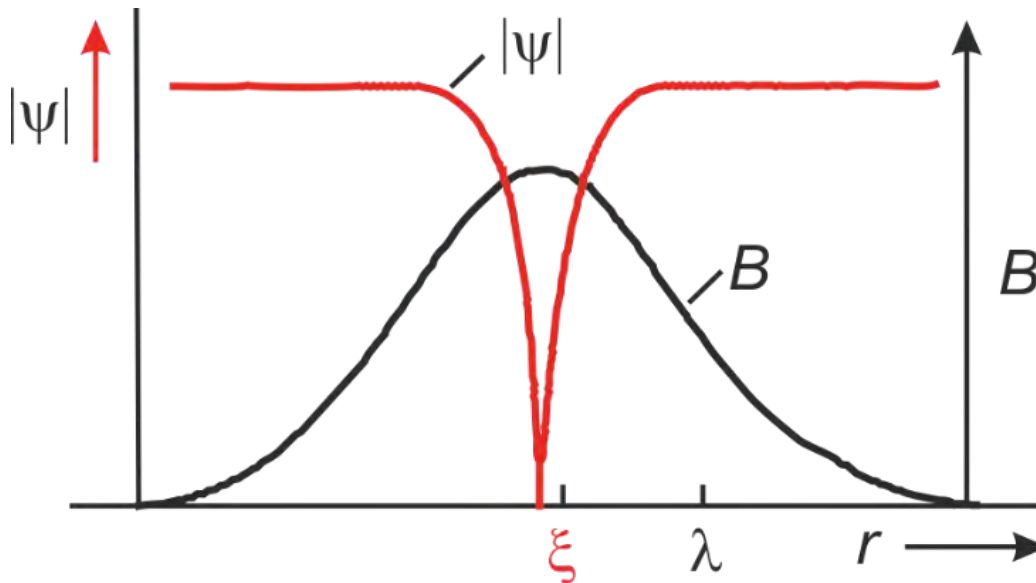


N. Qureshi et al.,
PRL **108**, 117001 (2012)

**Basic characterization:
Magnetic vortex analysis**

Vortices in Type-II Superconductors

In vortex: „mixture“ of normal and superconducting particles

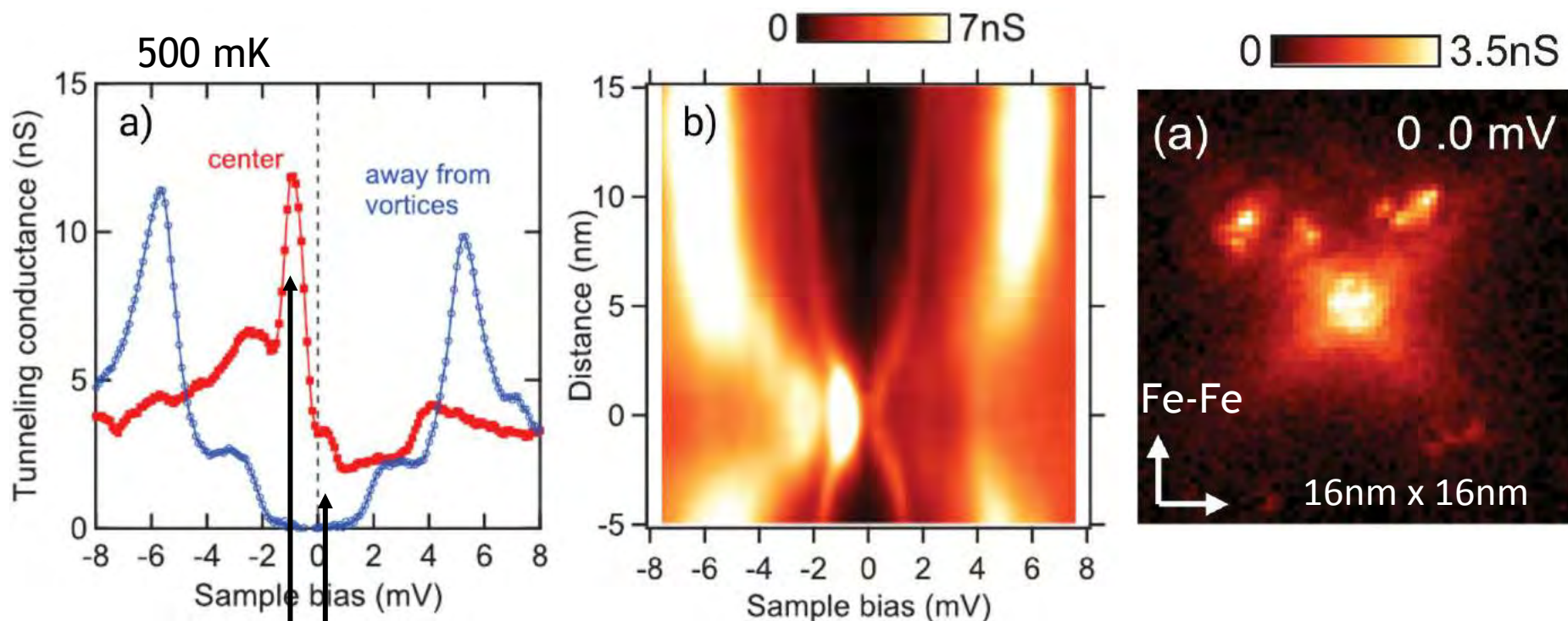


ψ superconducting wave function

ξ Ginzburg-Landau coherence length

λ London penetration depth

Vortex Core spectroscopy in LiFeAs



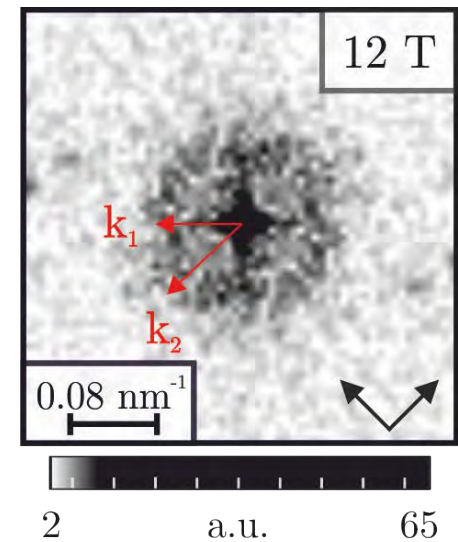
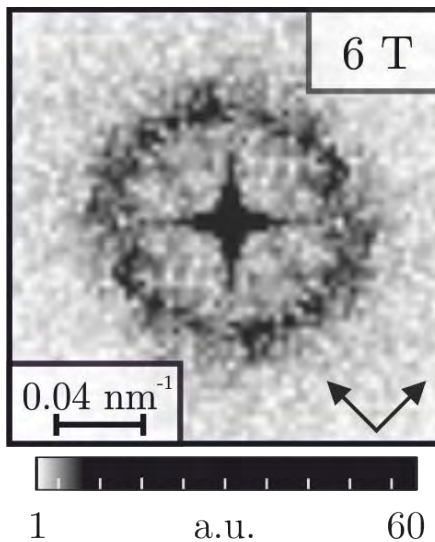
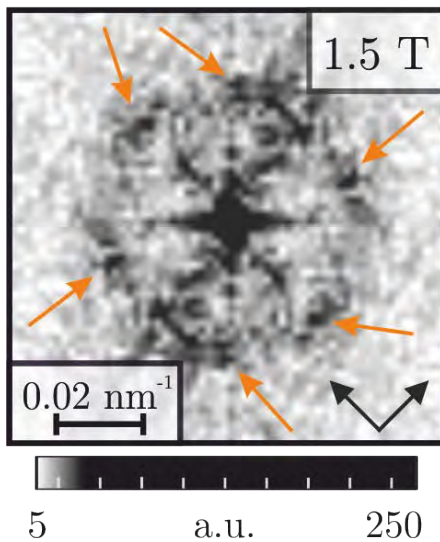
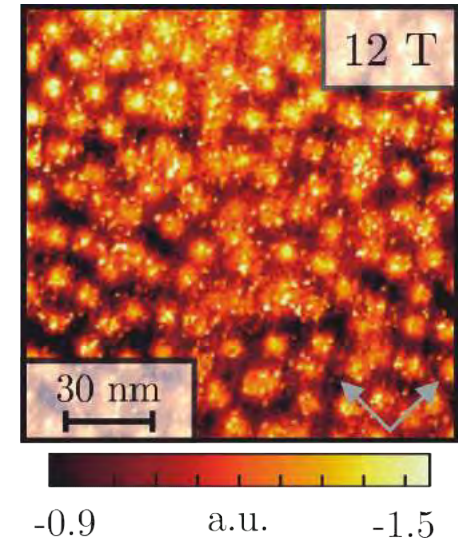
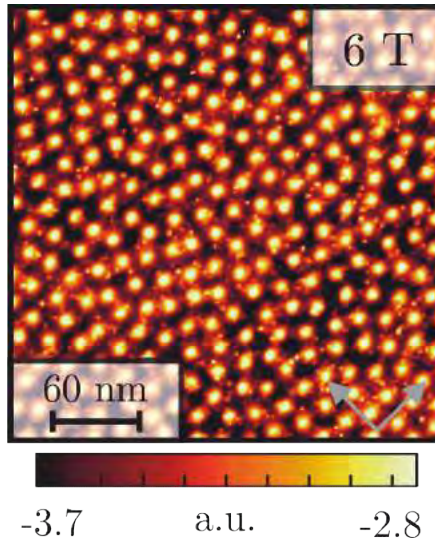
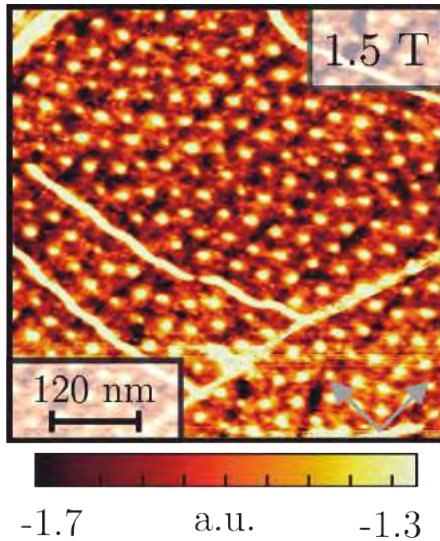
Vortex core states

Hanaguri et al., PRB 85, 214505 (2012)

Theory: Wang et al., PRB 85, 020506(R) (2012)

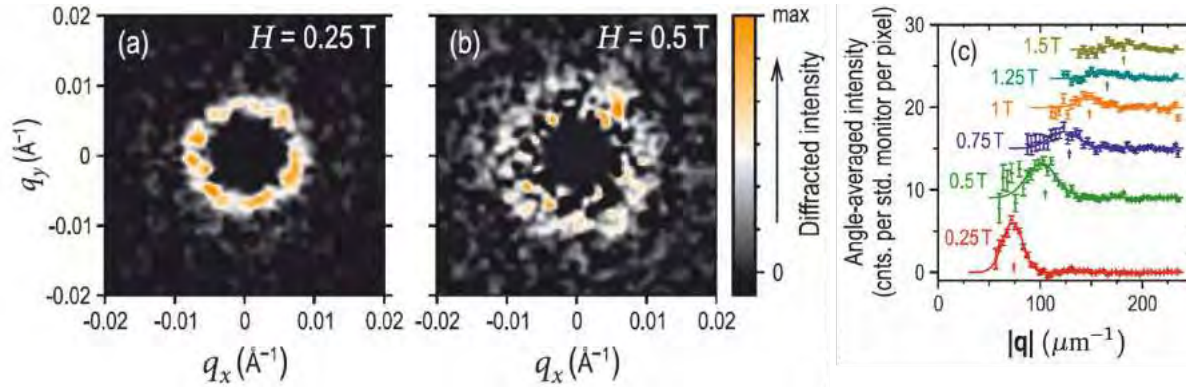
Vortex lattice in LiFeAs

$dI/dV(E_F)$ scans for various fields:



Vortex lattice in LiFeAs

SANS diffraction pattern and angle-averaged diffracted intensity

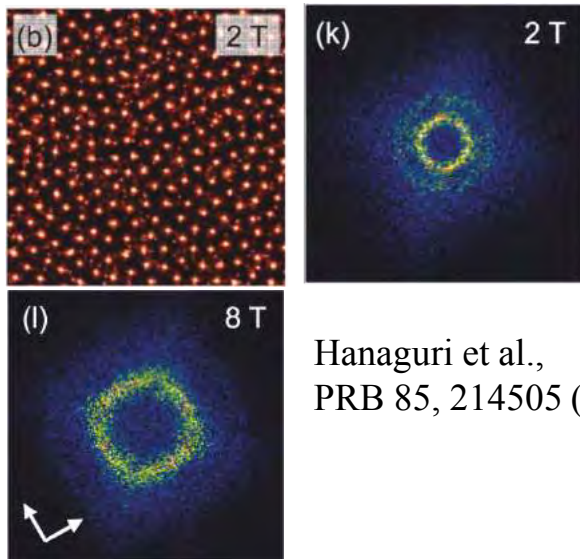


Trigonal vortex lattice:

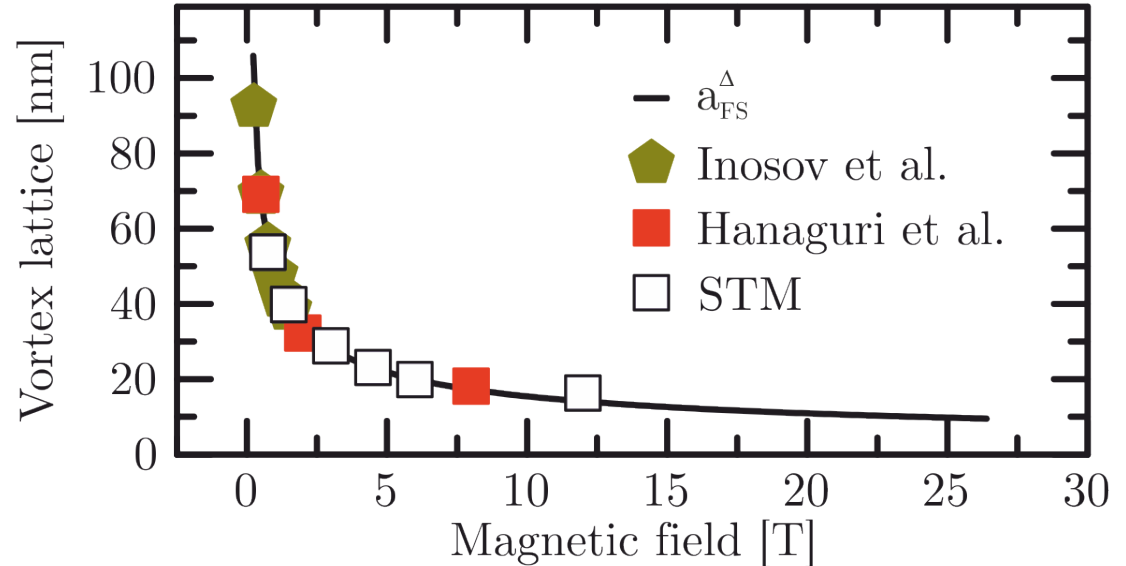
$$a_{\Delta} = \sqrt{\frac{2}{\sqrt{3}} \cdot \frac{\Phi_0}{B}}$$

Inosov et al., Phys. Rev. Lett 104, 187001 (2010)

STM...



Hanaguri et al.,
PRB 85, 214505 (2012)



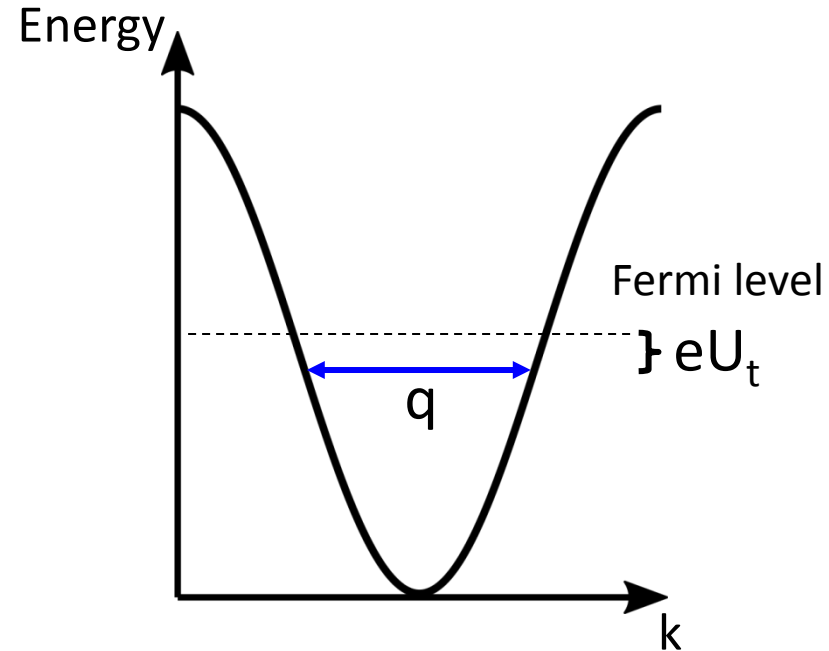
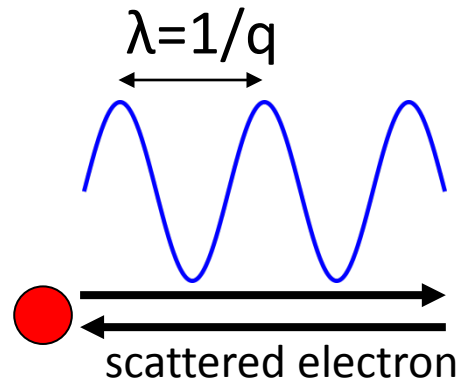
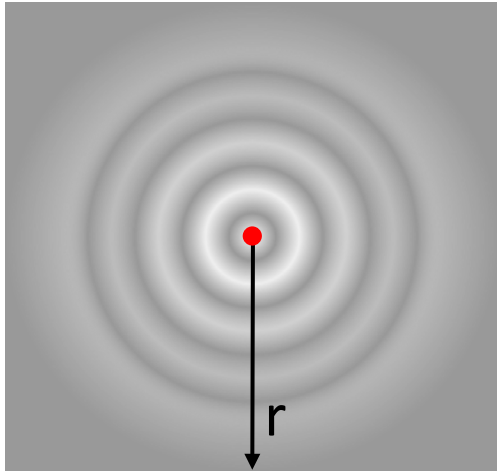
R. Schlegel, PhD thesis (2014)

Quasiparticle interference in LiFeAs

Quasiparticle interference

Quasiparticle scattering off defects → Friedel oscillations

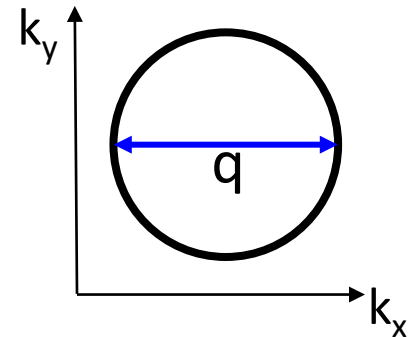
impurity in a metal



$$\Delta\text{LDOS} \sim \cos^2(rq)$$

„Quasiparticle Interference (QPI)“

→ probes band structure and scattering processes!



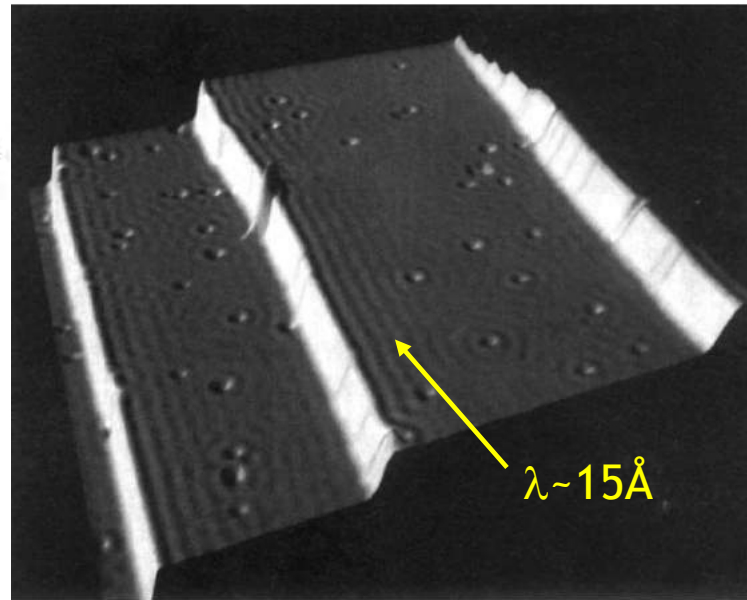
Quasiparticle Interference (QPI): normal metal

Imaging standing waves in a two-dimensional electron gas

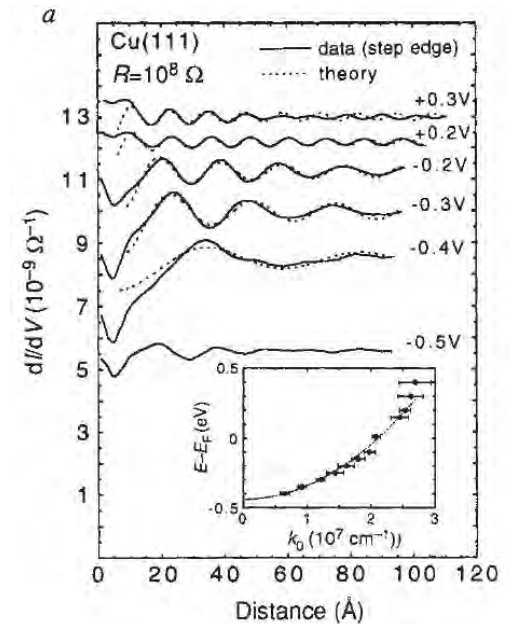
M. F. Crommie, C. P. Lutz & D. M. Eigler

IBM Research Division, Almaden Research Center, 650 Harry Road, San Jose, California 95120, USA

Nature **363**, 524 (1993)



Cu(111) in constant current mode
 $V=0.1\text{V}$, $I=1.0\text{nA}$



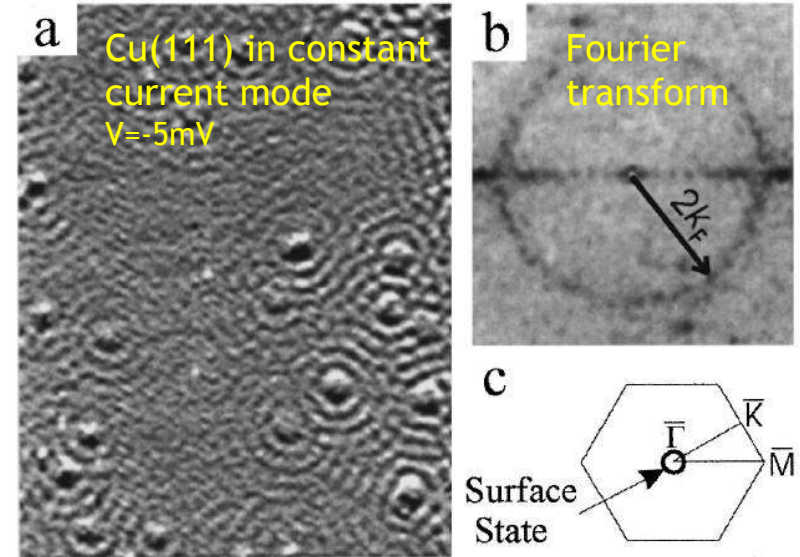
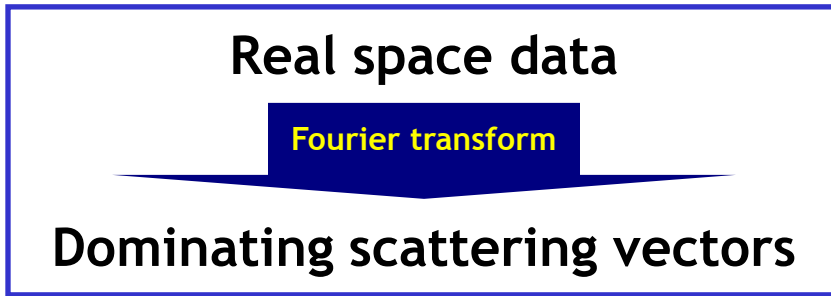
Differential conductance

Quasiparticle Interference (QPI): normal metal

Example:

Cu(111) topographic DOS data @ $\sim E_F$

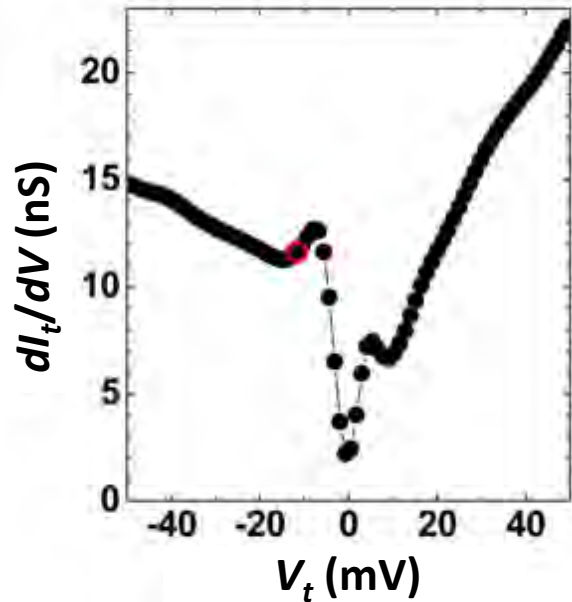
→ Dominating scattering vectors: $|\mathbf{q}| = 2\mathbf{k}_F$



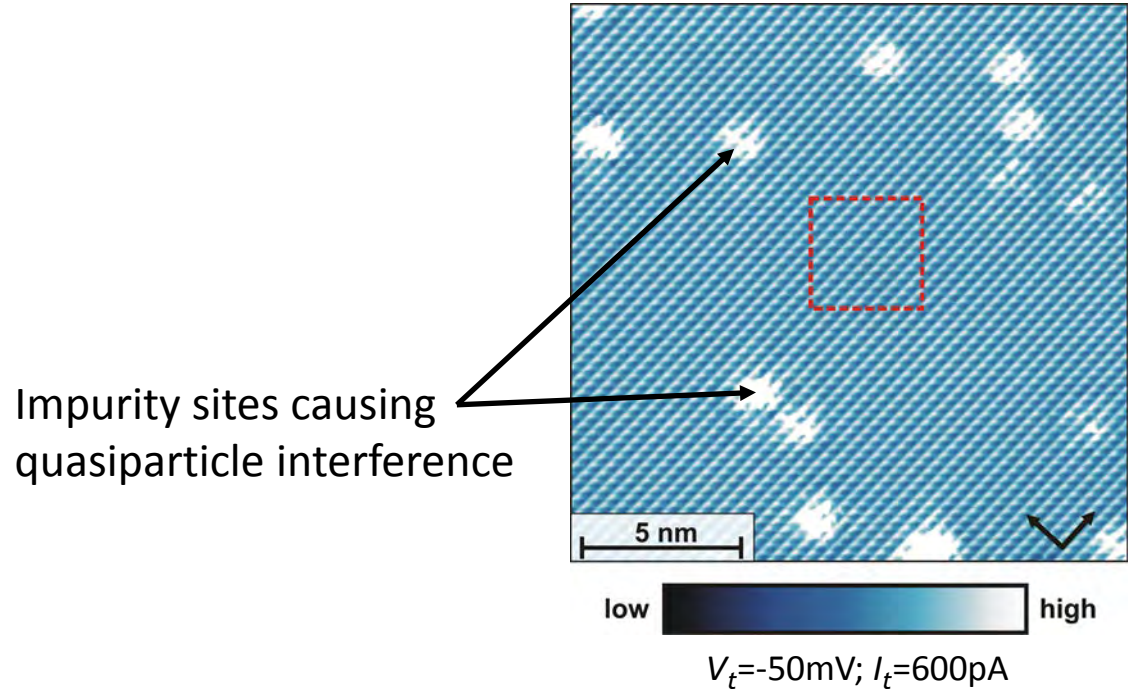
Petersen et al., PRB 57, R6858 (1998)

LiFeAs STM/STS results: quasiparticle interference

$dI_t/dV@6K$



Topography@6K

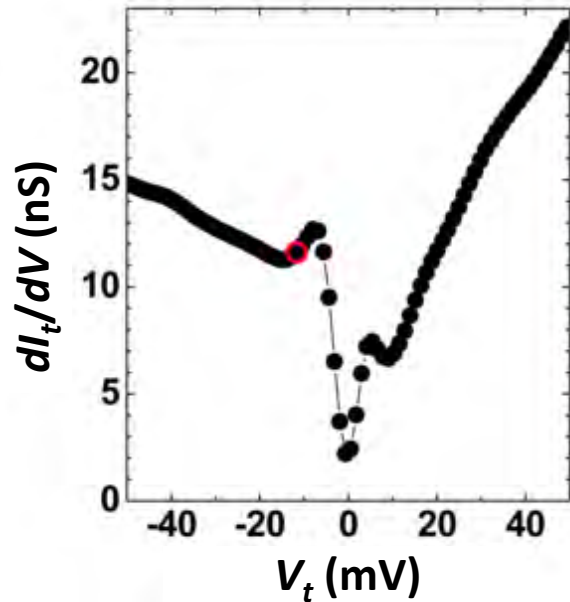


- Asymmetric DOS
- Average gap: $\Delta \sim 5$ meV

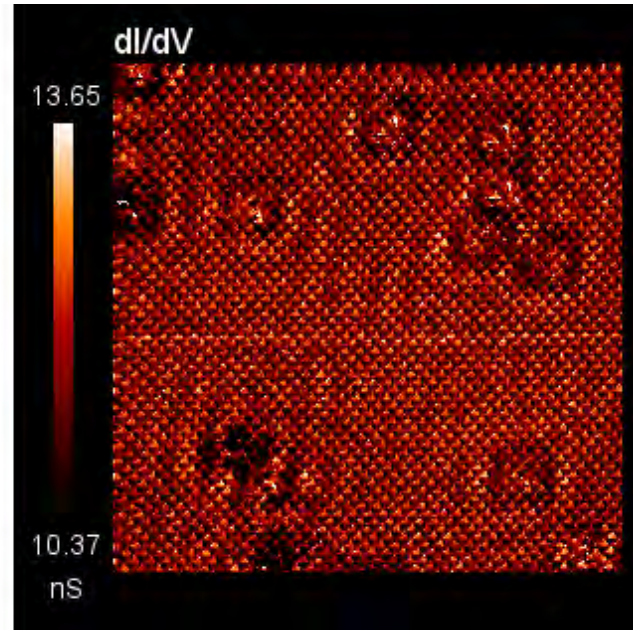
- ~ 2000 atoms @ $18 \text{ nm} \times 18 \text{ nm}$
- 14 impurity sites
➔ impurity density $< 1\%$

LiFeAs STM/STS results: quasiparticle interference

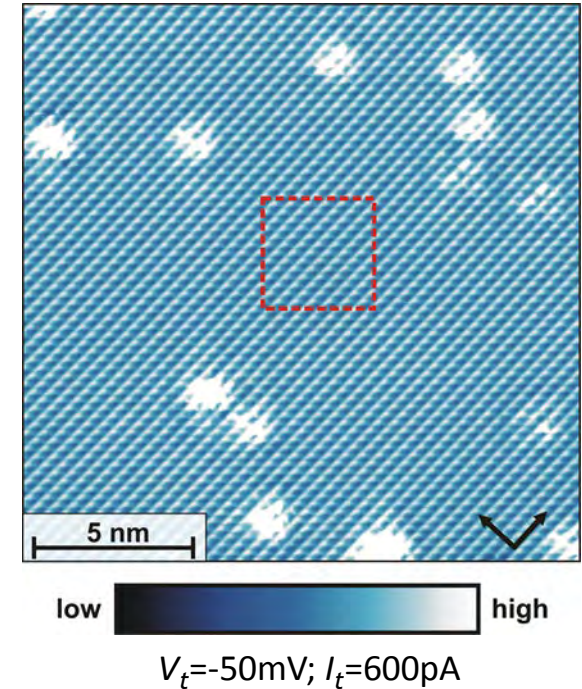
$dI_t/dV@6K$



dI_t/dV map @ -11.7mV



Topography@6K

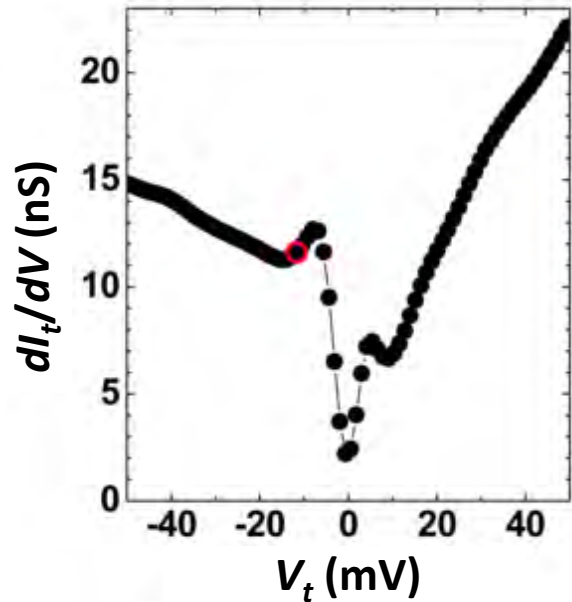


- Asymmetric DOS
- Average gap: $\Delta \sim 5$ meV

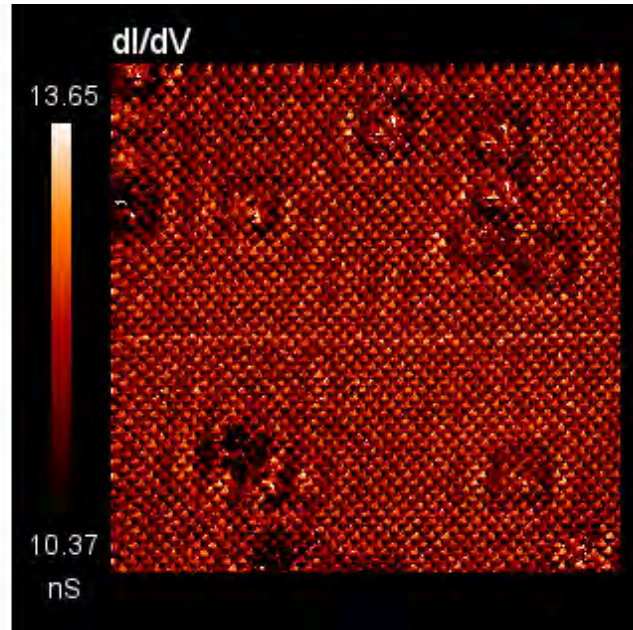
- ~ 2000 atoms @ 18 nm \times 18 nm
- 14 impurity sites
➔ impurity density $< 1\%$

LiFeAs STM/STS results: quasiparticle interference

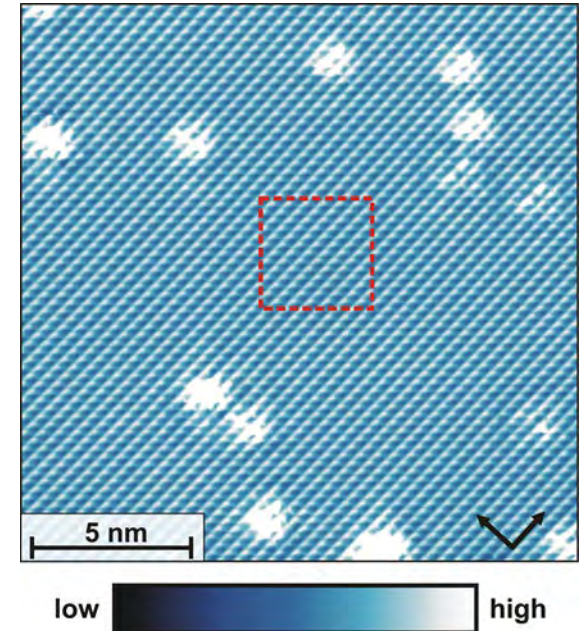
$dI_t/dV@6K$



dI_t/dV map @ -11.7mV

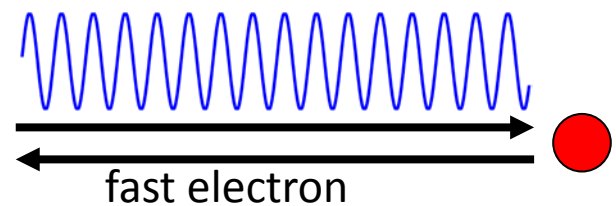
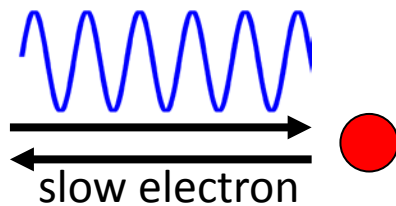


Topography@6K



$V_t = -50$ mV; $I_t = 600$ pA

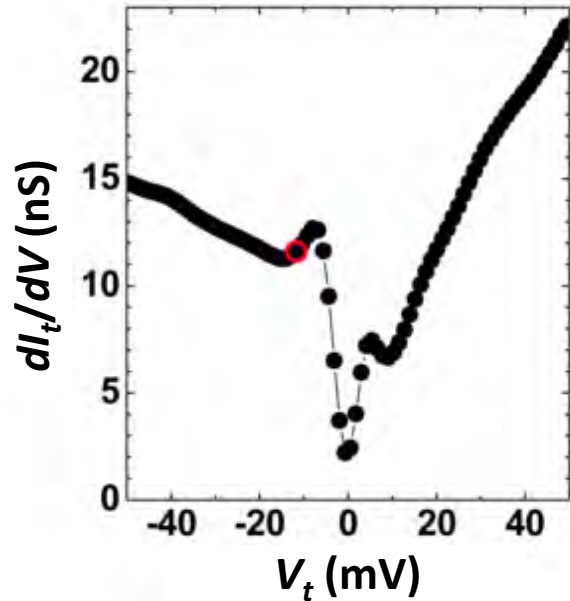
Quasiparticle scattering off defects



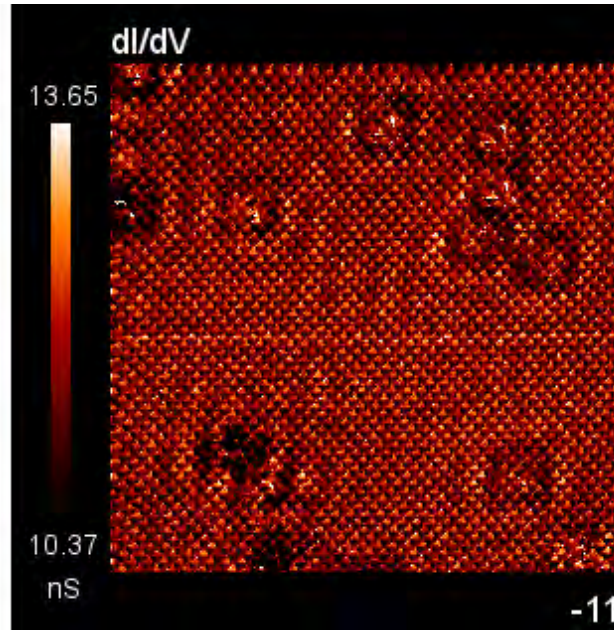
„quasiparticle interference (QPI)“

LiFeAs STM/STS results: quasiparticle interference

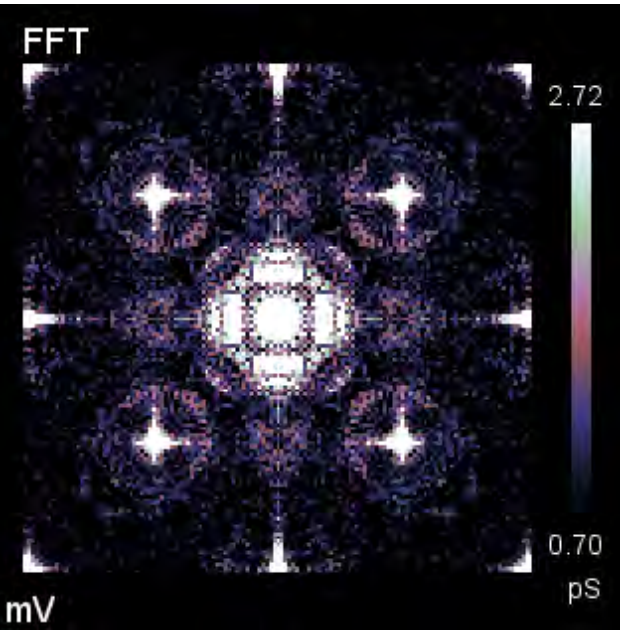
$dI_t/dV@6K$



dI_t/dV map

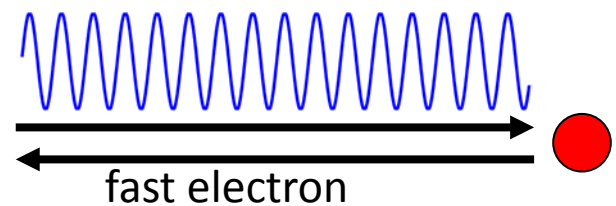
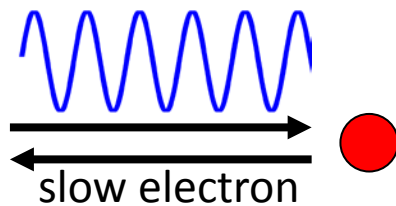


Fourier transform



Space of scattering momenta:
„q-space“

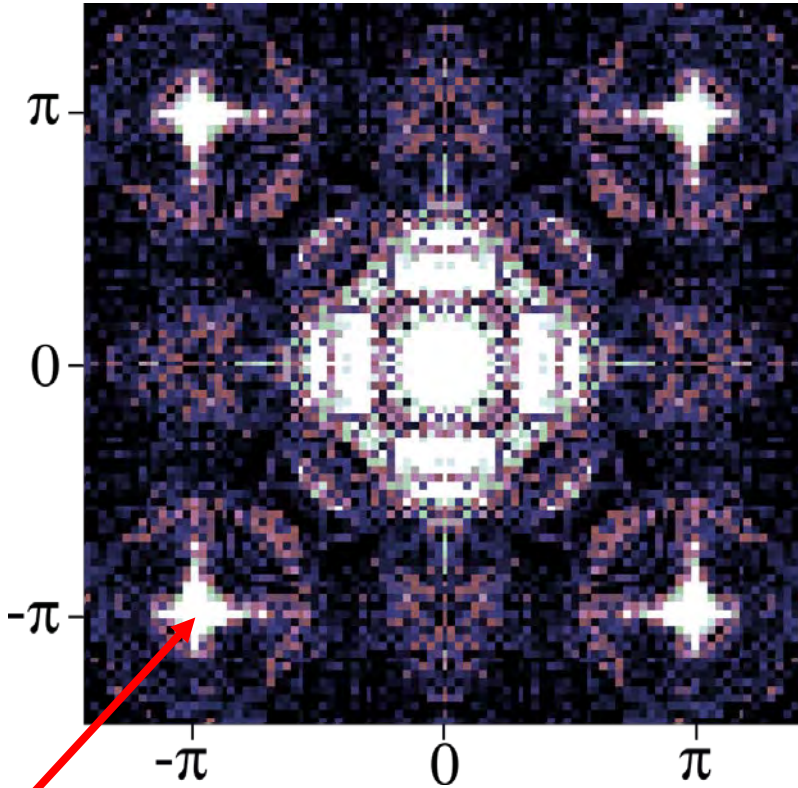
Quasiparticle scattering off defects



„quasiparticle interference (QPI)“

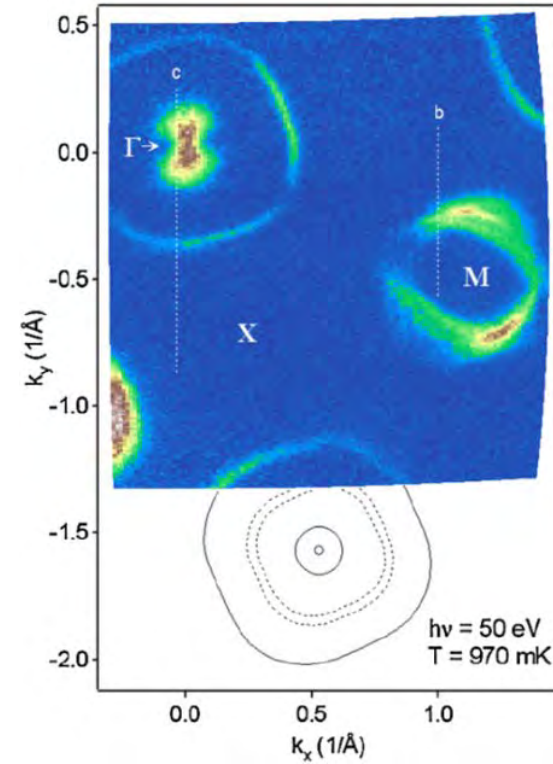
LiFeAs STM/STS results: quasiparticle interference

q-space image



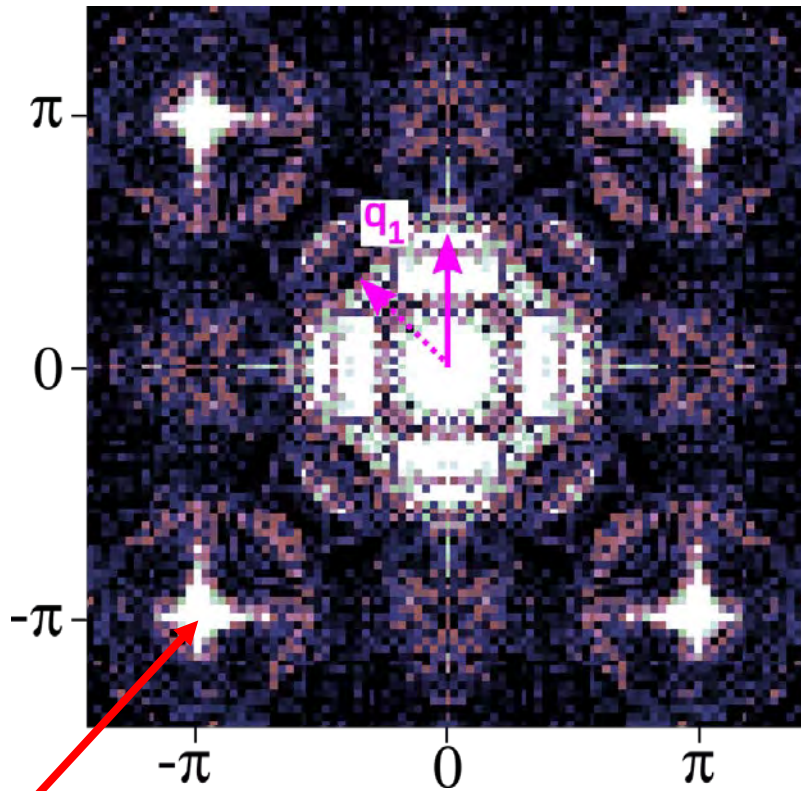
Reciprocal atomic lattice

Fermi surface (ARPES)



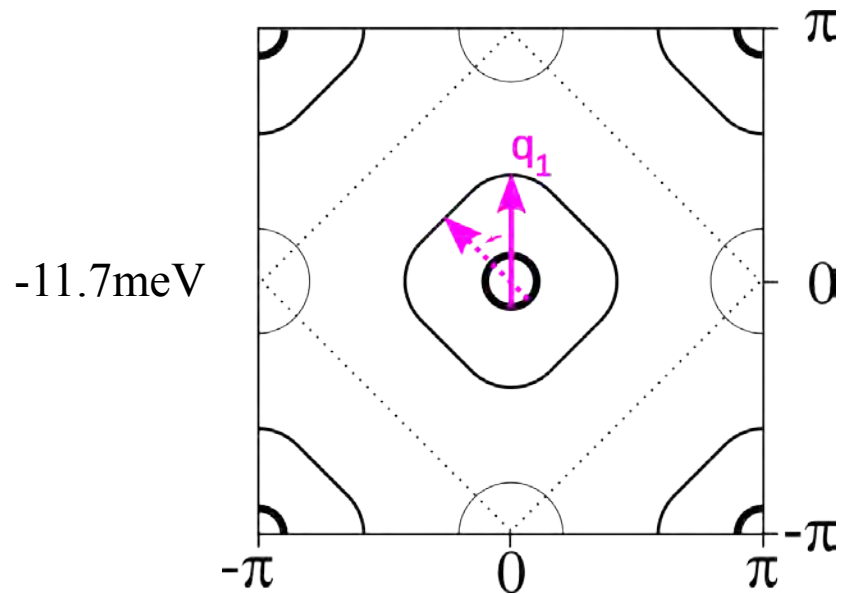
QPI matches experimental band structure

q-space image



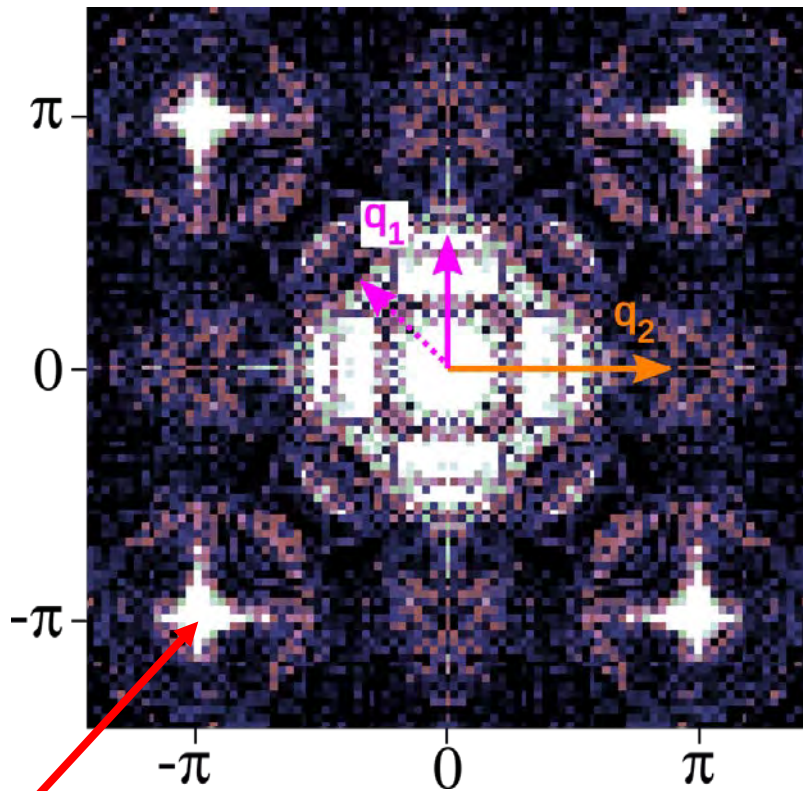
Reciprocal atomic lattice

ARPES band structure



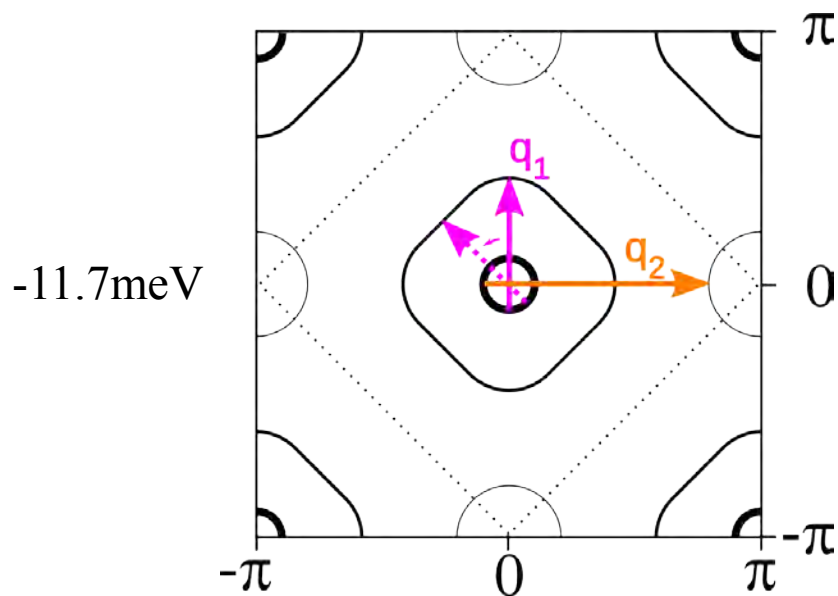
QPI matches experimental band structure

q-space image



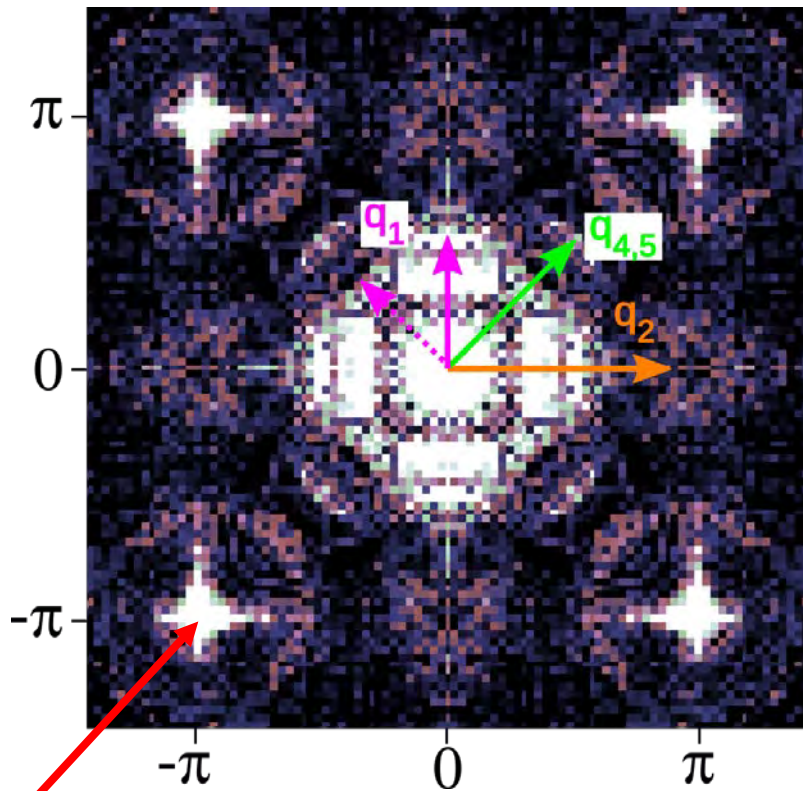
Reciprocal atomic lattice

ARPES band structure



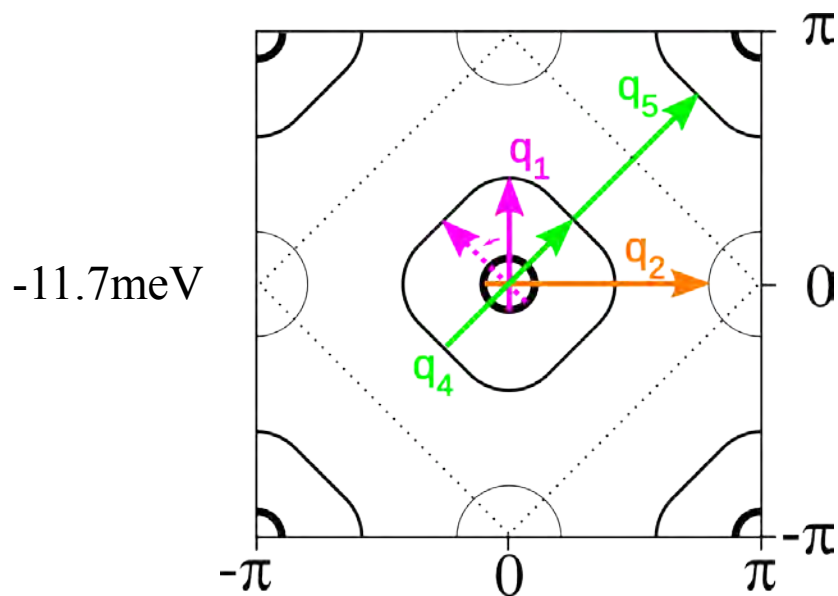
QPI matches experimental band structure

q-space image



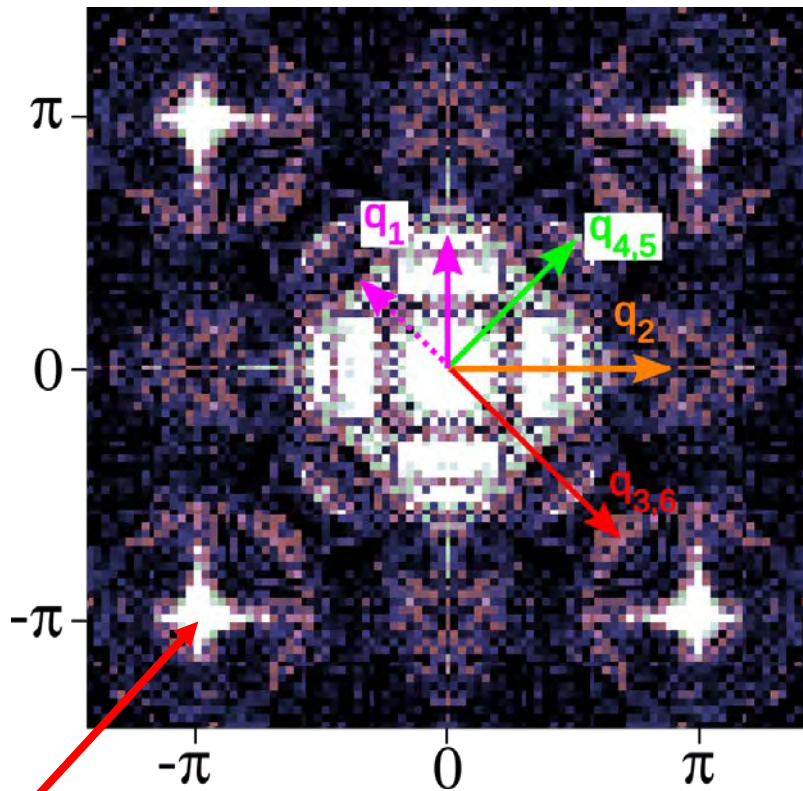
Reciprocal atomic lattice

ARPES band structure



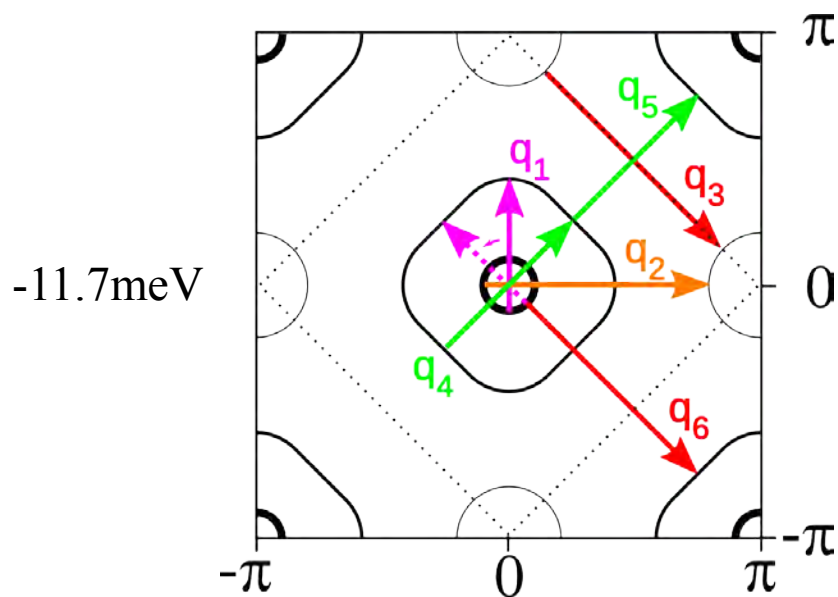
QPI matches experimental band structure

q-space image



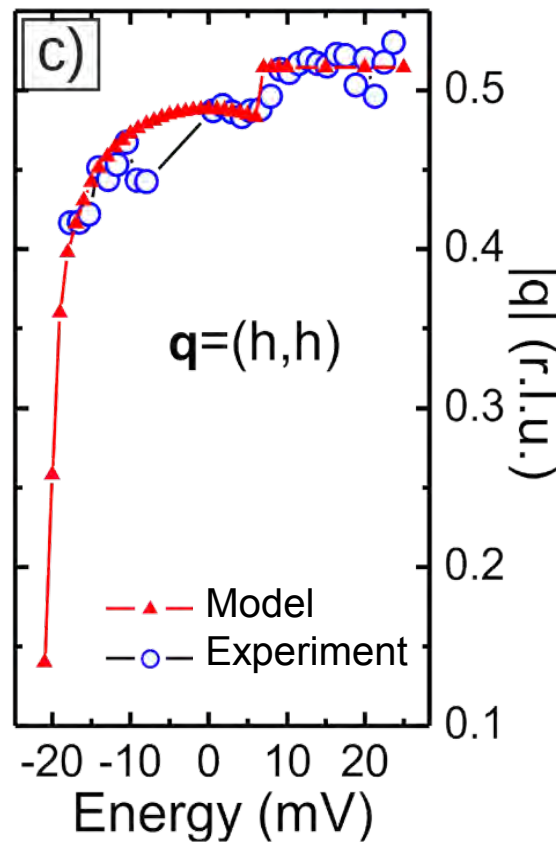
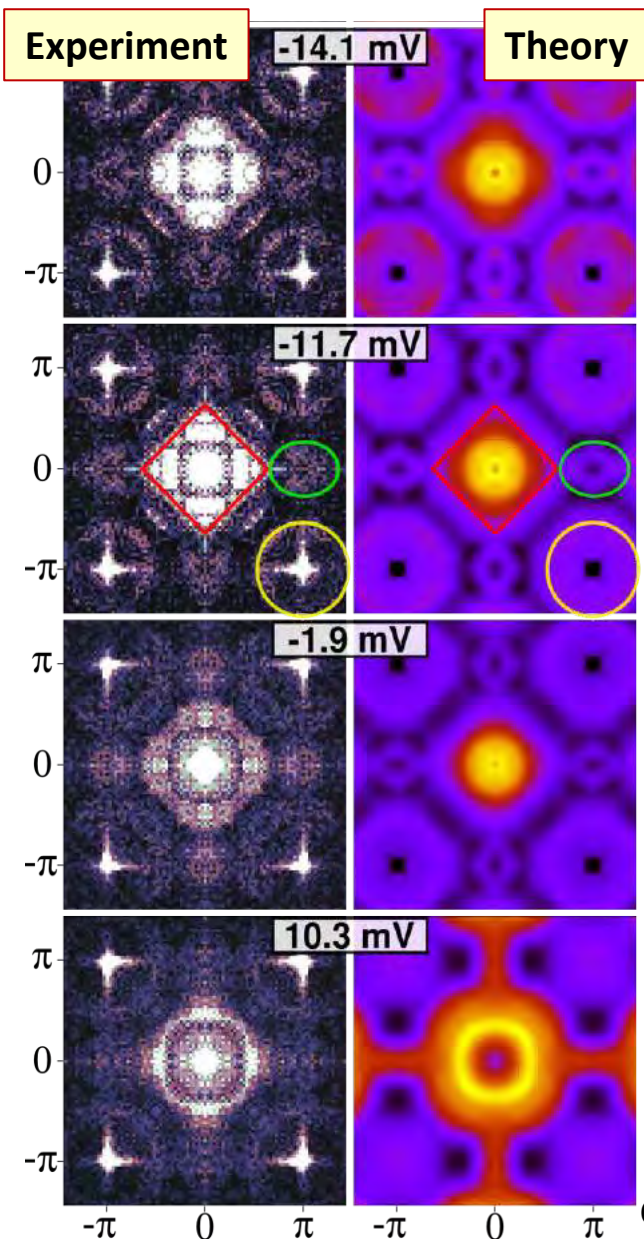
Reciprocal atomic lattice

ARPES band structure



QPI matches experimental band structure

QPI matches experimental band structure

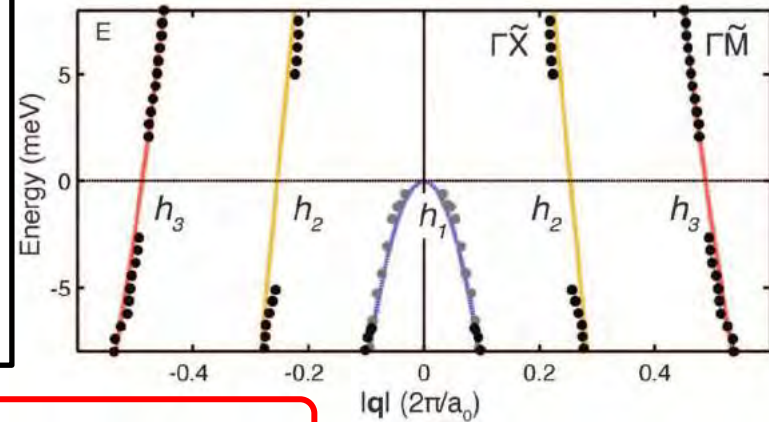


QPI matches experimental band structure

Interband vs intraband scattering

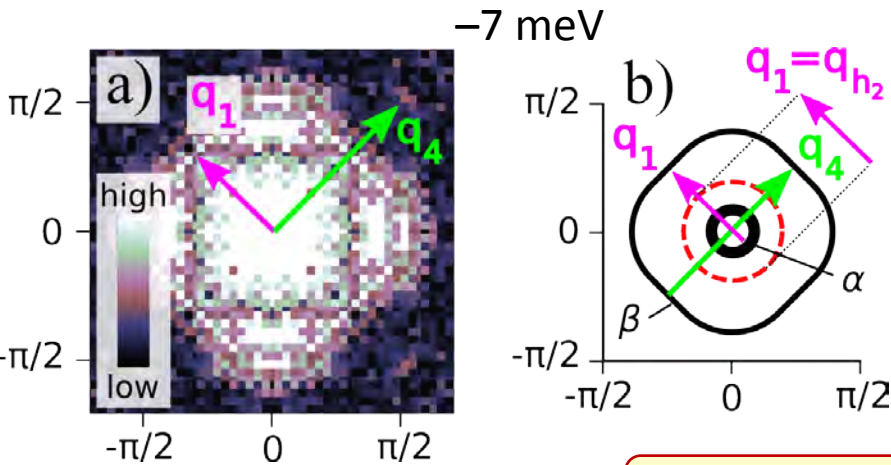
Anisotropic Energy Gaps of Iron-Based Superconductivity from **Intraband** Quasiparticle Interference in LiFeAs

M. P. Allan,^{1,2,3*} A. W. Rost,^{2,3*} A. P. Mackenzie,³ Yang Xie,² J. C. Davis,^{1,2,3,4†} K. Kihou,^{5,6} C. H. Lee,^{5,6} A. Iyo,^{5,6} H. Eisaki,^{5,6} T.-M. Chuang^{1,2,7†} **SCIENCE** VOL 336 4 MAY 2012

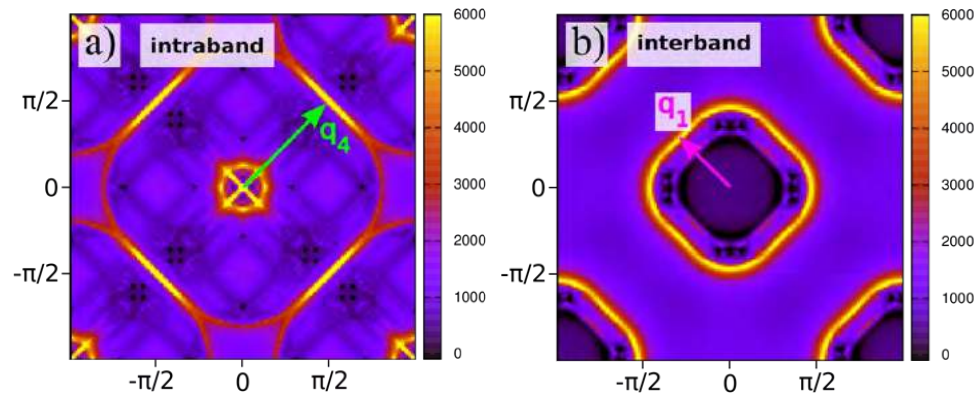


Three hole-like bands close E_F : h_2 inconsistent with ARPES data

Our data



QPI modelling (only hole-like bands)



$q_{h2} = q_1$ stems from **interband** scattering!

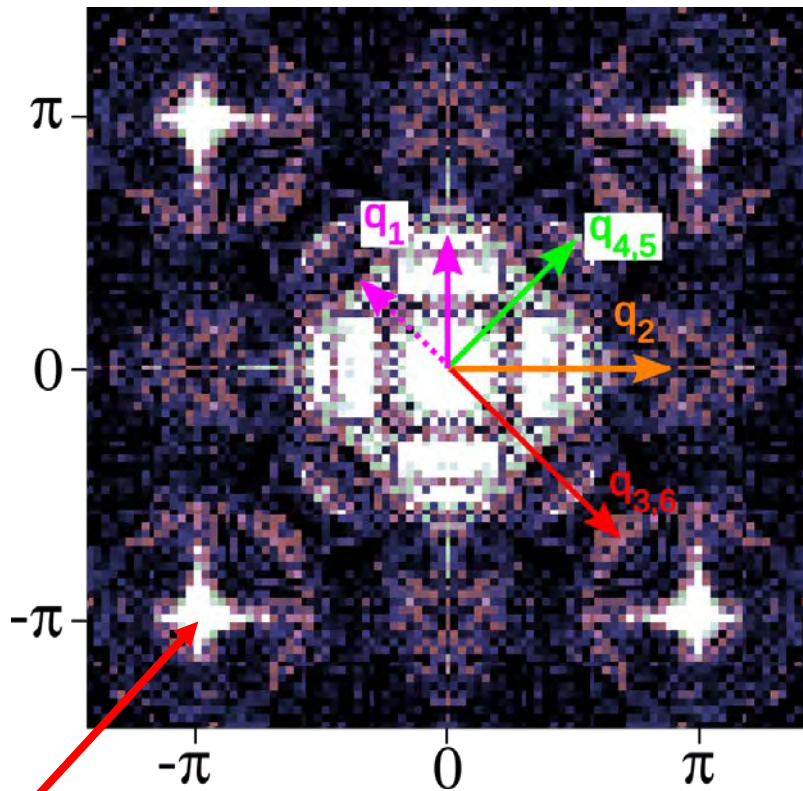
T. Hänke, CH et al., PRL 2012;

CH et al., PRL 2013

Calculations: S. Sykora

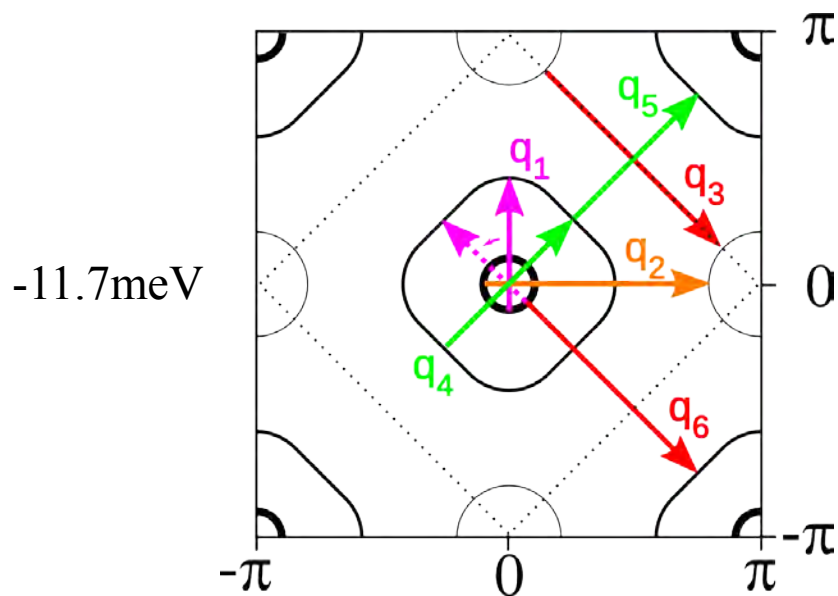
QPI matches experimental band structure

q-space image



Reciprocal atomic lattice

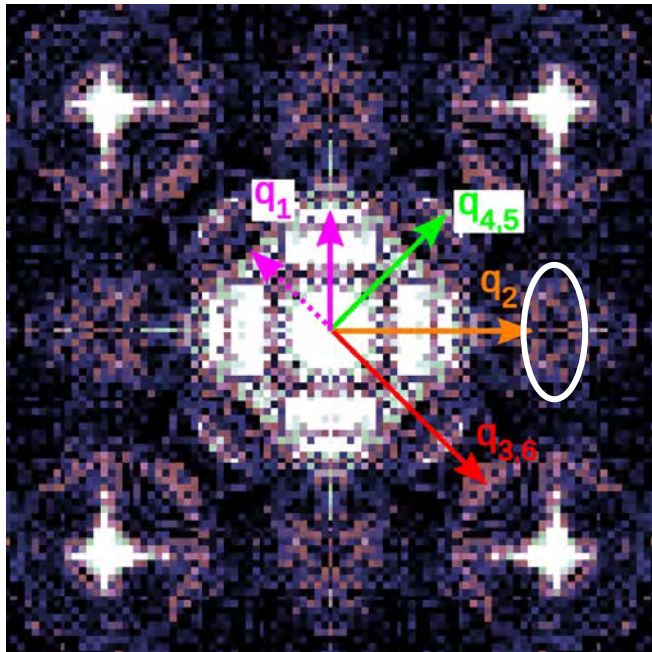
ARPES band structure



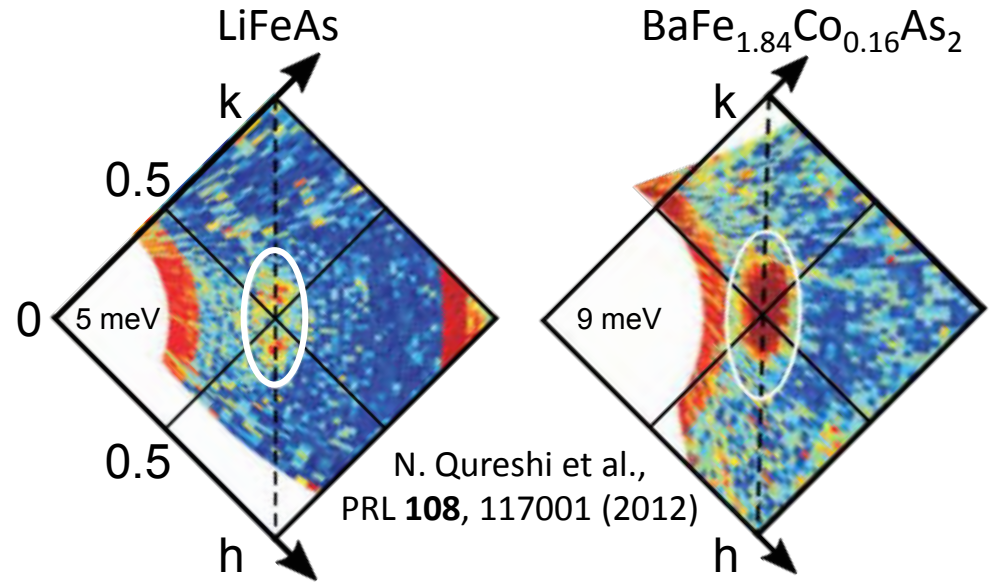
QPI matches experimental band structure

Consistent: ARPES, inelastic neutron scattering & QPI

Quasiparticle interference (QPI)



Inelastic neutron scattering (INS)

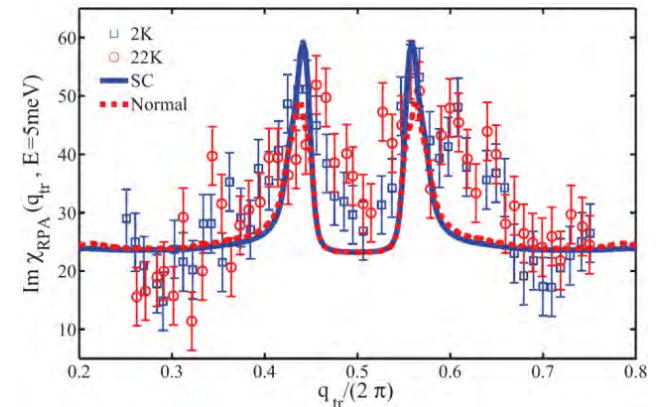


N. Qureshi et al.,
PRL **108**, 117001 (2012)

Incommensurate peaks: interband scattering

QPI matches inelastic neutron scattering

- INS+QPI: Weak scattering near $q_2 \sim Q_{\text{AFM}}$
 - QPI: Strong intensity at small q
- ➔ Small $q \leq q_1$ relevant for pairing?

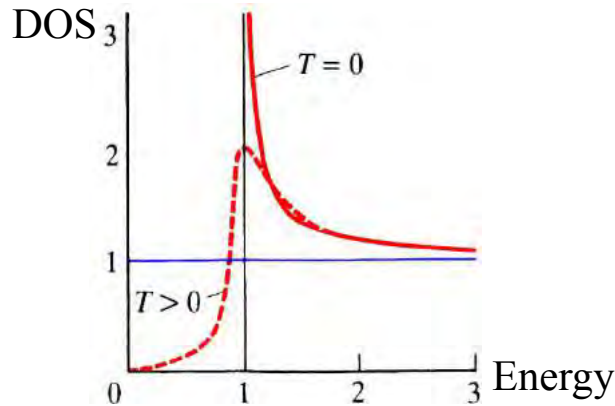


J. Knolle, CH et al., PRB **86**, 174519 (2012)

QPI and superconducting order parameter

Quasiparticle Interference in Superconductors

Quasiparticle Dispersion: $E_{\mathbf{k}} = \pm(\xi_{\mathbf{k}}^2 + |\Delta_{\mathbf{k}}|^2)^{1/2}$



↑
Normal State
Dispersion

↑
Gap function

Quasiparticle scattering & Coherence factors

- Standing QP waves with wave vector $\mathbf{q} = \mathbf{k}_i - \mathbf{k}_f$
- Scattering Rate $\propto (u_{\mathbf{k}_i} u_{\mathbf{k}_f} \pm v_{\mathbf{k}_i} v_{\mathbf{k}_f})$

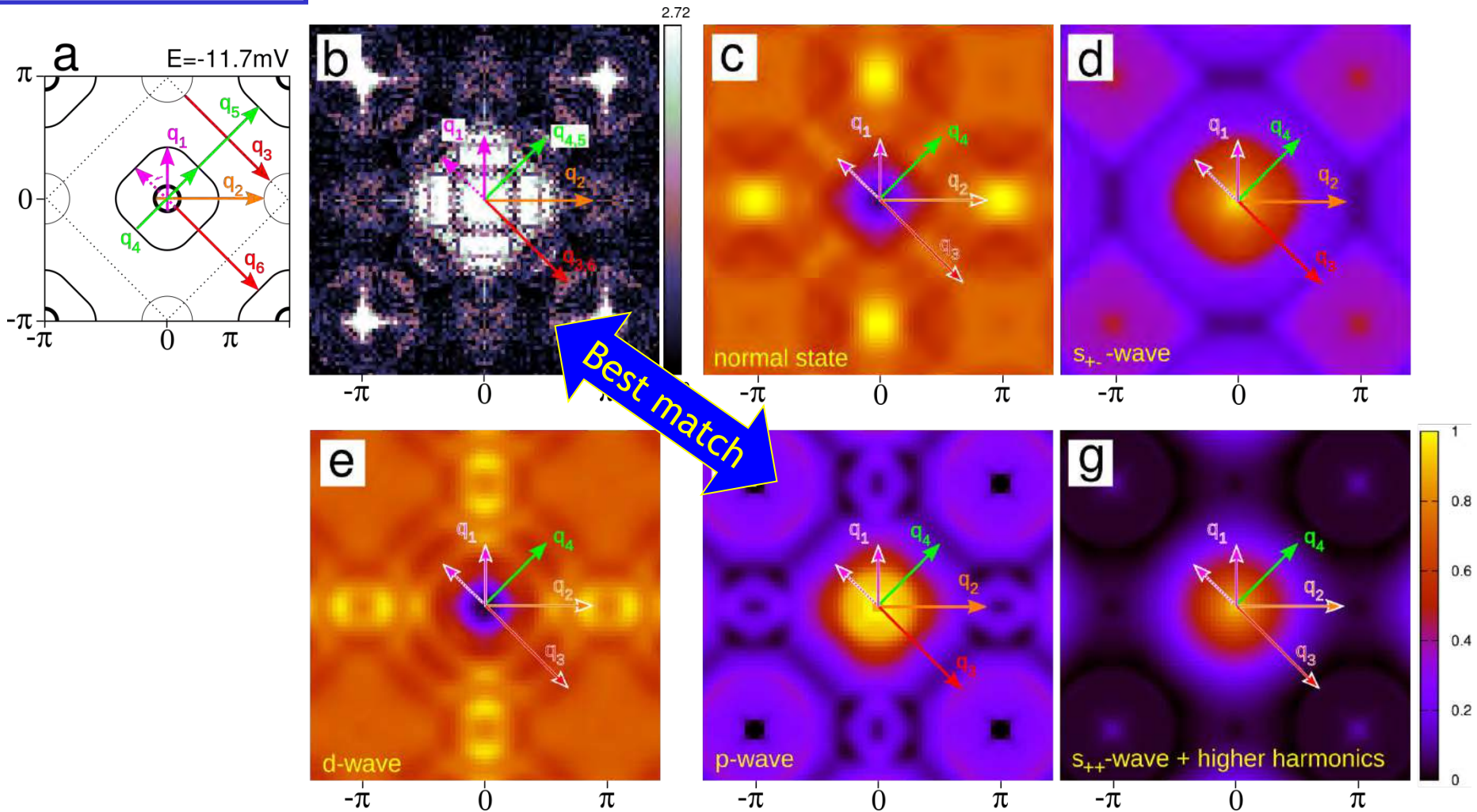
$$v_{\mathbf{k}}/u_{\mathbf{k}} = (E_{\mathbf{k}} - \xi_{\mathbf{k}})/\Delta_{\mathbf{k}}^* ; \quad u_{\mathbf{k}}^2 = 1 - v_{\mathbf{k}}^2$$

➡ **Phase sensitivity!**

- Interference pattern can directly be imaged in STM/STS

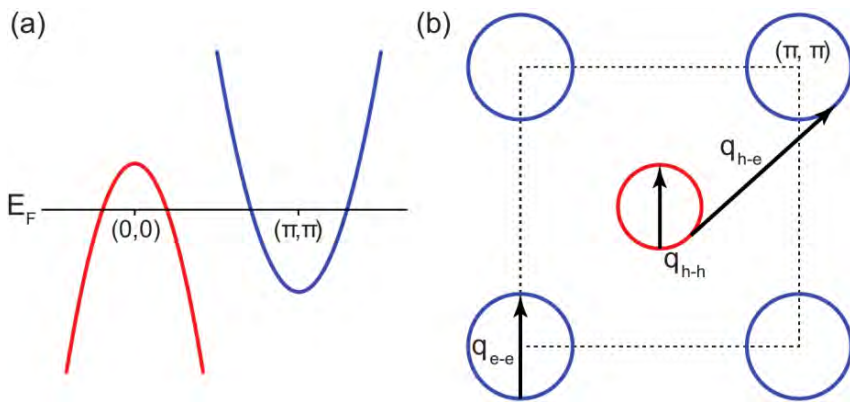
Compare with QPI Calculations

e.g., @ -11.7mV

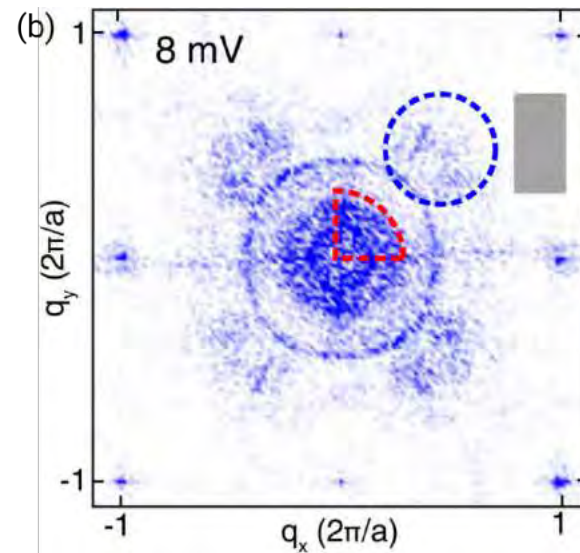
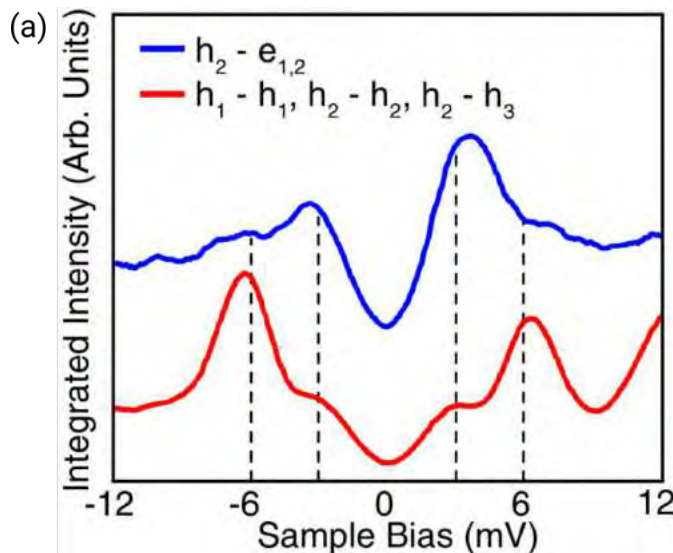


- Optimum agreement for assumed chiral p-wave pairing

Alternative Results



Scenario	\mathbf{q} Suppressed Intensity	\mathbf{q} Enhanced Intensity
nonmag. imp., s_{++}	$\mathbf{q}_{h-h}, \mathbf{q}_{e-e}, \mathbf{q}_{h-e}$	-
mag. imp., s_{++}	-	$\mathbf{q}_{h-h}, \mathbf{q}_{e-e}, \mathbf{q}_{h-e}$
nonmag. imp., s_{\pm}	$\mathbf{q}_{h-h}, \mathbf{q}_{e-e}$	\mathbf{q}_{h-e}
mag. imp., s_{\pm}	\mathbf{q}_{h-e}	$\mathbf{q}_{h-h}, \mathbf{q}_{e-e}$

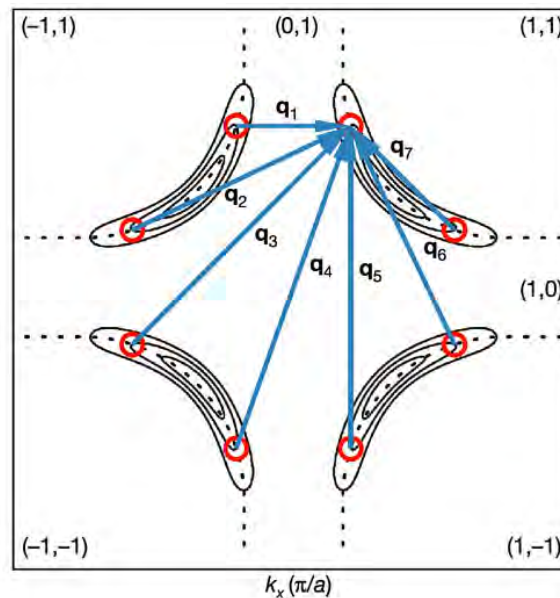
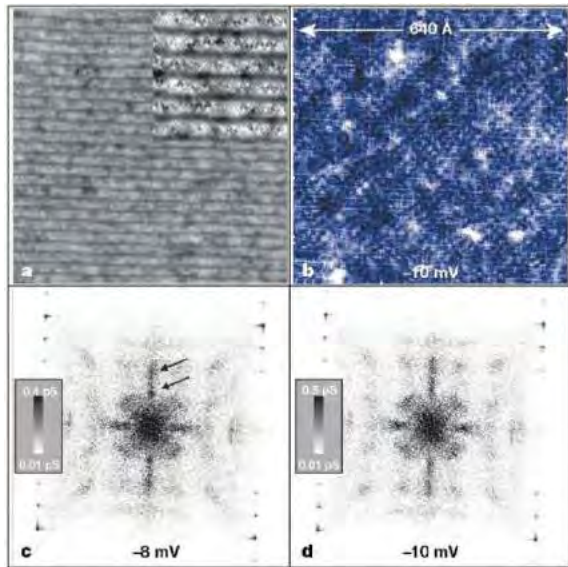


Data suggest s_{+-} -symmetry, if non-magnetic impurities are assumed.

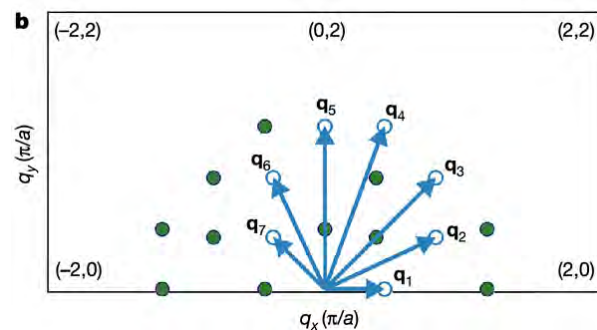
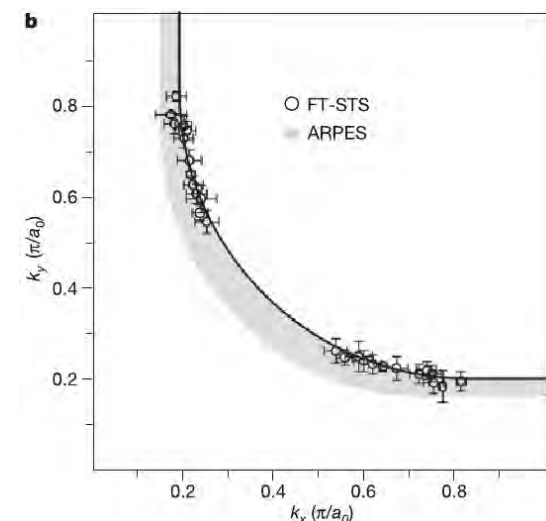
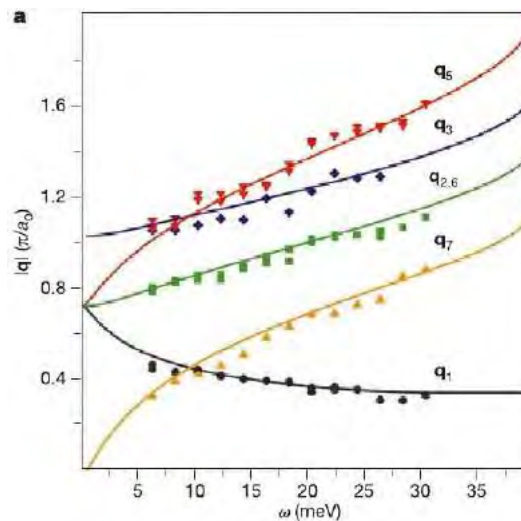
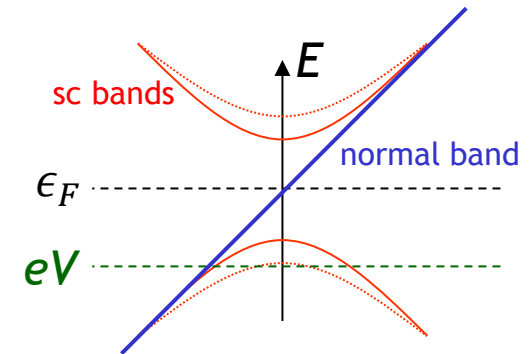
Cuprates

Quasiparticle Interference in Cuprates

Example: QPI in cuprate superconductors ($\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$): octet model

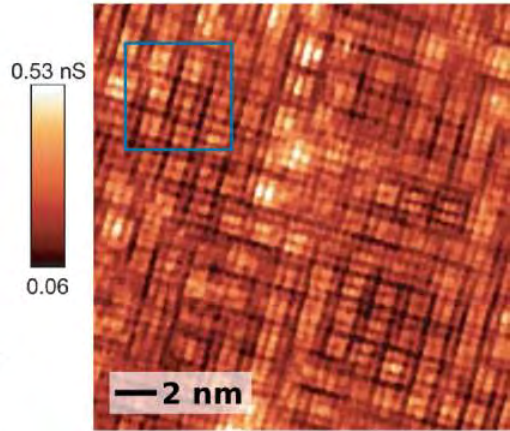
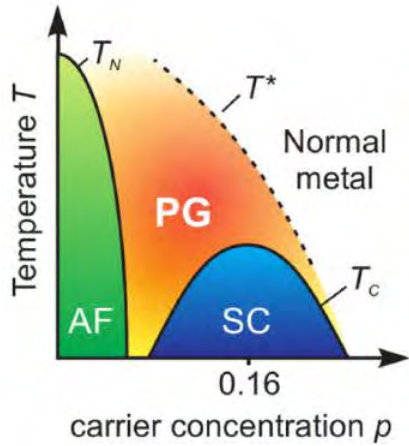


Enhanced QP DOS at banana tips:

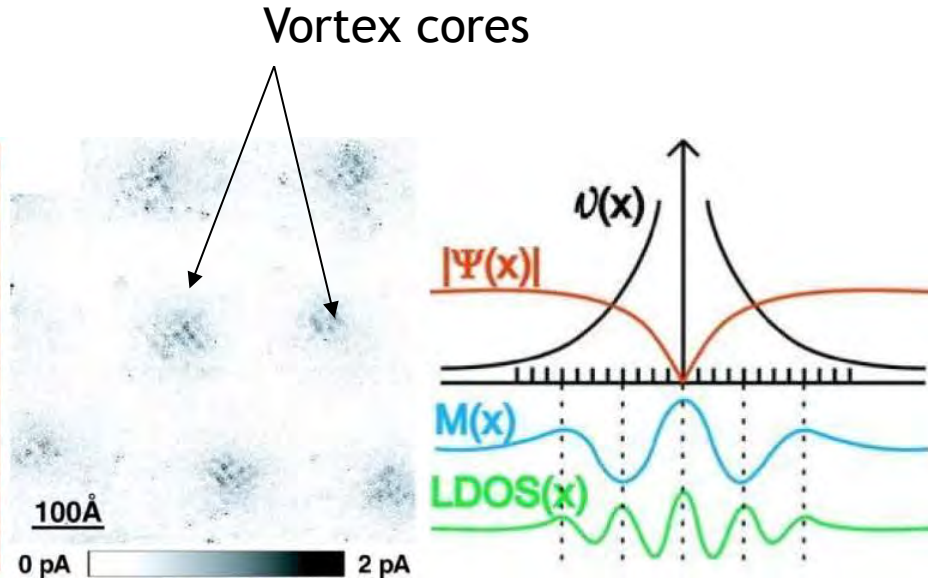


J.E. Hoffman et al., Science **297**, 1148 (2002)
 K. McElroy et al., Nature **422**, 592 (2003)
 Q.-H. Wang & D.-H. Lee, PRB **67**, 020511R (2003)

Cuprates: Nanoscale electronic order?



$\text{Ca}_{1.9}\text{Na}_{0.1}\text{CuO}_2\text{Cl}_2$
 $E = 24 \text{ meV}$



$\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$

Acknowledgements

At IFW

T. Hänke, D. Baumann, R. Schlegel, P.K. Nag

L. Harnagea, S. Wurmehl, R. Beck, B. Büchner

U. Gräfe, H. Grafe

S. Sykora, J. van den Brink

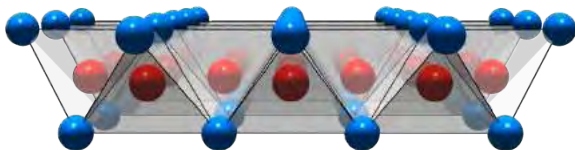
STM

Samples

NQR

Theory

GRK 1621



SPP1458

Deutsche
Forschungsgemeinschaft

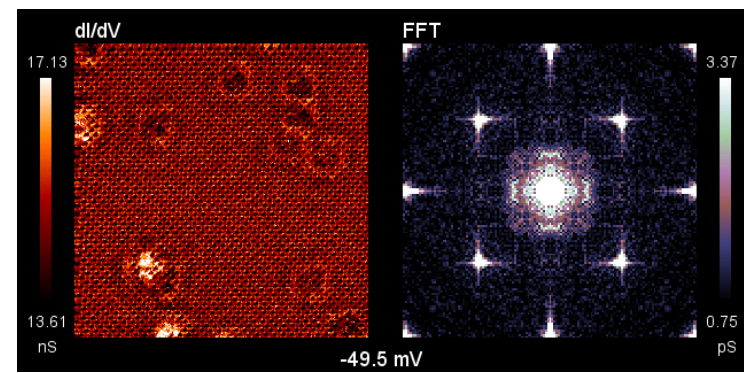
DFG



European Research Council

Established by the European Commission

Summary



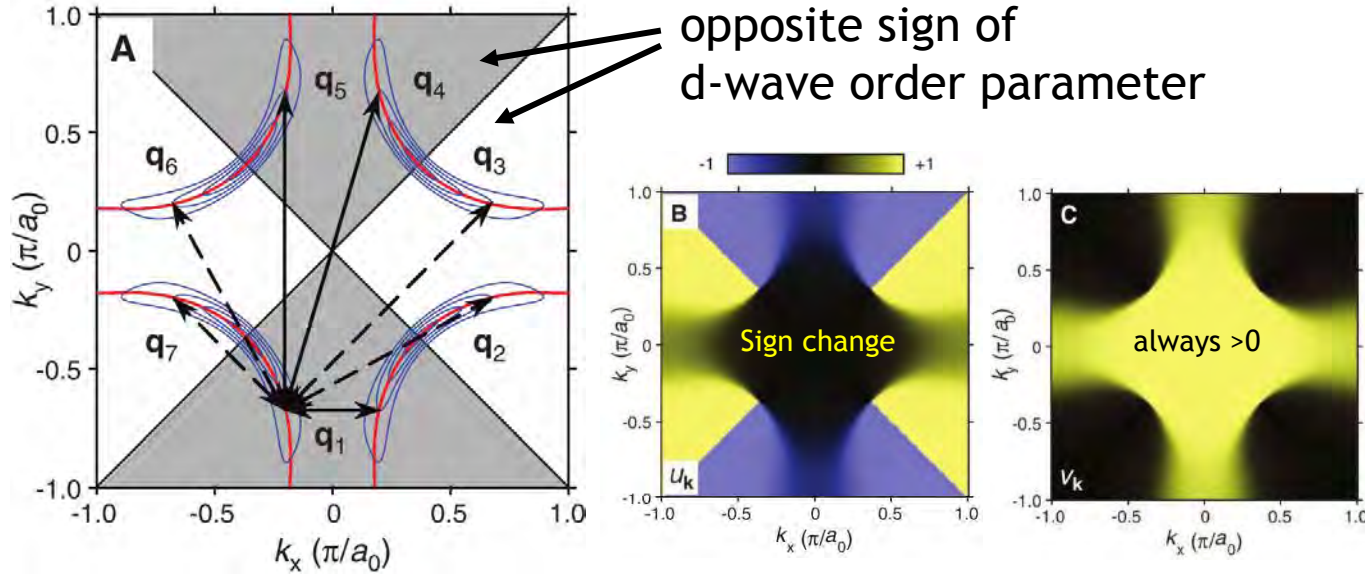
- **Magnetic vortex spectroscopy** → coherence length
- **Gap spectroscopy**
- **Quasiparticle interference** → band structure (order parameter)

other topics:

- **Defect spectroscopy** → information on sc order parameter
[arXiv:1603.07777](#); [arXiv:1607.03192](#)
- **Superconductivity and magnetism (spin-polarized STM)**
future...

Quasiparticle Interference in Superconductors

Example: QPI & coherence factors in cuprate superconductors ($\text{Ca}_{2-x}\text{Na}_x\text{CuO}_2\text{Cl}_2$):



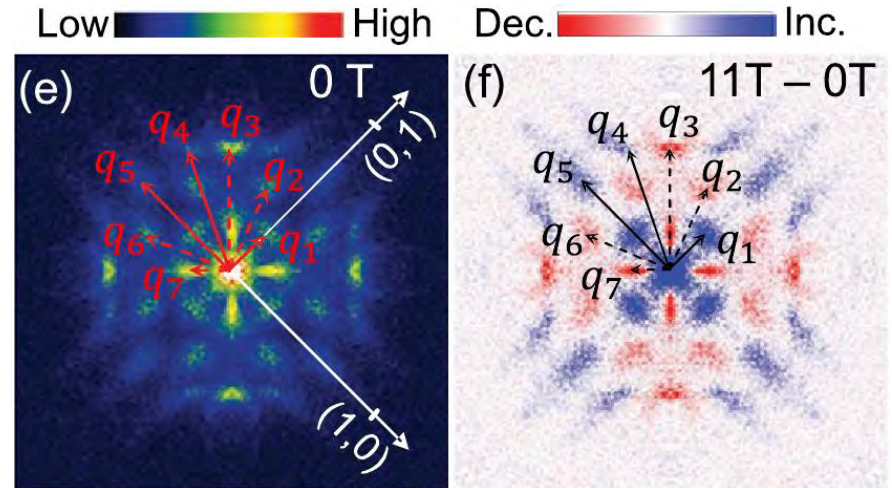
Potential scatterer

$$C(\mathbf{k}_i, \mathbf{k}_f) = (u_{\mathbf{k}_i}u_{\mathbf{k}_f} - v_{\mathbf{k}_i}v_{\mathbf{k}_f})^2$$

Magnetic scatterer

$$C(\mathbf{k}_i, \mathbf{k}_f) = (u_{\mathbf{k}_i}u_{\mathbf{k}_f} + v_{\mathbf{k}_i}v_{\mathbf{k}_f})^2$$

➡ Extinction possible: q_2, q_3, q_6, q_7



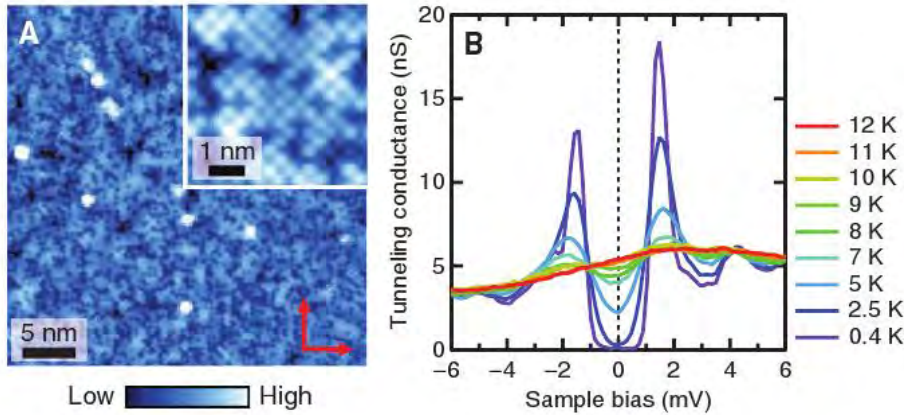
Idea: enhance magnetic scattering by magnetic field

Quasiparticle Interference in Fe(Se,Te)

Unconventional s-Wave Superconductivity in Fe(Se,Te)

T. Hanaguri,^{1,2*} S. Niitaka,^{1,2} K. Kuroki,^{2,3} H. Takagi^{1,2,4}

SCIENCE 328, 474, (2010)



Potential scatterer

$$C(\mathbf{k}_i, \mathbf{k}_f) = (u_{\mathbf{k}_i} u_{\mathbf{k}_f} - v_{\mathbf{k}_i} v_{\mathbf{k}_f})^2$$

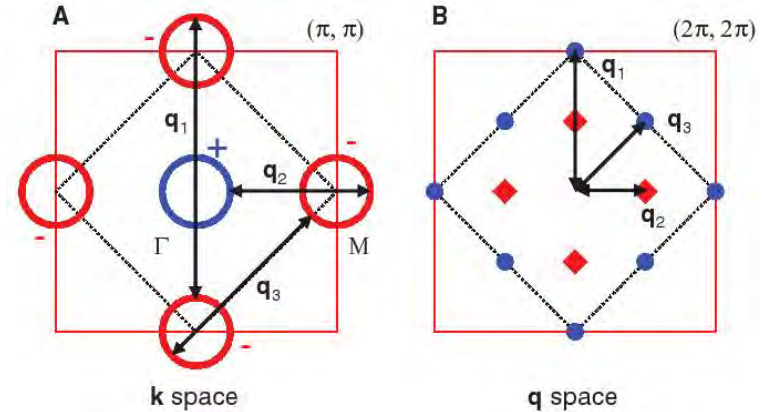
Magnetic scatterer

$$C(\mathbf{k}_i, \mathbf{k}_f) = (u_{\mathbf{k}_i} u_{\mathbf{k}_f} + v_{\mathbf{k}_i} v_{\mathbf{k}_f})^2$$

Idea:

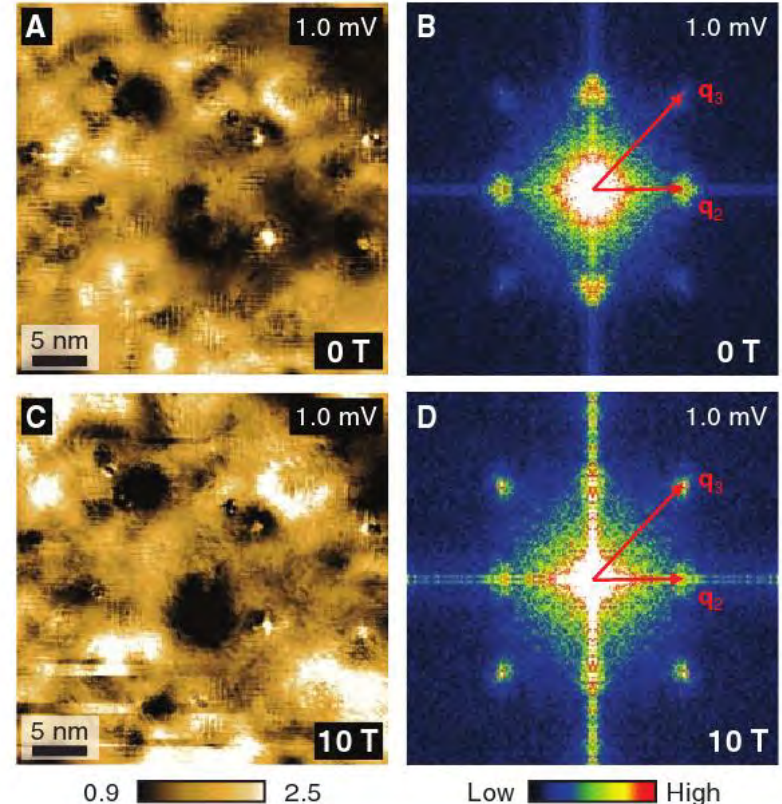
Magnetic field enhances sign preserving scattering (due to enhanced magnetic scattering)

→ Evidence for s_{\pm} -symmetry



$$Z(r, E) = g(r, +E) / g(r, -E)$$

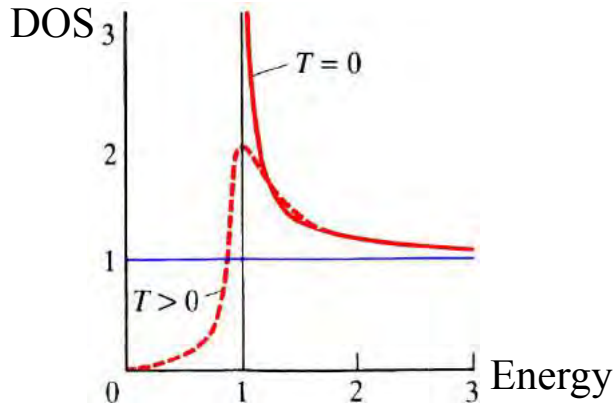
FT-Z



Quasiparticle interference (in superconductors)

Quasiparticle Interference in Superconductors

Quasiparticle Dispersion: $E_{\mathbf{k}} = \pm(\xi_{\mathbf{k}}^2 + |\Delta_{\mathbf{k}}|^2)^{1/2}$



Normal State
Dispersion

Gap function

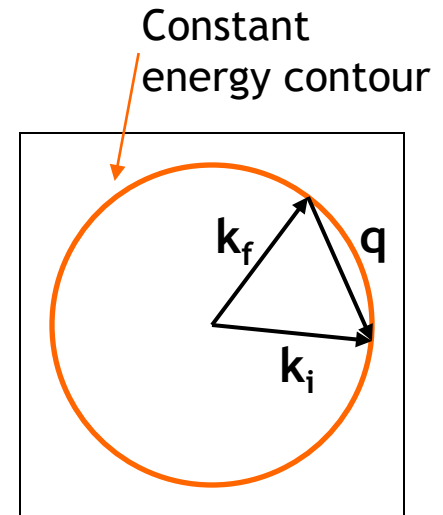
Quasiparticle scattering & Coherence factors

- Standing QP waves with wave vector $\mathbf{q} = \mathbf{k}_i - \mathbf{k}_f$
- Scattering Rate $\propto (u_{\mathbf{k}_i} u_{\mathbf{k}_f} \pm \nu_{\mathbf{k}_i} \nu_{\mathbf{k}_f})$

$$\nu_{\mathbf{k}}/u_{\mathbf{k}} = (E_{\mathbf{k}} - \xi_{\mathbf{k}})/\Delta_{\mathbf{k}}^* ; \quad u_{\mathbf{k}}^2 = 1 - \nu_{\mathbf{k}}^2$$

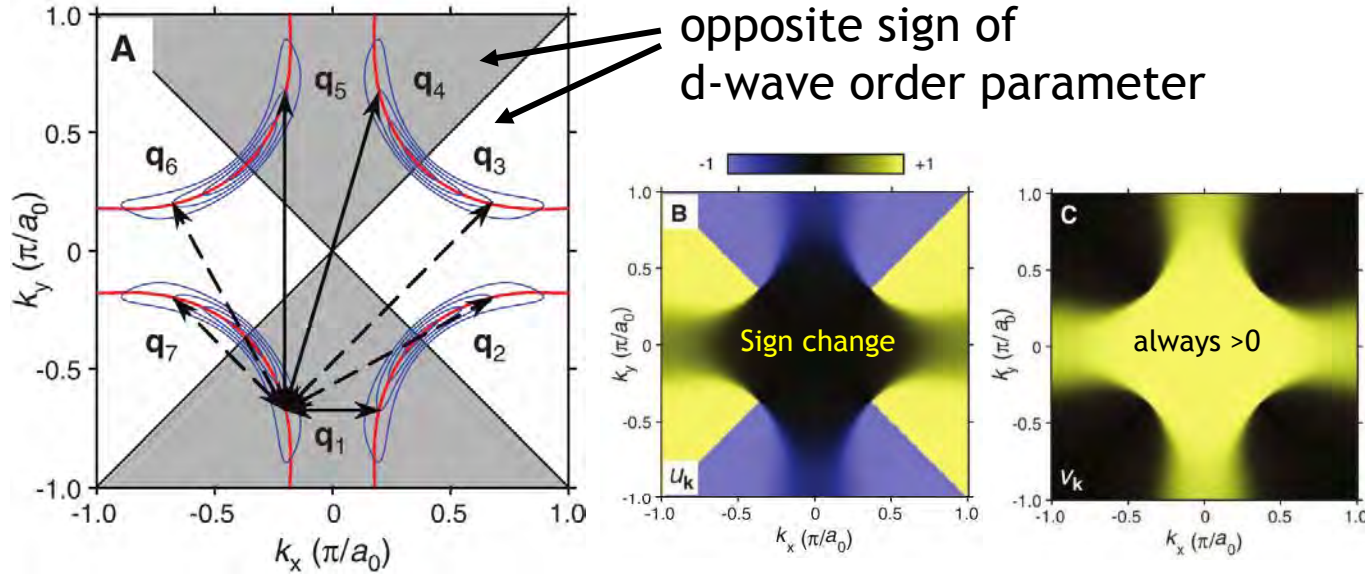
➡ Phase sensitivity!

- Interference pattern can directly be imaged in STM/STS



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Example: QPI & coherence factors in cuprate superconductors ($\text{Ca}_{2-x}\text{Na}_x\text{CuO}_2\text{Cl}_2$):



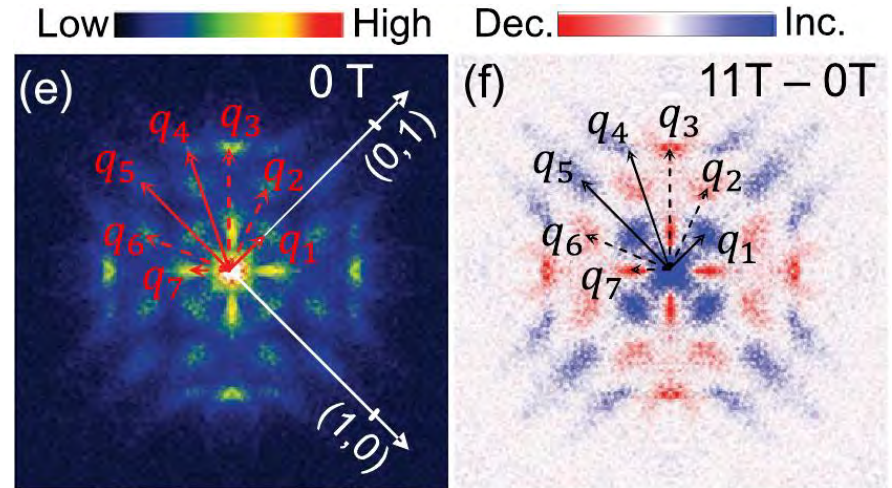
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$$C(\mathbf{k}_i, \mathbf{k}_f) = (u_{\mathbf{k}_i}u_{\mathbf{k}_f} + v_{\mathbf{k}_i}v_{\mathbf{k}_f})^2$$

➡ Extinction possible: q_2, q_3, q_6, q_7



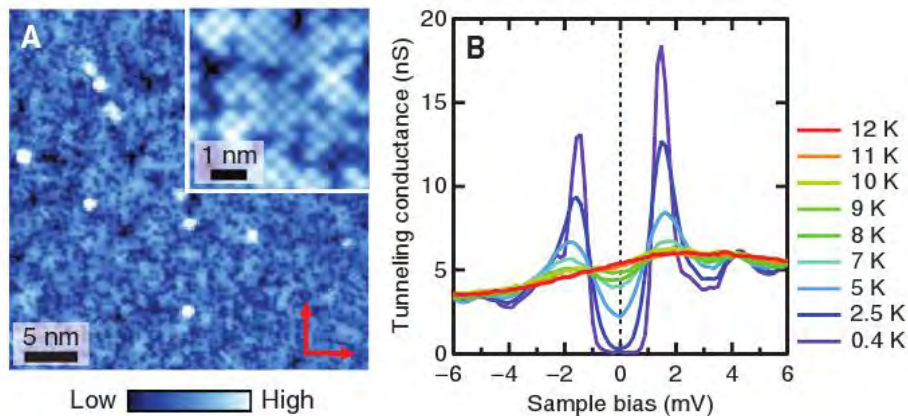
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SCIENCE 328, 474, (2010)



Potential scatterer

$$C(\mathbf{k}_i, \mathbf{k}_f) = (u_{\mathbf{k}_i} u_{\mathbf{k}_f} - v_{\mathbf{k}_i} v_{\mathbf{k}_f})^2$$

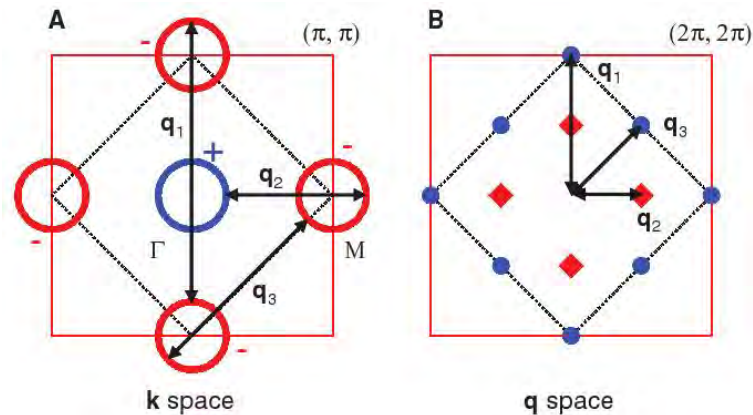
Magnetic scatterer

$$C(\mathbf{k}_i, \mathbf{k}_f) = (u_{\mathbf{k}_i} u_{\mathbf{k}_f} + v_{\mathbf{k}_i} v_{\mathbf{k}_f})^2$$

Idea:

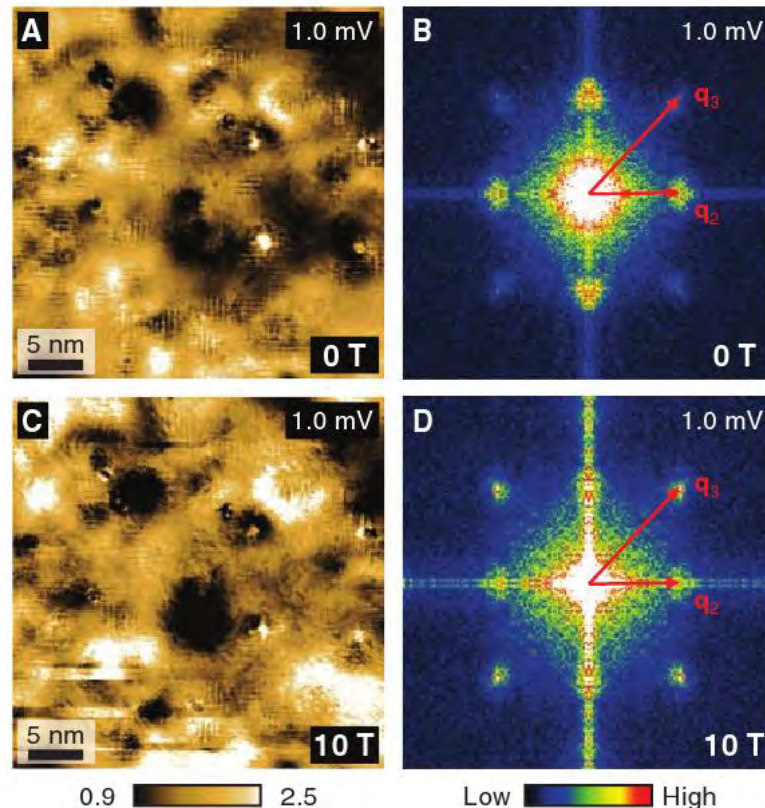
Magnetic field enhances sign preserving scattering (due to enhanced magnetic scattering)

→ Evidence for s_{\pm} -symmetry



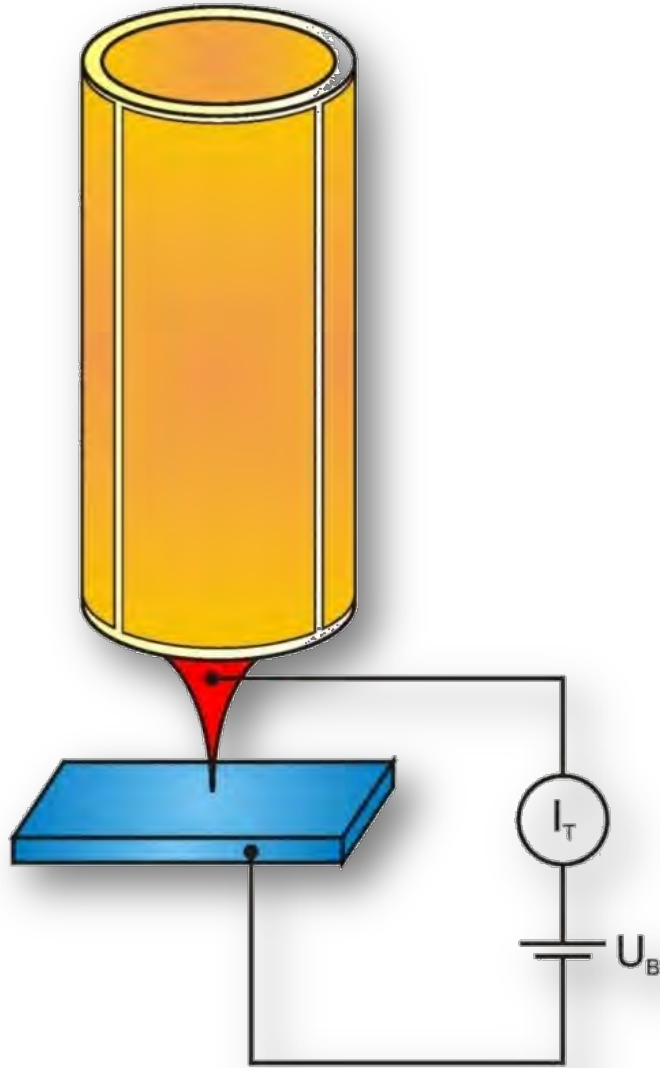
$$Z(r, E) = g(r, +E) / g(r, -E)$$

FT-Z



„Real“ Microscopes

STM - basic setup



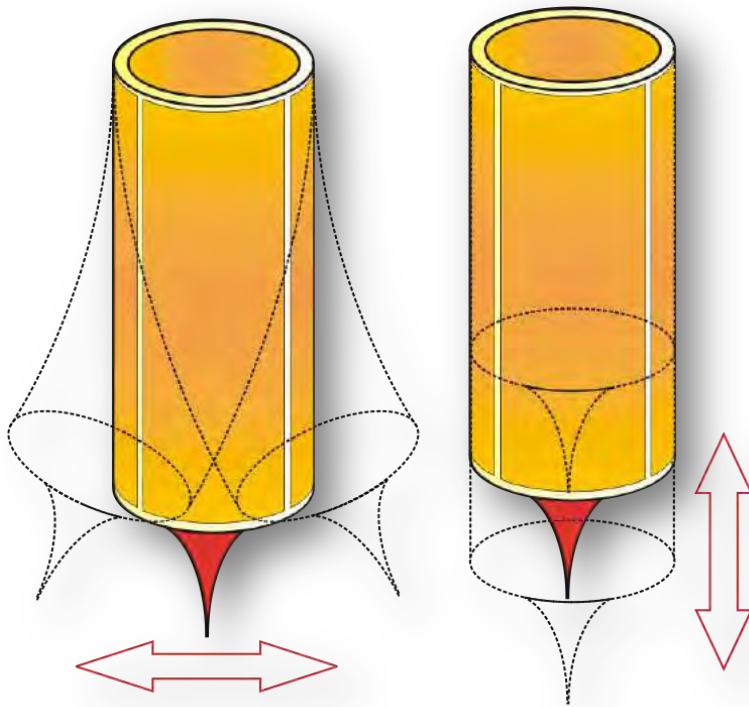
Tip positioning

- Use piezo electric tube scanner
- Four 90° outside electrodes
- One inside electrode

Movement:

- Apply el. field
- Changing partially the scanner length
- 3 dim. movement with sub Å accuracy

STM - basic setup

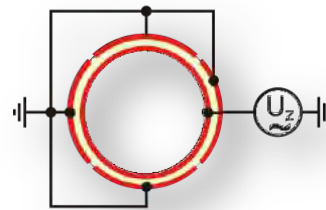
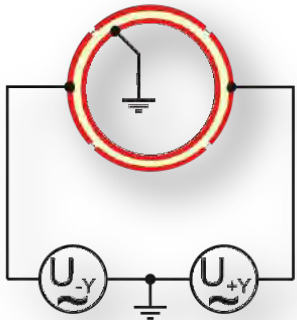


Tip positioning

- Use piezo electric tube scanner
- Four 90° outside electrodes
- One inside electrode

Movement:

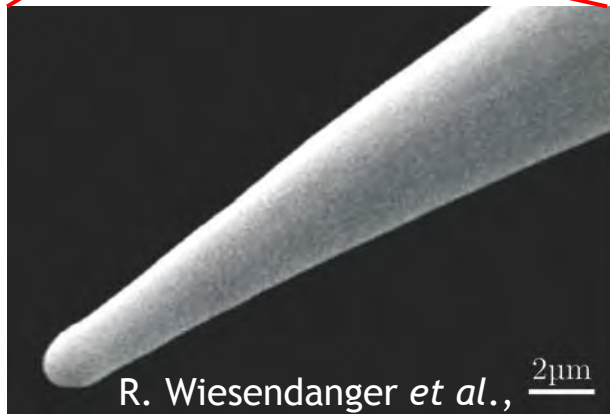
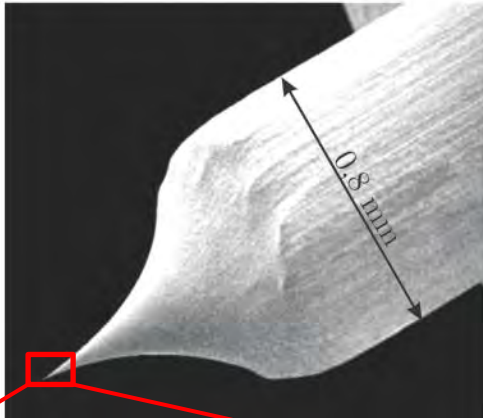
- Apply el. field
- Changing partially the scanner length
- 3 dim. movement with sub Å accuracy



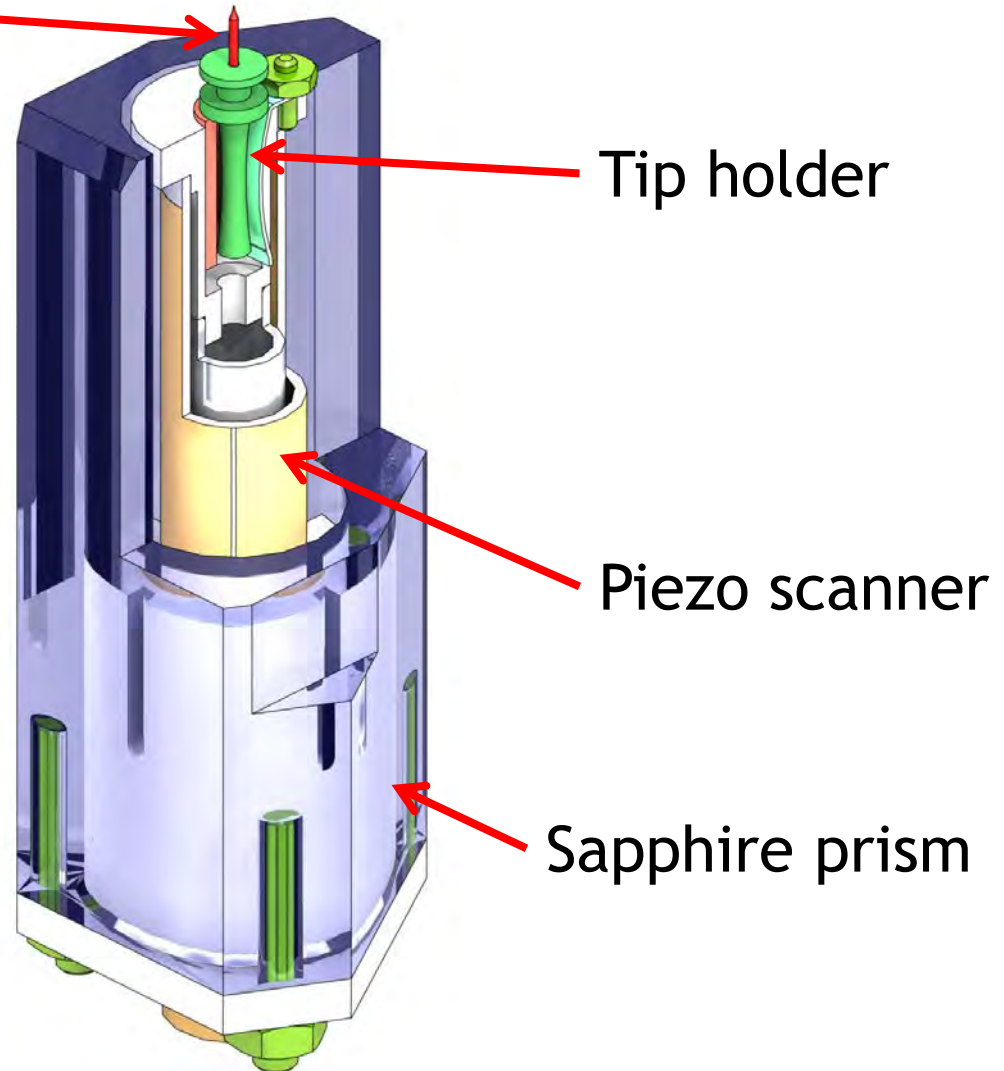
STM - basic setup

STM tip

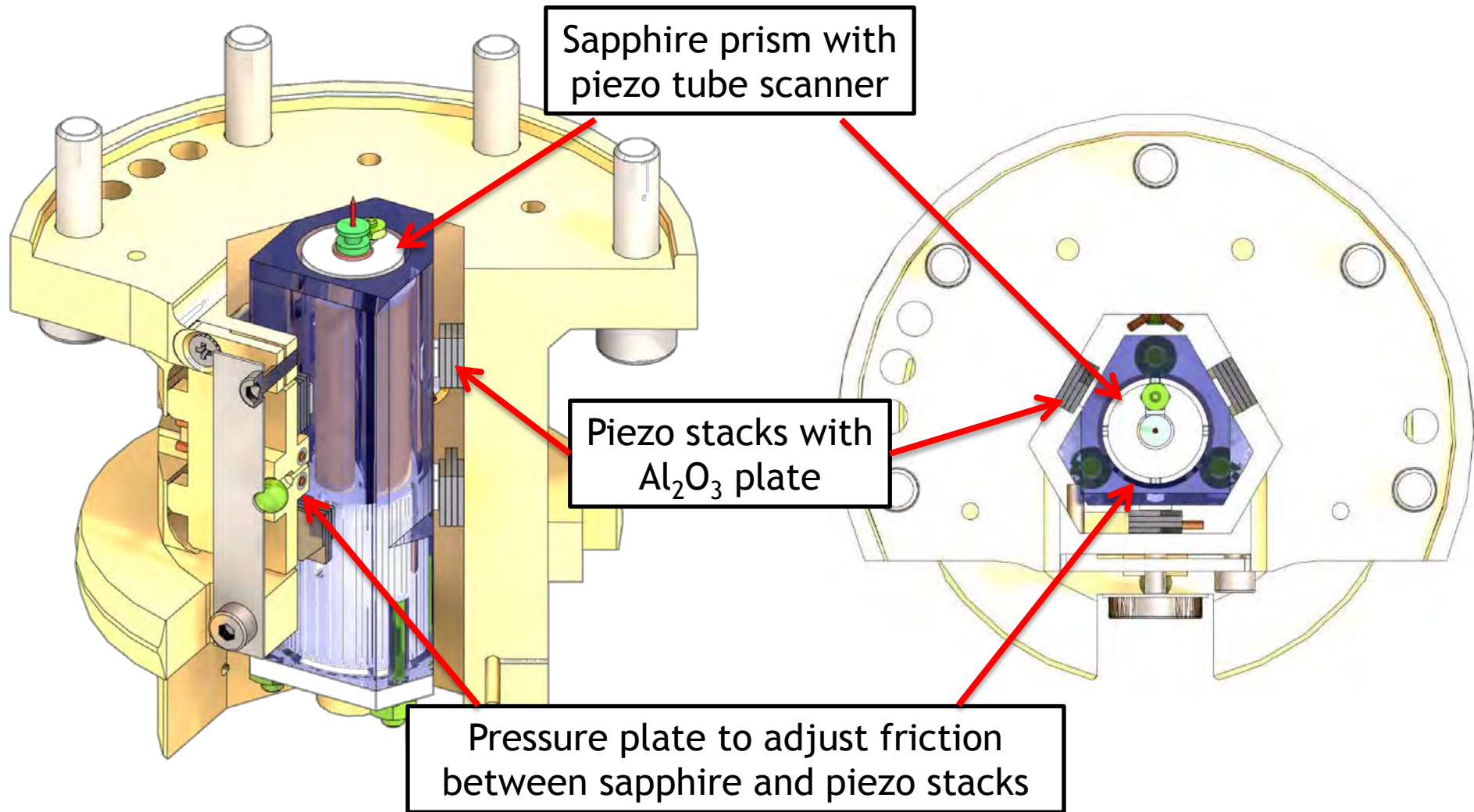
SEM image of wet etched W-tip:



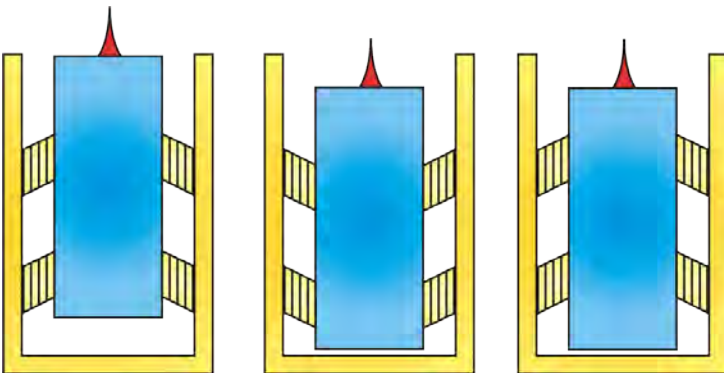
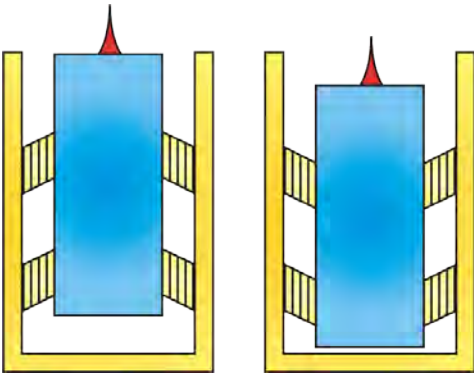
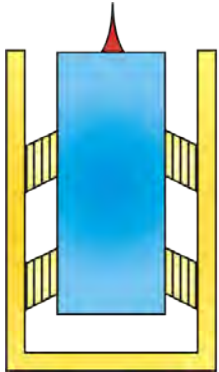
Rev. Mod. Phys. 81, 1495 (2009)



STM - basic setup

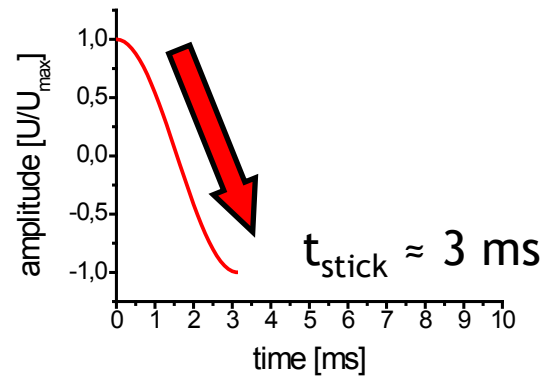


STM - basic setup

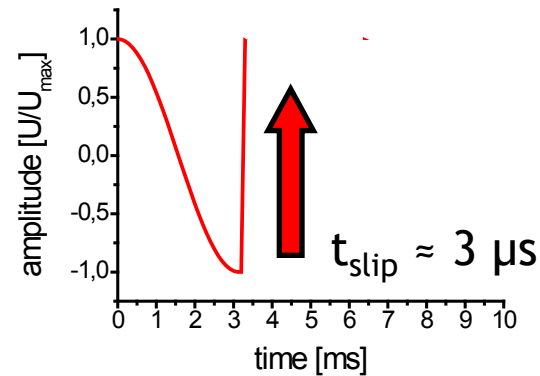


Starting position

$$V = V_{\max}$$



‘Stick’ - Phase
slow movement of
the piezo stacks



‘Slip’ - Phase
fast movement of
the piezo stacks

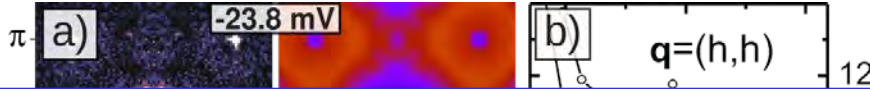
STM's @ IFW-Dresden

Description	VT-STM	Dip-Stick STM	300 mK STM
Atmosphere	UHV – $p \approx 10^{-9}$ mbar	Cryogenic vacuum	UHV - $p \approx 10^{-11}$ mbar
Temperature Range	14 K – RT	4.8 K – below RT	268 mK – 40 K
Scanning range	3.4 μm x 3.4 μm	2 μm x 2 μm	1 μm x 1 μm
Magnetic field	No field	Up to 18 T	9 T superconducting magnet
Energy resolution	3.6 meV	1.2 meV	100 μeV
Sample exchange	10 min	1 day	1.5 days
Acquisition time	\sim 1 day	6 weeks	8 days
Typical samples	Nanostructures, Molecules	Unconventional Superconductors	Unconventional superconductors

Good match between experimental and theoretical dispersion

Is it really triplet???

Experiment Theory



PHYSICAL REVIEW B **83**, 060501(R) (2011)



Theory of magnetism and triplet superconductivity in LiFeAs

PHYSICAL REVIEW B **84**, 235121 (2011)

P. M

¹Instit

Superconducting state of the iron pnictide LiFeAs: A combined density-functional and functional-renormalization-group study

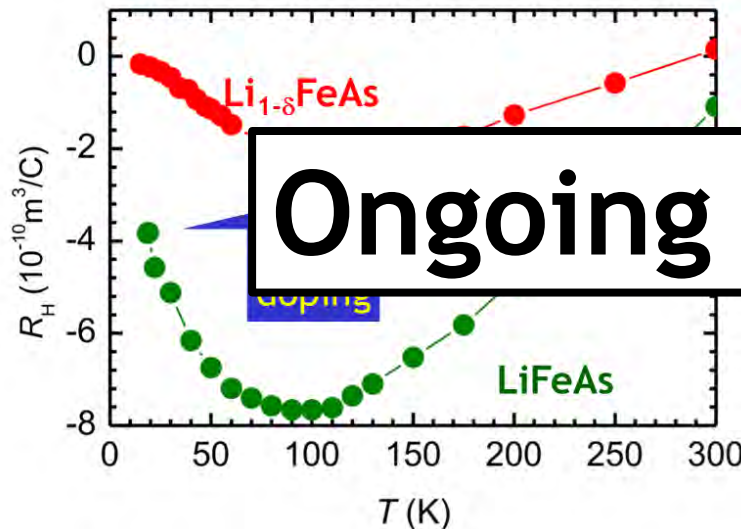
⁷⁵As NMR-NQR study in superconducting LiFeAs

S.-H. Baek^a, H.-J. Grafo, F. Hammerath, M. Fuchs, C. Rudisch, L. Harnagea, S. Aswartham, S. Wurmehl, J. van den Brink, and B. Büchner

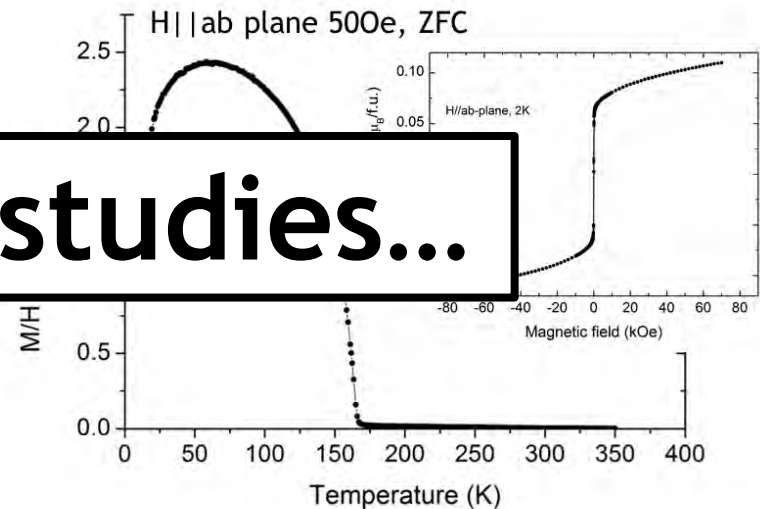
PHYSICAL REVIEW B **87**, 024512 (2013)

Anomalous hysteresis as evidence for a magnetic-field-induced chiral

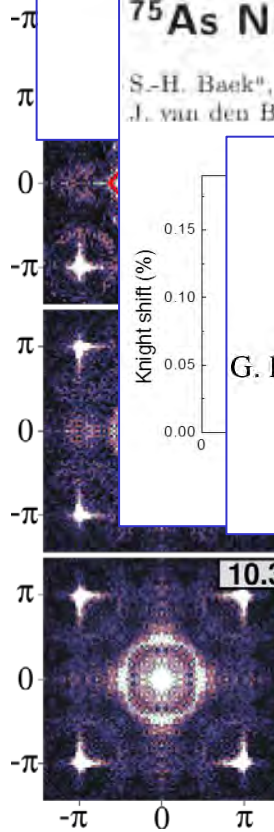
Hall effect



Magnetization



Ongoing studies...



Summary Slide

- **Tunneling Current:**

$$I \propto e^{-2\kappa s} \int_{-eV}^0 N_2(E) dE$$

distance DOS_{sample}

➡ Topography (contours of constant integrated DOS)

➡ LDOS maps

- **Measurement of**

➡ Gap spectroscopy (gap size, bosonic modes)

➡ Vortex mapping (Vortex lattice, coherence length)

➡ Quasiparticle interference (band structure, order parameter)

Unconventional superconductivity in LiFeAs as seen by STM/STS

Summer School on Iron-Pnictides
Storkow 4.4. - 08.04. 2016

Christian Hess



IFW Dresden
*Institute for
Solid State Research*

Outline

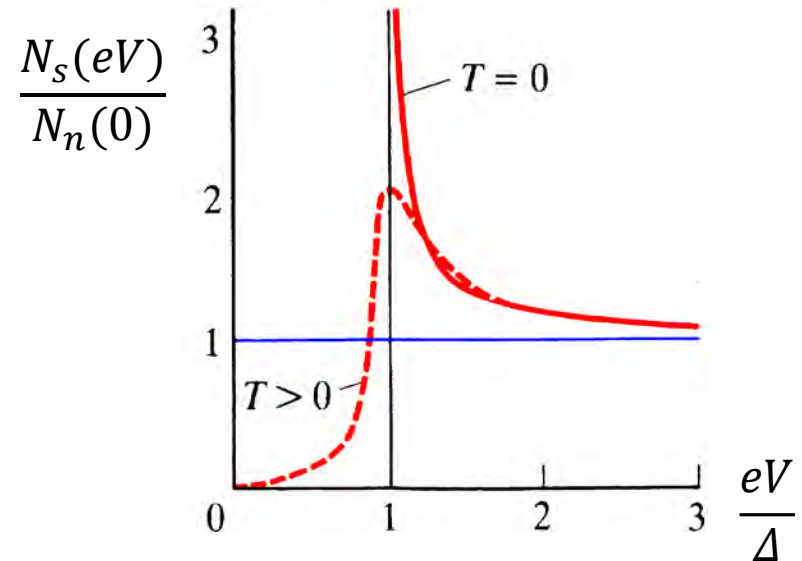
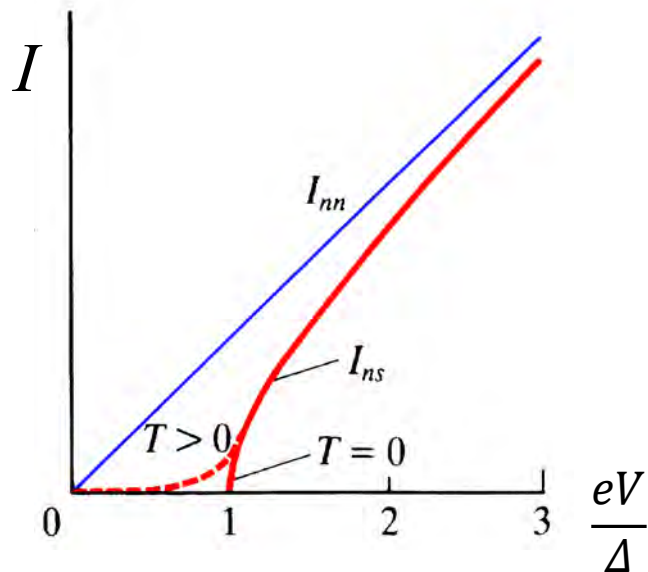
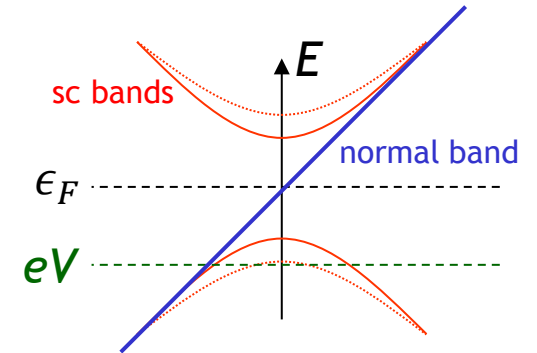
- Iron pnictides: magnetism vs superconductivity
- Magnetic vortex spectroscopy
- Quasiparticle interference in LiFeAs
- Gap spectroscopy

Tunneling spectra in superconductors

Elektronentunneln: Normalleiter - Supraleiter

From BCS-Theory: $E_k^2 = \xi_k^2 + \Delta_k^2$

$$\frac{N_s(E)}{N_n(0)} = \frac{d\xi}{dE} = \begin{cases} \frac{E}{\sqrt{(E^2 - \Delta^2)}} & (E > \Delta) \\ 0 & (E < \Delta) \end{cases}$$



Electron tunneling: normal metal (Al) - superconductor (Pb)

VOLUME 5, NUMBER 4

PHYSICAL REVIEW LETTERS

AUGUST 15, 1960

ENERGY GAP IN SUPERCONDUCTORS MEASURED BY ELECTRON TUNNELING

Ivar Giaever

General Electric Research Laboratory, Schenectady, New York

(Received July 5, 1960)

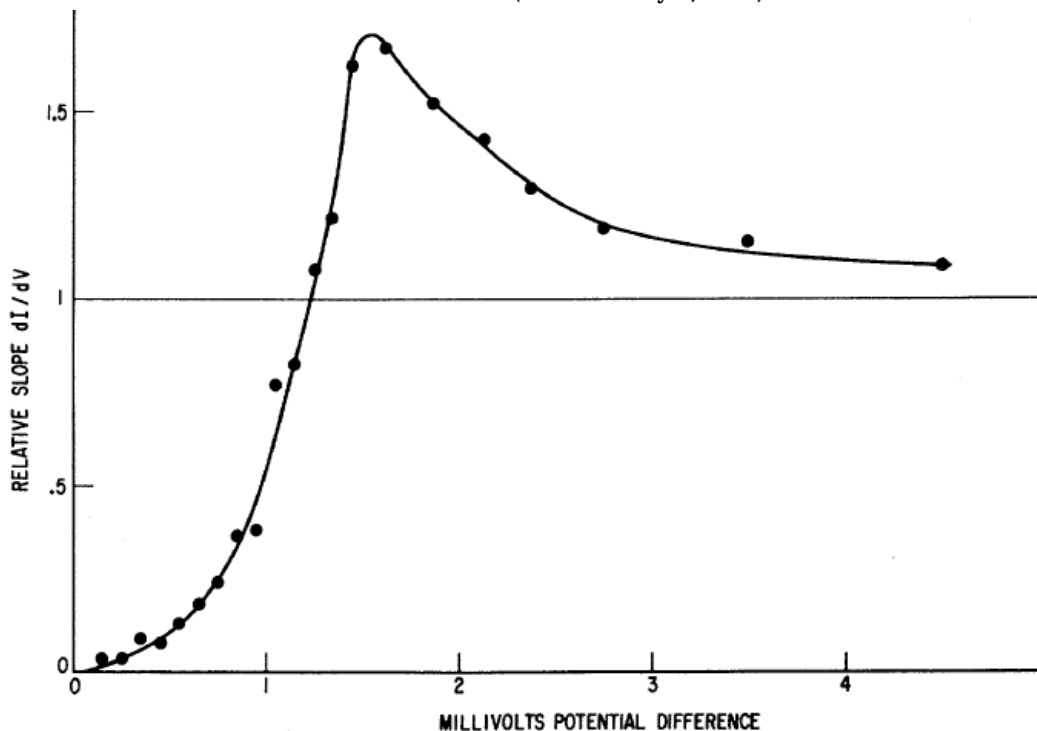


FIG. 2. From Fig. 1, slope dI/dV of curve 5 relative to slope of curve 1.

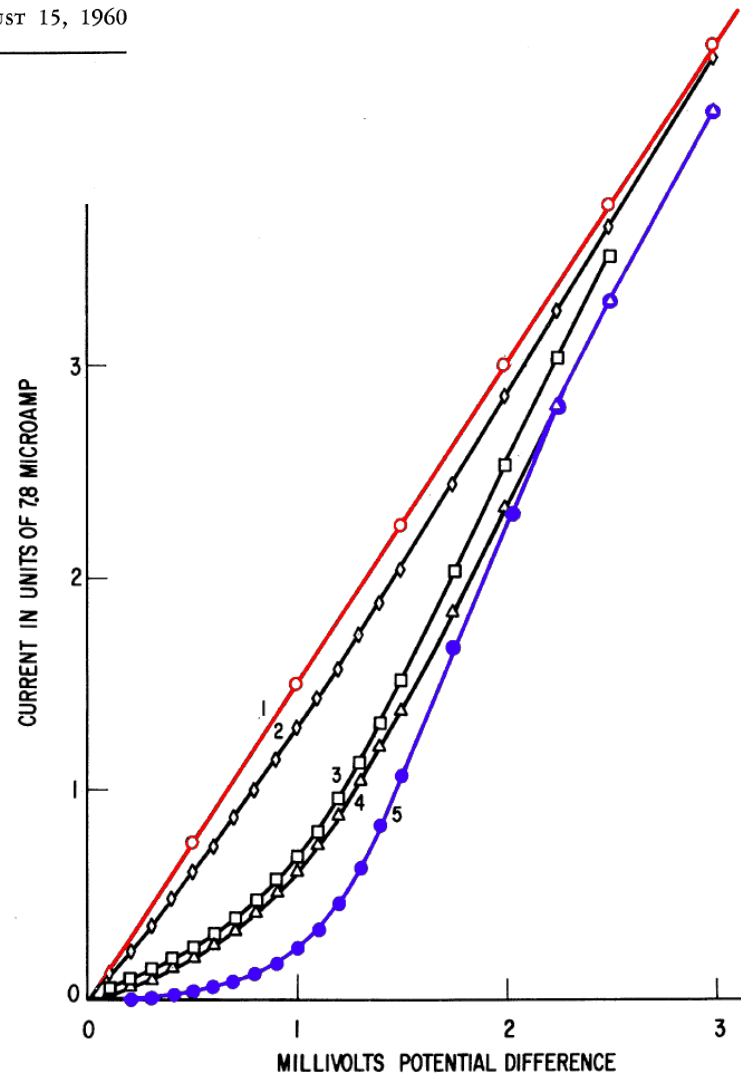
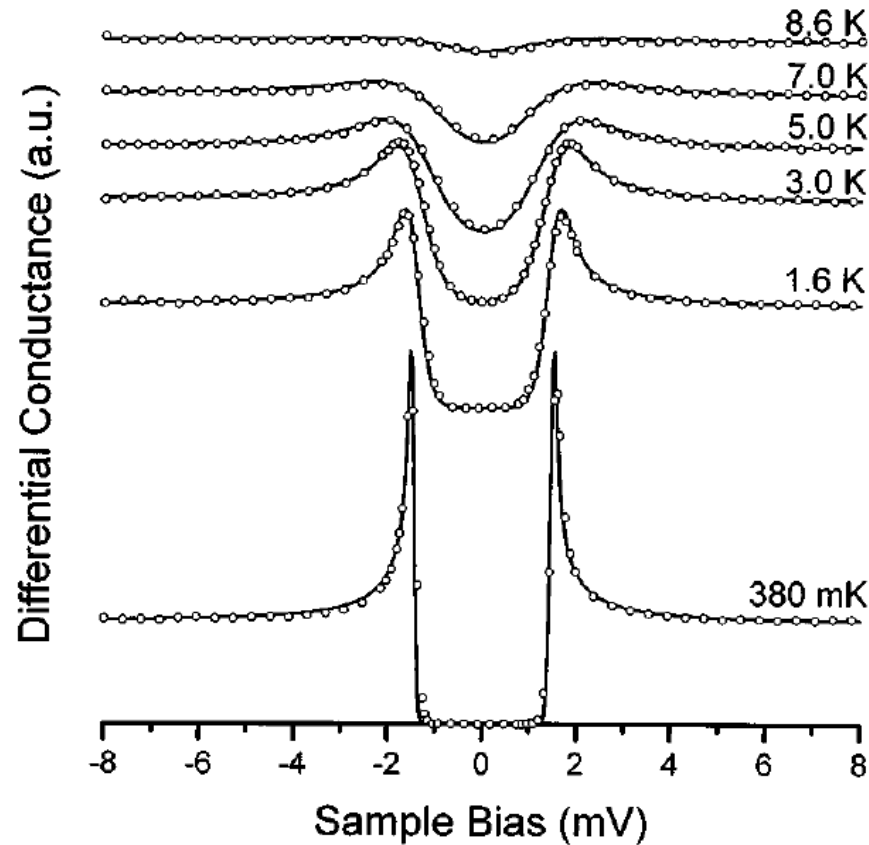


FIG. 1. Tunnel current between Al and Pb through Al_2O_3 film as a function of voltage. (1) $T=4.2^\circ\text{K}$ and 1.6°K , $H=2.7$ koe (Pb normal). (2) $T=4.2^\circ\text{K}$, $H=0.8$ koe. (3) $T=1.6^\circ\text{K}$, $H=0.8$ koe. (4) $T=4.2^\circ\text{K}$, $H=0$ (Pb superconducting). (5) $T=1.6^\circ\text{K}$, $H=0$ (Pb superconducting).

Elektronentunneln: Normalleiter - Supraleiter

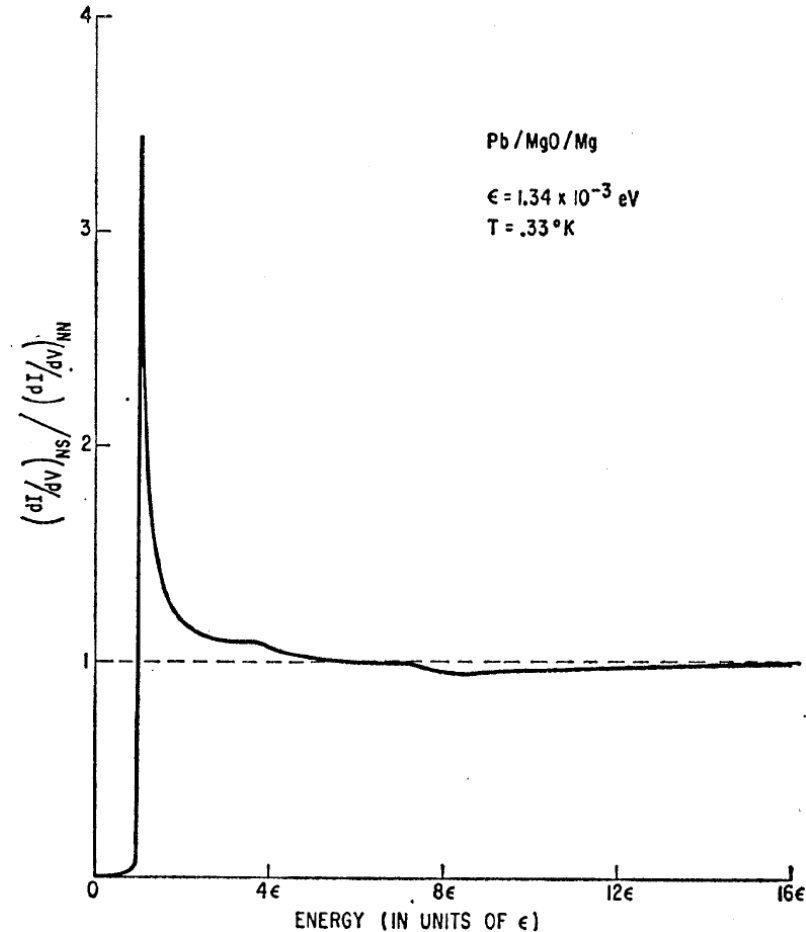
Nb, $T_c \sim 9\text{K}$ (Superconductor) - Vacuum - Au (Metal)



S. H. Pan, E. W. Hudson, J. C. Davis
Appl. Phys. Lett. 73, 2992 (1998)

Normal metal-insulator-superconductor junction: Strong electron-phonon coupling

Pb/MgO/Mg



I. Giaever, H.R. Hart, K. Megerle, Phys. Rev. **126**, 941 (1962)

Pb/AlO/Al

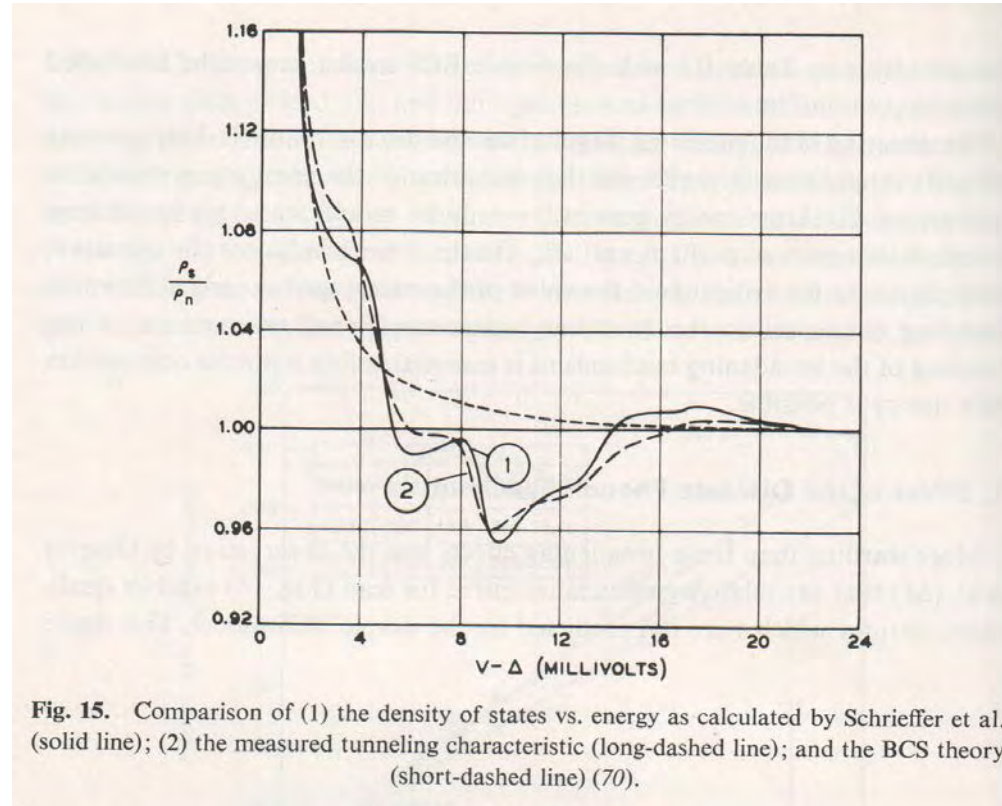


Fig. 15. Comparison of (1) the density of states vs. energy as calculated by Schrieffer et al. (solid line); (2) the measured tunneling characteristic (long-dashed line); and the BCS theory (short-dashed line) (70).

J.M. Rowell, P.W. Anderson, D.E. Thomas, Phys. Rev. Lett. **10**, 334 (1963)
 J. R. Schrieffer, D.J. Scalapino, J.W. Wilkins, Phys. Rev. Lett. **10**, 336 (1963);
 Phys. Rev. **148**, 263 (1966)

Normal metal-insulator-superconductor junction: Strong electron-phonon coupling

Idea: phonon spectrum causes fine structure
→ Eliashberg-Theory
Zh. Eksperim.: Theor. Fiz. 38, 966 (1960)
Soviet Phys. JETP 11, 696 (1960)

